

Jet Quenching in Holographic QCD in Vicinity of the 1-st Order Phase Transitions

Pavel Slepov

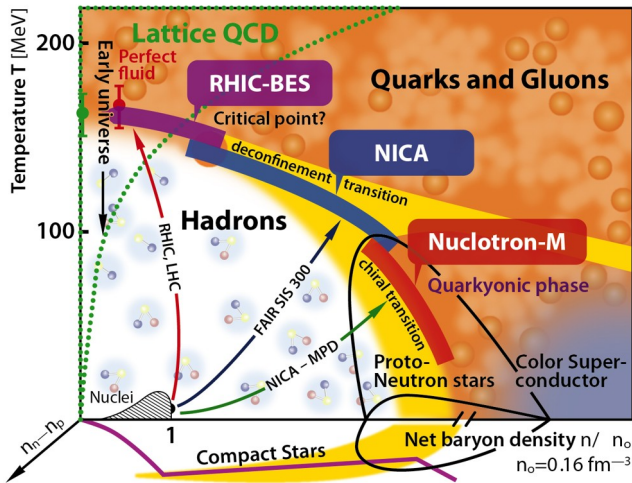
Based on arXiv:2507.19426 with I.Ya.Aref'eva, A.Hajilou and A.Nikolaev

Steklov Mathematical Institute of Russian Academy of Sciences

22nd Lomonosov Conference on Elementary Particle Physics

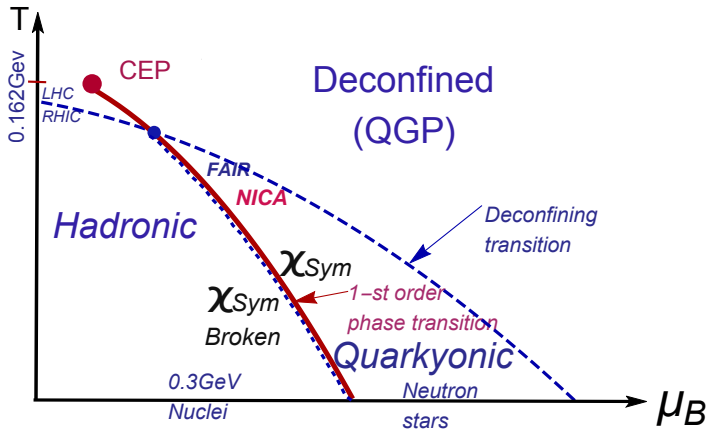
25.08.2025

Studies of QCD Phase Diagram is the main goal of new facilities



From: <https://nica.jinr.ru/physics.php>

Holographic QCD phase diagram for light quarks



The main question to discuss is: what directly measurable quantities indicate the presence of 1-st order phase transitions?

- Jet Quenching – this talk
- Direct photons – I.Ya. Aref'eva, A. Ermakov and P. S.,
"Direct photons emission rate ... with first-order phase
transition," EPJC **82** (2022) 85
- Energy loss – I.Ya. Aref'eva, K. Rannu and P. S.,
"Energy Loss in Holographic Anisotropic Model ...,"
arXiv:2012.05758; TMPH **206** (2021) 400
- Cross-sections – I.Ya.Aref'eva, A. Hajilou, P. S. and M. Usova,
"Running coupling for HQCD...: Isotropic case,"
PRD **110** (2024) 126009
I.Ya. Aref'eva, A. Hajilou, A. Nikolaev and P. S.,
"HQCD running coupling ... in strong magnetic field,"
PRD **110** (2024) 086021

Holographic model of an anisotropic plasma in a magnetic field at a non-zero chemical potential

I.Aref'eva, K.Rannu'18; I Aref'eva, K. Rannu, P.S.'21

$$S = \int d^5x \sqrt{-g} \left[R - \frac{f_1(\phi)}{4} F_{(1)}^2 - \frac{f_2(\phi)}{4} F_{(2)}^2 - \frac{f_B(\phi)}{4} F_{(B)}^2 - \frac{1}{2} \partial_M \phi \partial^M \phi - V(\phi) \right]$$

$$ds^2 = \frac{L^2}{z^2} \mathfrak{b}(z) \left[-g(z) dt^2 + dx^2 + \left(\frac{z}{L} \right)^{2-\frac{2}{\nu}} dy_1^2 + e^{c_B} z^2 \left(\frac{z}{L} \right)^{2-\frac{2}{\nu}} dy_2^2 + \frac{dz^2}{g(z)} \right]$$

$$A_{(1)\mu} = A_t(z) \delta_\mu^0 \quad A_t(0) = \mu \quad F_{(2)} = dy^1 \wedge dy^2 \quad F_{(B)} = dx \wedge dy^1$$

Giataanas'13; Aref'eva, Golubtsova'14; Gürsoy, Järvinen '19; Dudal et al.'19

$$\mathfrak{b}(z) = e^{2\mathcal{A}(z)} \Leftrightarrow \text{quarks mass}$$

“Bottom-up approach”

Heavy quarks (c, b):

$$\mathcal{A}(z) = -cz^2/4$$

$$\mathcal{A}(z) = -cz^2/4 + p(c_B)z^4$$

Andreev, Zakharov'06

Aref'eva, Hajilou, Rannu, P.S.'23

Light quarks (u, d, s)

$$\mathcal{A}(z) = -a \ln(bz^2 + 1)$$

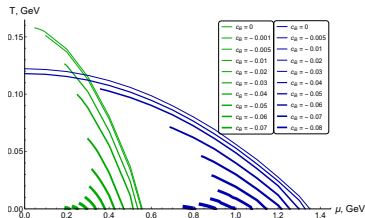
$$\mathcal{A}(z) = -a \ln((bz^2 + 1)(dz^4 + 1))$$

Li, Yang, Yuan'17

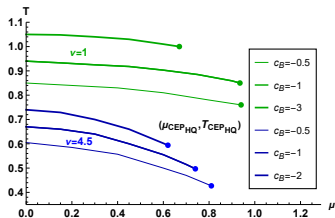
Zhu, Chen, Zhou, Zhang, Huang'25

1-st order phase transition for “light” and “heavy” quarks in Holography

Light quarks



Heavy quarks

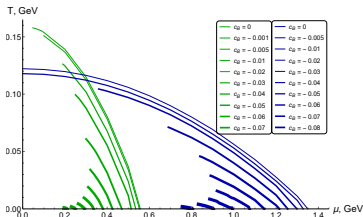


Aref'eva, Ermakov, Rannu, P.S., EPJC'23

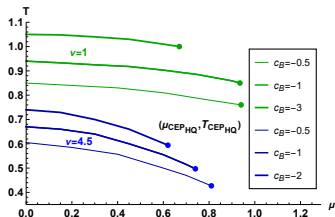
Aref'eva, Hajilou, Rannu, P.S., EPJC'23

1-st order phase transition for “light” and “heavy” quarks in Holography

Light quarks



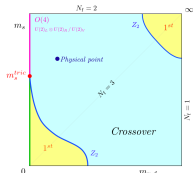
Heavy quarks



Aref'eva, Ermakov, Rannu, P.S., EPJC'23

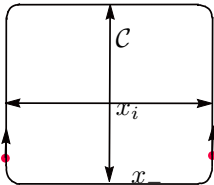
Aref'eva, Hajilou, Rannu, P.S., EPJC'23

- QCD Phase Diagram from Lattice Columbia plot
Brown et al. '90 Philipsen, Pinke'16
- Main problem on Lattice: $\mu \neq 0$



Jet quenching

- The jet quenching parameter q quantifies the average transverse momentum squared that a parton transfers to the medium per unit of path length.
- **Light-like loop** $\mathcal{C} = x_- \times x_i$, $x_- \gg x_i > \ell_{QCD}$,
 $i = 2, 3$



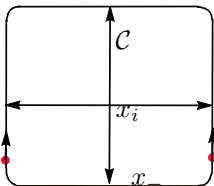
$$\langle W_{Ad}[\mathcal{C}] \rangle \underset{x_i \rightarrow 0}{\underset{x_- \rightarrow \infty}{\sim}} e^{-q x_- x_i^2}$$

q - jet quenching
parameter

Jet quenching

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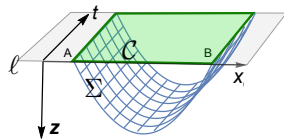


$$\langle W_{Ad}[\mathcal{C}] \rangle \underset{x_i \rightarrow 0}{\underset{x_- \rightarrow \infty} \sim} e^{-q x_- x_i^2}$$

q - jet quenching parameter

- Wilson Loops in holographic QCD

J. Maldacena'98



- String action "on a barn": $S_{NG} = \int d\tau d\xi M(z(\xi)) \sqrt{\mathcal{F}(z(\xi)) + (z'(\xi))^2}$

H. Liu, K. Rajagopal, U. Wiedemann,'06 Conformal case: $q \sim T^3$

Light-like Wilson loops in a deformed metric

$$ds^2 = \frac{L^2 e^{2A_s}}{z^2} \left(-g(z) dt^2 + dx_1^2 + \left(\frac{z}{L} \right)^{2-2/\nu} \left(dx_2^2 + e^{c_B z^2} dx_3^2 \right) + \frac{dz^2}{g(z)} \right)$$

$$dt = \frac{dx_+ + dx_-}{\sqrt{2}}, \quad dx_1 = \frac{dx_+ - dx_-}{\sqrt{2}}.$$

The contour $\mathcal{C}$: “short sides” with length ℓ along the x_3 (or x_2) direction and the “long sides” with length L_- along the x_- direction

$$x_- = \tau; \quad x_3(\text{or } x_2) = \xi$$

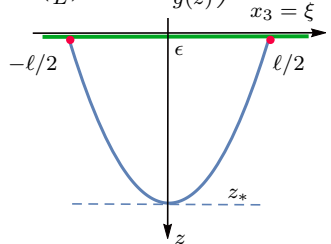
$$S_{NG,3} = \frac{L^2 L_-}{\pi \alpha'} \int_0^{\frac{\ell}{2}} d\xi \frac{e^{2A_s(z)}}{z^2} \sqrt{\frac{1-g(z)}{2} \left(e^{c_B z^2} \left(\frac{z}{L} \right)^{2-2/\nu} + \frac{z'^2}{g(z)} \right)}$$

The integral of motion

$$P = \frac{e^{2A_s(z)}(g(z) - 1)}{\sqrt{2} z^2 g(z) \sqrt{(1-g(z)) \left(e^{c_B z^2} \left(\frac{z}{L} \right)^{2-2/\nu} + \frac{z'^2}{g(z)} \right)}}$$

and we get for z'

$$z' = \frac{e^{2A_s + c_B z^2} \left(\frac{z}{L} \right)^{-2/\nu}}{\sqrt{2} L^2 P} \sqrt{g(1-g) - 2g L^2 P^2 z^2 \left(\frac{z}{L} \right)^{2/\nu} e^{-4A_s - c_B z^2}}$$



Light-like Wilson loops in a deformed metric

"Returning point":

$$\underbrace{g(z_*) \left((1 - g(z_*)) e^{4A_s + c_B z_*^2} - 2L^2 P^2 z_*^2 \left(\frac{z_*}{L} \right)^{2/\nu} \right)}_{\mathcal{I}} = 0 \quad (*)$$

Equation (*) has two possible solutions:

- a) $g(z_*) = 0$, this holds for $z_* = z_h$,
- b) $\mathcal{I} = 0$, in our case is unstable

● a) $z_* = z_h$.

$$\begin{aligned} \frac{\ell}{2} &= PL^2 \int_0^{z_h} \frac{\sqrt{2} e^{-2A_s - c_B z^2} \left(\frac{z}{L} \right)^{2/\nu}}{\sqrt{g(1-g)}} dz + \dots \\ \frac{\mathcal{S}}{2} &= S_0 + L^2 P^2 \int_0^{z_h} \frac{e^{-2A_s(z) - c_B z^2} \left(\frac{z}{L} \right)^{2/\nu}}{\sqrt{2g(1-g)}} dz + \dots \end{aligned}$$

Jet quenching for non-zero magnetic field and initial anisotropy.

Analytical formula & Numerical results

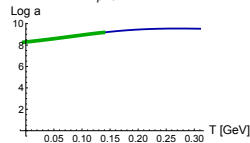
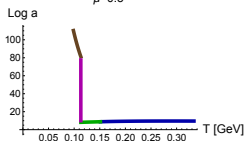
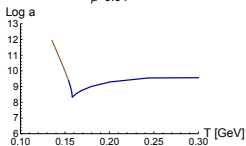
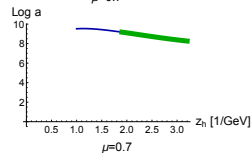
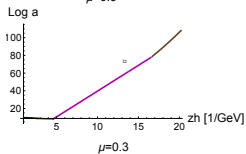
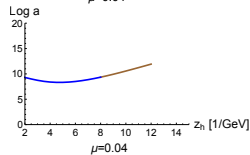
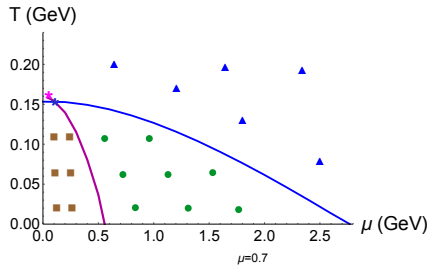
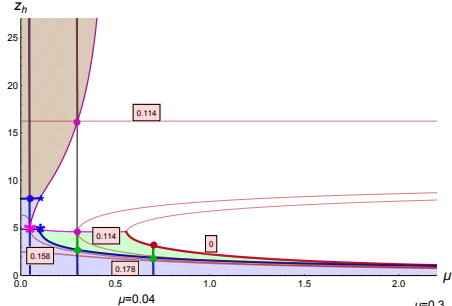
$$q_i(z_h, \mu, c_B, \nu) = \frac{L^2}{\pi \alpha' a_i} \sim \frac{1}{a_i}, \quad i = 2, 3$$

$$a_2 = \int_0^{z_h} \frac{e^{-2\mathcal{A}_s(z)} \left(\frac{z}{L}\right)^{2/\nu}}{\sqrt{g(z)(1-g(z))}} dz \quad a_3 = \int_0^{z_h} \frac{e^{-2\mathcal{A}_s(z) - c_B z^2} \left(\frac{z}{L}\right)^{2/\nu}}{\sqrt{g(z)(1-g(z))}} dz$$

$$g(z, z_h, \mu, c_B, \nu) = e^{c_B z^2} \left[1 - \frac{I_1(z)}{I_1(z_h)} + \frac{\mu^2 (2c - c_B) I_2(z)}{L^2 \left(1 - e^{(2c - c_B) z_h^2/2}\right)^2} \left(1 - \frac{I_1(z) I_2(z_h)}{I_1(z_h) I_2(z)}\right) \right]$$

$$I_1(z) = \int_0^z (1 + b\chi^2)^{3a} \frac{\chi^{1+\frac{2}{\nu}}}{e^{\frac{3}{2}c_B \chi^2}} d\chi, \quad I_2(z) = \int_0^z (1 + b\chi^2)^{3a} \frac{\chi^{1+\frac{2}{\nu}}}{e^{(-c+2c_B)\chi^2}} d\chi$$

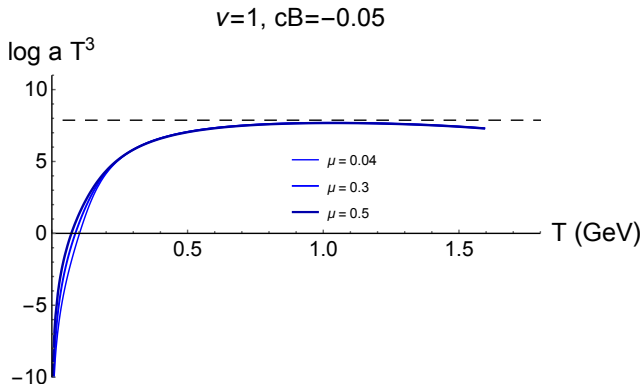
$$T = \frac{|g'|}{4\pi} \Big|_{z=z_h} \quad s = \left(\frac{L}{z_h}\right)^{1+\frac{2}{\nu}} \frac{e^{c_B z_h^2/2} (1 + b z_h^2)^{-3a}}{4} \quad F = \int_{z_h}^{z_{h2}} s dT = \int_{z_h}^{z_{h2}} s T' dz$$



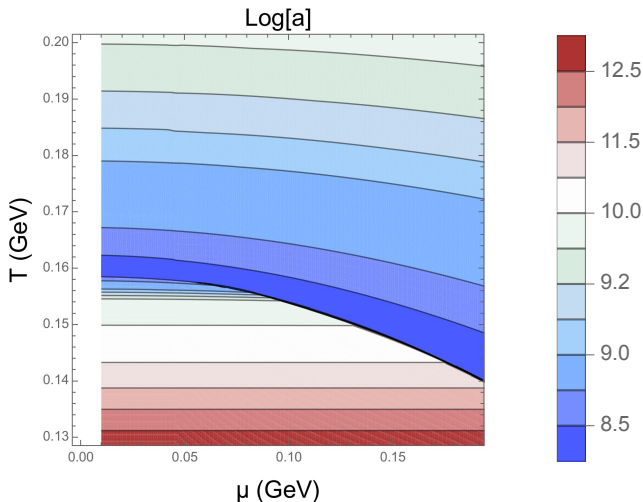
Non-monotonic behaviour of the jet quenching parameter

Early observed by M.Huang et al'14; Zhu, Hou'23

Jet quenching asymptotics at large T for LQ model

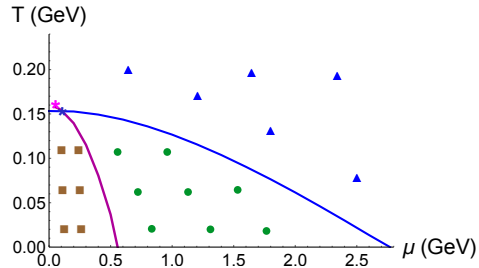
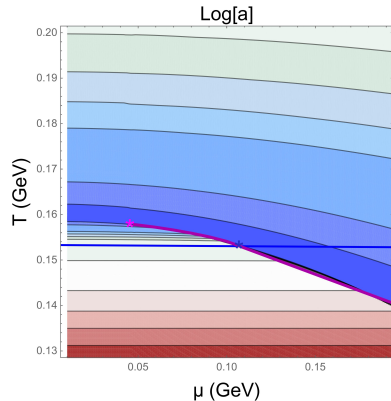


Jet quenching for zero magnetic field and $\nu = 1$ for LQ model. Numerical results

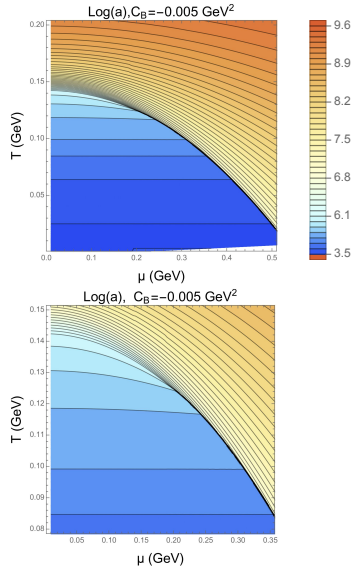


Density plots for $\log a$ for light quarks

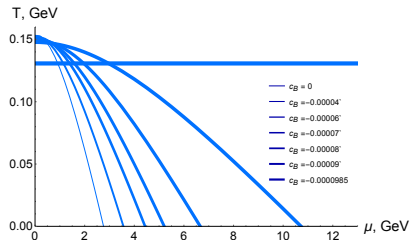
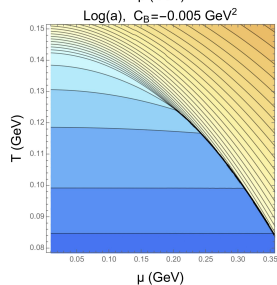
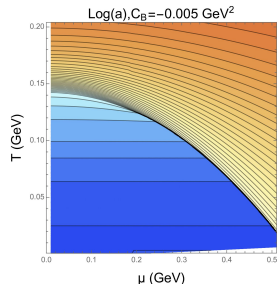
Jet quenching for zero magnetic field and $\nu = 1$ for LQ model. Numerical results



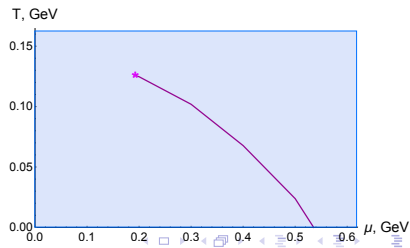
Jet quenching for non-zero magnetic field and $\nu = 1$ for LQ model. Numerical results for a_2



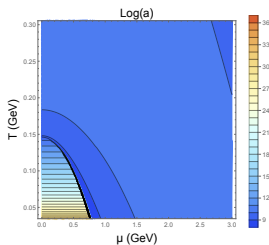
Jet quenching for non-zero magnetic field and $\nu = 1$ for LQ model. Numerical results for a_2



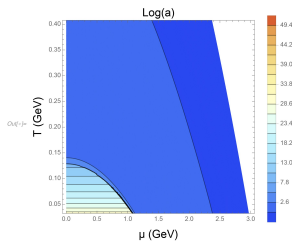
Conf/deconf. phase transition lines



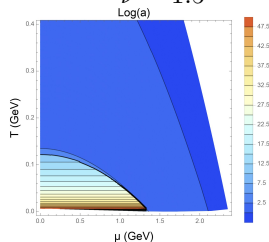
Jet quenching for non-trivial initial anisotropy and $c_B = 0$ for LQ model. Numerical results for a_2



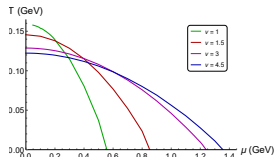
$\nu = 1.5$



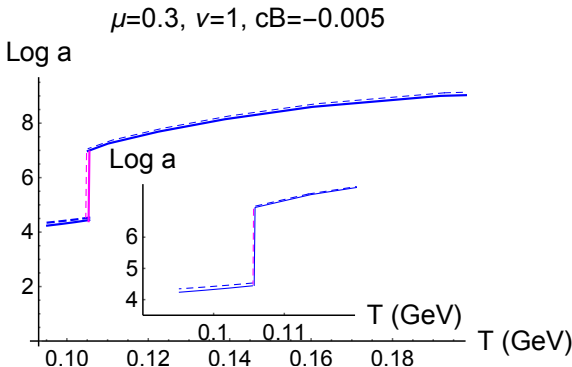
$\nu = 3$



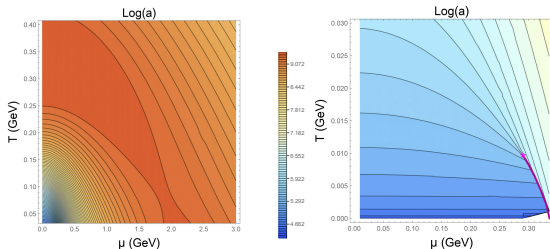
$\nu = 4.5$



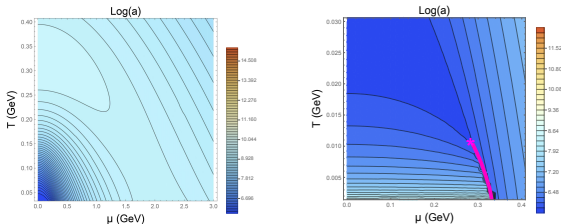
$\log a_2$ (solid lines) and $\log a_3$ (dashed lines) for LQ model with $\nu = 1$ and $c_B = -0.005$



Jet quenching for $c_B = -0.05$ and $\nu = 1$ for LQ model. Numerical results for a_2 and a_3



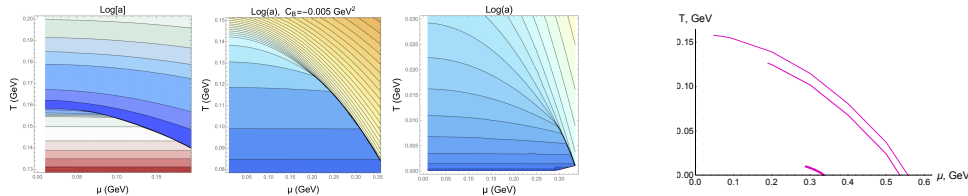
a_2 orientation



a_3 orientation

Conclusion

- Jet quenching parameter can serve as an indicator of the 1-st order phase transitions



Plots for the light quarks model

- Change in the slope of $\log(a)$ versus temperature T (at fixed μ) at the confinement/deconfinement phase transition line
- There is no strong orientation dependence near 1-st order phase transitions
- Similar behavior is observed in the heavy quark model

Open question:

- *Hybrid holographic model for light and heavy quarks*

Thank you for your attention!