# Theoretically motivated dark electromagnetism as the origin of relativistic MOND

- A status report -

## Tejinder P. Singh

Tata Institute of Fundamental Research, Mumbai

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References: arXiv: 2312.08811 [gr-qc], 2508.10131 [hep-ph]

# Milgrom's MOND vs ACDM

- Why is there a critical acceleration scale  $a_0$  in galaxy rotation curves?
- Why is this acceleration scale numerically close to the observed cosmic acceleration?
- Modeled by MOND: a new scale invariant theory of dynamics (gravity/inertia) involving a new constant  $a_0$  (besides  $G_N$ ).

Standard limit  $(a_0 \rightarrow 0)$ : Newtonian limit

Scale invariance :  $(t, \mathbf{r}) \to \lambda(t, \mathbf{r})$  ; deep MOND limit :  $(a_0 \to \infty, G_N \to 0)$ 

Instead of F = ma,  $F = GMm/r^2$ ; MOND proposes

$$F=ma^2/a_0, \quad F=GMm/r^2$$
 OR  $F=ma, \quad F\propto \frac{m(GMa_0)^{1/2}}{r}$ 

# Milgrom's MOND vs ACDM

- Because of scale invariance, MOND predicts flat rotation curves (RAR) asymptotically obeying the baryonic Tully-Fisher relation (BTFR).
- MOND shares its scale invariance property with deSitter spacetime.
- $\Lambda CDM$  does better than MOND in explaining galaxy cluster dynamics, linear growth of perturbations and CMB anisotropies, and BAO.
- Therefore, we seek a hybrid relativistic (MOND + CDM) model which obeys deSitter scale invariance.
- Such a hybrid model should come from a perturbatively renormalizable underlying quantum field theory.
- CDM should dominate at high accelerations; MOND dominates at low accelerations.

# An $E_{6L} \times E_{6R}$ theory of unification [arXiv:2206.06911]

Concurrent with the electroweak symmetry breaking:

$$E_{6L} \to SU(3)_c \times SU(3)_{F,L} \times SU(3)_L \xrightarrow{SU(3)_L} SU(2)_L \times U(1)_Y \xrightarrow{U(1)_Y} U(1)_{em}$$

$$E_{6R} \to SU(3)_{c'} \times SU(3)_{F,R} \times SU(3)_R \xrightarrow{SU(3)_R} SU(2)_R \times U(1)_Y \xrightarrow{U(1)_{Y'}} U(1)_{dem}$$

The RH sector introduces two new unbroken gauge symmetries: strong gravity  $SU(3)_{c'}$  and dark electromagnetism  $U(1)_{dem}$ :  $\pm \sqrt{m/\kappa}$ 

 $SU(3)_{F,L} \& SU(3)_{F,R}$  are global flavor symmetries [flavor / mass eigenstates]

These, along with  $U(1)_{em} \ \& \ U(1)_{dem}$  explain the observed mass-hierarchy

[arXiv:2508.10131 [hep-ph]]

 $SU(2)_R$  when broken, gives rise to GR and also to MOND, as we now see:

# GR and MOND from a broken $SU(2)_R$ symmetry

### 1 Symmetry structure and breaking

**Left sector.**  $E_6^L \to SU(3)_c \times SU(3)_F \times SU(3)_L$  (visible quarks/leptons originate here).

**Right sector.**  $E_6^R \to SU(3)'_c \times SU(3)'_F \times SU(3)_R \to SU(2)_R \times U(1)_{Y'} \to U(1)_{\text{dem}}$ . The unbroken  $U(1)_{\text{dem}}$  generator  $S_{\text{dem}}$  has eigenvalues  $s = \pm \sqrt{m/\kappa}$ ; in the late Universe the +s sector dominates. The  $U(1)_{\text{dem}}$  Lagrangian is ordinary Maxwell, hence like signs repel; it is not the MOND mediator and is kept subleading in late-time dynamics.

## 2 Gauge gravity from $SU(2)_R$

Let  $\omega^i_{\mu}$  be the  $SU(2)_R$  connection with curvature  $F^i = d\omega^i + \frac{1}{2}\epsilon^i_{jk}\omega^j \wedge \omega^k$ . The fundamental seed is BF+constraints:

$$S_{\text{BF+cons}}^{R} = \frac{1}{8\pi G} \int B^{i} \wedge F^{i} + \int \lambda_{ij} B^{i} \wedge B^{j} + S_{\text{trans}}[\text{Higgs}_{R}], \tag{1}$$

where the algebraic multipliers  $\lambda_{ij}$  enforce the simplicity constraints  $B^i = \frac{1}{2} \epsilon^i{}_{jk} e^j \wedge e^k$ . After soldering, (1) reduces to Einstein gravity for  $g_{\mu\nu} = e^I{}_{\mu} e^J{}_{\nu} \eta_{IJ}$ . No extra propagating fields are added beyond those in  $E_6^R$ .

# GR and MOND from a broken $SU(2)_R$ symmetry

#### 3 De Sitter IR vacuum and the MOND scale

We impose that the deep IR of the  $SU(2)_R$  sector realizes de Sitter kinematics with radius  $\ell_{dS}$ . Scale invariance then selects a single acceleration

$$a_0 = \frac{c^2}{\xi \,\ell_{\rm dS}} \qquad (\xi = \mathcal{O}(1)). \tag{2}$$

## 4 Metric-only IR functional and $r_{\rm eff}$

We add to (1) a metric-only IR piece fixed by dS scaling:

$$S_{\rm IR}[g] = rac{a_0^2}{16\pi G} \int d^4x \sqrt{-g} \ F\left(rac{I[g]}{a_0^2}
ight), \qquad I[g] \equiv a_\mu a^\mu, \quad a_\mu \equiv \nabla_\mu \ln N, \ N \equiv \sqrt{-g_{00}}.$$
 (3)

In the static weak-field limit  $g_{00} = -(1 + 2\Phi)$ , so  $I \to |\nabla \Phi|^2$ . As a geometric bookkeeping of the cosmological tie we use the *effective distance* (R proper distance in FRW,  $R_H = a/\dot{a}$ ):

$$r_{\text{eff}}^2 = R(t) R_H(t), \tag{4}$$

and evaluate static spatial derivatives w.r.t.  $r_{\text{eff}}$ . In deep MOND we freeze  $R_H \to R_{H0}$  so that  $a_0$  is epoch-independent in galaxies, while the background retains dS kinematics.

Uniqueness (asymptotics). dS scale invariance and GR matching fix

$$F(y) \to y \quad (y \gg 1), \qquad F(y) \to \frac{2}{3}y^{3/2} \quad (y \ll 1).$$
 (5)

An exactly integrable choice consistent with (5) and the interpolating function  $\mu(x) = x/(1+x)$  is

$$F(y) = y - 2\sqrt{y} + 2\ln(1 + \sqrt{y}), \qquad (6)$$

which has no tunable parameter beyond  $a_0$ .

#### 5 Field equations and static MOND

Varying  $S_{\text{BF+cons}}^{R} + S_{\text{IR}} + S_{\text{dem}} + S_{\text{matter}}$  gives

$$G_{\mu\nu} + \Xi_{\mu\nu}[g; F, a_0] = 8\pi G \left(T_{\mu\nu}^{\text{matter}} + T_{\mu\nu}^{\text{dem}}\right).$$
 (7)

With  $y = I/a_0^2$  and  $F_y \equiv dF/dy$  one finds (schematically)

$$\Xi_{\mu\nu} = \frac{a_0^2}{2} \Big[ (F - 2yF_y)g_{\mu\nu} + 2F_y a_\mu a_\nu \Big] - a_0^2 \Big[ \nabla_{(\mu}(F_y a_{\nu)}) - g_{\mu\nu} \nabla_\alpha(F_y a^\alpha) \Big]. \tag{8}$$

The static weak-field limit yields the Bekenstein-Milgrom equation written with  $r_{\text{eff}}$ :

$$\nabla_{\text{eff}} \cdot \left[ \mu \left( \frac{|\nabla_{\text{eff}} \Phi|}{a_0} \right) \nabla_{\text{eff}} \Phi \right] = 4\pi G \rho, \qquad \mu(x) = F'(x^2). \tag{9}$$

For spherical symmetry one may use the algebraic map

$$g(r) = \frac{1}{2} \left[ g_N(r) + \sqrt{g_N^2(r) + 4a_0 g_N(r)} \right], \qquad g_N = \frac{GM_N(\langle r) \rangle}{r^2}, \tag{10}$$

which immediately gives the baryonic Tully–Fisher relation  $v^4 = Ga_0M_b$  in the deep-MOND regime.

#### 6 FRW background and perturbations

In cosmic time  $N=1 \Rightarrow a_{\mu}=0$ , so  $S_{\rm IR}$  does not alter the homogeneous background:

$$H^{2} = \frac{8\pi G}{3}\rho - \frac{kc^{2}}{a^{2}} + \frac{\Lambda_{\text{eff}}}{3}, \qquad \Lambda_{\text{eff}} = \frac{3c^{2}}{\ell_{\text{dS}}^{2}} = \frac{3\xi^{2}a_{0}^{2}}{c^{2}}.$$
 (11)

Perturb in Newtonian gauge  $ds^2 = -(1+2\Phi)dt^2 + a^2(1-2\Psi)d\mathbf{x}^2$ . In the quasi-static regime there is no slip  $(\Psi = \Phi)$  and the Poisson closure reads

$$-k^{2}\Phi = 4\pi G a^{2} \mu_{\cos}(k, a) \delta \rho, \qquad \mu_{\cos}(k, a) \simeq 1 + \frac{1}{1 + (k_{\star}/k)^{p}} \frac{g_{N}}{a_{0}}, \quad k_{\star} = \alpha \, aH, \tag{12}$$

with  $(\alpha, p) \sim (3, 4)$  implementing the horizon taper. Matter growth obeys

$$\ddot{\delta} + 2H\dot{\delta} - 4\pi G \,\mu_{\cos}\,\bar{\rho}\,\delta = 0. \tag{13}$$

A useful approximation is  $f \equiv d \ln D/d \ln a \simeq \Omega_m^{\gamma}$  with  $\gamma \simeq 0.55 - 0.05[\mu_{\cos}(k, a) - 1]$  on subhorizon scales.

## 7 Why MOND+ $\chi_R$ is superior to pure MOND

- CMB & BAO: primary peaks at  $z \sim 1100$  require a pressureless component unless recombination physics is altered.
- Clusters: MOND reduces but does not remove the mass deficit; a collisionless component fits cores and mergers.
- LSS: MOND enhances late growth (good for early massive galaxies) but a cold component is needed for BAO and large-scale power.

We keep one minimal,  $E_6^R$ -native collisionless species without spoiling galaxy MOND.

# 8 A right-handed cold component from $E_6^R$

In trinification, one family of the **27** contains  $L_R \sim (1, \bar{3}', 3_R)$  under  $SU(3)'_c \times SU(3)'_F \times SU(3)_R$ . After  $SU(3)_{F,R} \to SU(2)_{F,R} \times U(1)$  there is an (1,1) SM singlet  $\chi_R$  with  $Y'(\chi_R) = T_{3R}(\chi_R) = 0$ , hence  $Q_{\text{dem}}(\chi_R) = 0$  (no dark-electromagnetic force). A Dirac/Majorana mass  $m_\chi \simeq y_\chi v_R$  follows from the same RH Higgs that breaks  $SU(3)_R$ , with  $v_R$  few-tens of TeV  $\Rightarrow m_\chi \sim 10^2-10^3$  GeV for  $y_\chi = \mathcal{O}(0.1-1)$ . Annihilation via heavy  $Z_R/W_R$  gives the correct relic for  $M_{Z_R}/g_R = \mathcal{O}(10 \text{ TeV})$ ; direct detection is suppressed by small L-R mixings, consistent with current bounds.

Quantitative coexistence prior (for RCs). Impose inside  $r_M = \sqrt{GM_b/a_0}$ 

$$\boxed{\frac{g_{N,\chi}}{g_{N,b}} \le \varepsilon \quad (r \in [2,4]R_d), \quad \varepsilon \simeq 0.1-0.2} \quad \iff \quad M_{\chi}(< r_M) \le \varepsilon M_b(< r_M). \tag{14}$$

This keeps galaxies MOND-dominated while allowing a diffuse/cored  $\chi_R$  halo for clusters and the CMB.

## 9 Analytic expectations for LSS and CMB in the hybrid

#### Linear growth

For subhorizon  $k \gg k_{\star}$  and epochs with typical accelerations below  $a_0$ , take  $\mu_{\cos} \approx 1 + \epsilon(a)$  with  $\epsilon \lesssim \mathcal{O}(0.1)$ . Solving (13) gives  $D(a) \approx D_{\Lambda\text{CDM}}(a) \exp\left[\frac{3}{5}\int \epsilon(a)\Omega_m(a) d \ln a\right]$ , so D is enhanced by a few percent to  $\sim 10\%$  by  $z \sim 1$  (scale-dependent via  $k_{\star}$ ).

#### CMB anisotropy and lensing

Primary anisotropies (last scattering) are GR-like. The change is late-time: (i) low- $\ell$  TT gets a positive ISW shift from  $\dot{\Phi} \neq 0$  as growth is enhanced; (ii) lensing potential  $C_L^{\phi\phi}$  increases at the percent level due to the larger D(a) along the line of sight. These features match the CLASS runs (TT suppression at high  $\ell$  from added smoothing; low- $\ell$  enhancement).

• Clusters, Spirals, Dwarfs/LSB: work in progress.

In preparation: General Relativity and Relativistic MOND from broken  $SU(2)_R imes U(1)_{Y'}$ 

#### THANK YOU FOR YOUR ATTENTION!