

# Semileptonic $B$ -decays at Belle and Belle II

22<sup>nd</sup> Lomonosov Conference on Elementary Particle Physics

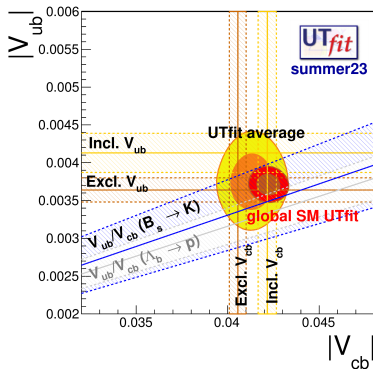
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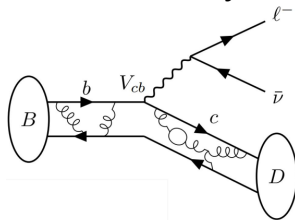
# Motivation



$$|V_{qb}| = \sqrt{\frac{\mathcal{B}(B \rightarrow X_q \ell \nu_\ell)}{\tau_B \Gamma(B \rightarrow X_q \ell \nu_\ell)}}$$

Tension between inclusive and exclusive  $V_{qb}$  measurements  $2 - 3\sigma$

Precise measurements important to constrain **CKM Unitarity**

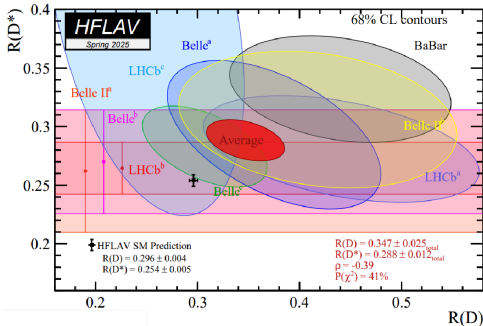


Direct information on  $V_{cb}$  and  $V_{ub}$  can be extracted from **semileptonic decay rate** exclusively or inclusively

**Experimentally measured branching fraction**

**Predicted partial rate sans CKM factors (with  $V_{qb}$  set to 1)**

# Motivation



- In the Standard Model (SM), the  $W$ -boson couples equally to  $\tau, \mu, e$  Lepton-Flavor Universality (LFU)
- Semileptonic  $B$  decays are sensitive to new physics beyond SM
- Ratio measurements provide stringent LFU tests: branching fractions, angular asymmetry

- Measurement of ratio leads to partial cancellation of theoretical and experimental uncertainties

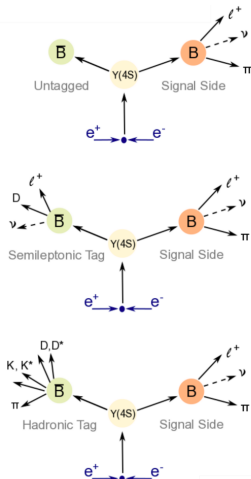
$$R(X_{\tau/\ell}) = \frac{\mathcal{B}(B \rightarrow X\tau\nu)}{\mathcal{B}(B \rightarrow X\ell\nu)}; \ell = e, \mu$$

**Tension of  $R(D_{\tau/\ell}^{(*)})$  with SM  $\sim 3.1\sigma$**

# Kinematics at $B$ -factories

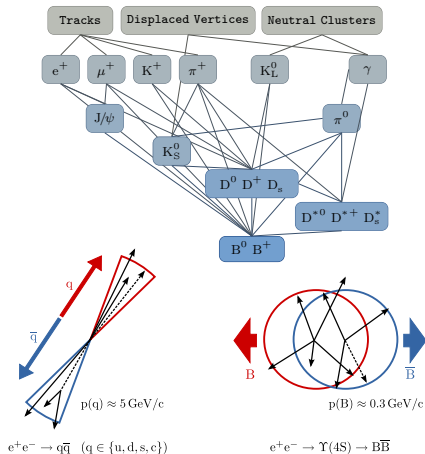



purity  
 efficiency



Strategy for event tagging

## Schematic Overview of Full Event Interpretation



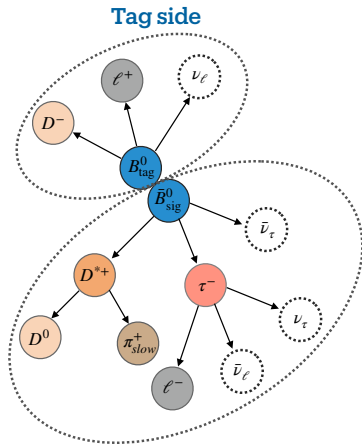
Event topology in  $\Upsilon(4S)$  frame

Test of lepton flavor universality with  
measurements of  $R(D^+)$  and  $R(D^{*+})$  using  
semileptonic B tagging at the Belle II experiment

$$R(D_{\tau/\ell}^{(*)+}) = \frac{\mathcal{B}(B \rightarrow D^{(*)+} \tau \nu)}{\mathcal{B}(B \rightarrow D^{(*)+} \ell \nu)}; \ell = e, \mu$$

# $R(D^{(*)})$ : reconstruction

- First  $R(D^{(*)})$  Belle II measurement with **semileptonic  $B$  tagging**:  
 $B_{\text{tag}}^0 \rightarrow D^{(*)} \ell \nu_\ell$
- Neutral mode  $\Upsilon(4S) \rightarrow B^0 \bar{B}^0$  is studied
- Reconstruct  $B_{\text{sig}}^0$  candidates in  $D^+ \ell^-$  and  $D^* \ell^-$  final states not associated with the  $B_{\text{tag}}$  candidate
- $\tau$  decays identification from  
 $\tau^- \rightarrow \ell^- \bar{\nu}_\ell \nu_\tau$
- $D$  mesons reconstructed in multiple hadronic decays on both sides: **tag** side 26 decay modes, **signal** – 13
- Require  $\cos \theta_{BY}^{\text{tag}} \in [-1.75, 1.1]$  and  $\cos \theta_{BY}^{\text{sig}} \in [-15, 1.1]$

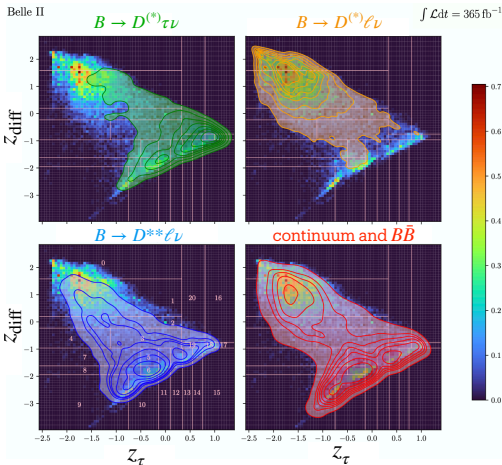


**Signal side**

$$\cos \theta_{BY} = \frac{2E_{\text{Beam}} E_Y - m_B^2 - m_Y^2}{2|\vec{p}_B| |\vec{p}_Y|},$$

$$Y = D^{(*)} \ell$$

# $R(D^{(*)})$ : analysis strategy



BDT used to separate the events in 3 different types:

1. **Semitauconic** signal events:  
 $B \rightarrow D^{(*)}\tau\nu$
2. **Semileptonic** events:  
 $B \rightarrow D^{(*)}\ell\nu$  and  $B \rightarrow D^{**}\ell\nu$
3. **Background** events:  
continuum and  $B\bar{B}$

BDT trained on five input variables:  
the most discriminating variables are  $\cos\theta_{BY}$  and  $E_{ECL}^{\text{extra}}$

Each event is assigned a BDT score:

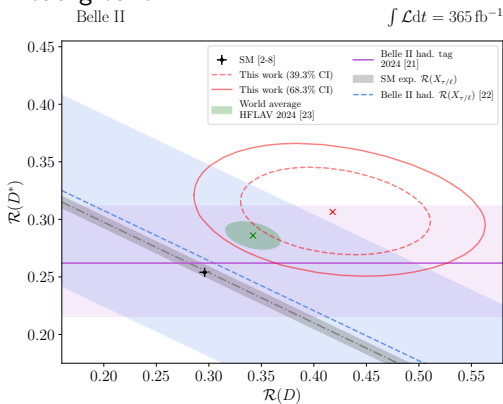
$$z_{\tau}, z_{\ell}, z_{\text{bkg}}$$

$$\text{Define } z_{\text{diff}} = z_{\ell} - z_{\text{bkg}}$$

Densities of four fit categories in  $(z_{\text{diff}}, z_{\tau})$  plane

# $R(D^{(*)})$ : results

- Extract signal and normalisation yields using a **2D binned likelihood fit** of  $z_\tau$  and  $z_{\text{diff}}$
- The fit is performed over 4 separate channels:  $D^+ e^-$ ,  $D^+ \mu^-$ ,  $D^{*+} e^-$ ,  $D^{*+} \mu^-$
- 10 fit parameters: 2 for the signal, 2 for the normalisation and 6 for the background



$$R(D_{\tau/\ell}^{*+}) = 0.306 \pm 0.034_{\text{stat}} \pm 0.018_{\text{syst}}$$

$$R(D_{\tau/\ell}^{+}) = 0.418 \pm 0.074_{\text{stat}} \pm 0.051_{\text{syst}}$$

**Tension** between the LFU-sensitive quantities  $R(D_{\tau/\ell}) - R(D_{\tau/\ell}^{*})$  and SM predictions **increases to  $3.8\sigma$**

$$R(D_{e/\mu}^{*+}) = 1.08 \pm 0.04_{\text{stat}} \pm 0.02_{\text{syst}}$$

$$R(D_{e/\mu}^{+}) = 1.07 \pm 0.05_{\text{stat}} \pm 0.02_{\text{syst}}$$

**Consistent with the SM within  $1.6\sigma - 1.2\sigma$**



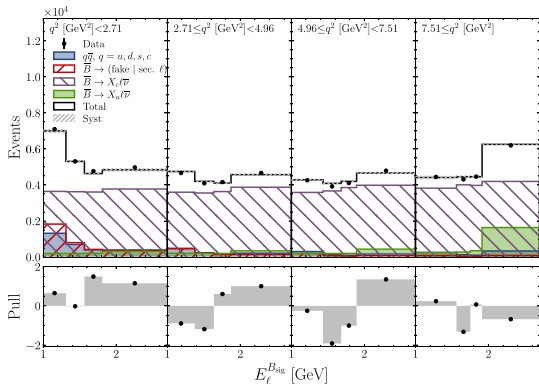
Measurement of the ratio of partial branching fraction of inclusive  $\bar{B} \rightarrow X_u \ell \bar{\nu}$  to  $\bar{B} \rightarrow X_c \ell \bar{\nu}$  and the ratio of their spectra with hadronic tagging

# $|V_{ub}|/|V_{cb}|$ : reconstruction

## Dataset and Tagging:

711 fb<sup>-1</sup> Belle data  
(772 × 10<sup>6</sup>  $B\bar{B}$  pairs) with improved Belle II hadronic tagging algorithm

- $K^+$  and  $K_S$  reconstruction for tagging  $b \rightarrow c$  decay
  - $N(K) > 0$  signal depleted sample for  $X_c \ell \nu$  decays
  - $N(K) = 0$  signal enhanced sample to extract signal yields
- Inclusive  $D^*$  reconstruction for  $b \rightarrow c$  veto via **soft pion** and **high  $M_{miss}^2$**



1D fit to  $E_\ell$  in  $u$ -depleted sample to get  $N^{X_{cl}\nu}$   
 2D fit to  $E_\ell \times q^2$  in  $u$ -enhanced sample to get  $N^{X_{ul}\nu}$

# $|V_{ub}|/|V_{cb}|$ : results

Unfolding  $B \rightarrow X_u \ell \nu$  and  $B \rightarrow X_c \ell \nu$  yields in ratio with corrected efficiencies

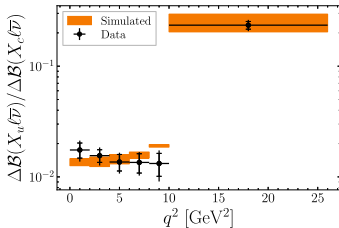
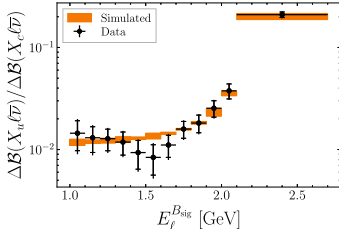
$$\frac{|V_{ub}|}{|V_{cb}|} = \sqrt{\frac{\Delta\mathcal{B}(B \rightarrow X_u \ell \nu) \Delta\Gamma(B \rightarrow X_c \ell \nu)}{\Delta\mathcal{B}(B \rightarrow X_c \ell \nu) \Delta\Gamma(B \rightarrow X_u \ell \nu)}}$$

Theory decay rates:

$$\Delta\Gamma^{\text{GGOU}}(B \rightarrow X_u \ell \nu) = 58.5^{+2.7}_{-2.3} \text{ ps}^{-1}$$

$$\Delta\Gamma^{\text{BLNP}}(B \rightarrow X_u \ell \nu) = 61.5^{+6.4}_{-5.1} \text{ ps}^{-1}$$

$$\Delta\Gamma^{\text{Kin}}(B \rightarrow X_c \ell \nu) = 29.7 \pm 1.2 \text{ ps}^{-1}$$



Branching fraction for BLNP and GGOU:

$$\frac{|V_{ub}|}{|V_{cb}|} = \left( 9.81 \pm 0.42_{\text{stat.}} \pm 0.38_{\text{syst.}} \pm 0.51_{\Delta\Gamma(B \rightarrow X_u \ell \nu)} \pm 0.20_{\Delta\Gamma(B \rightarrow X_c \ell \nu)} \right) \times 10^{-2}$$

$$\frac{|V_{ub}|}{|V_{cb}|} = \left( 10.06 \pm 0.43_{\text{stat.}} \pm 0.39_{\text{syst.}} \pm 0.23_{\Delta\Gamma(B \rightarrow X_u \ell \nu)} \pm 0.20_{\Delta\Gamma(B \rightarrow X_c \ell \nu)} \right) \times 10^{-2}$$

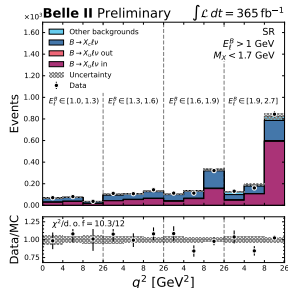
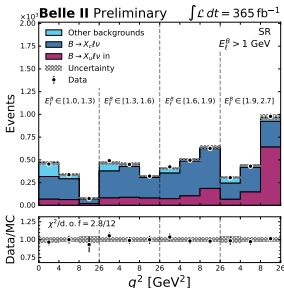
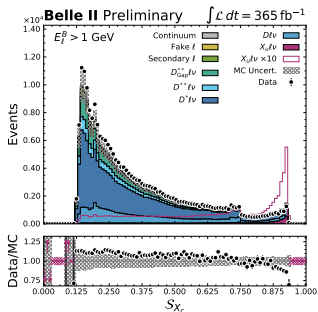
# Measurement of inclusive $B \rightarrow X_u \ell \nu$ partial branching fractions and $|V_{ub}|$ at Belle II

# $V_{ub}$ : reconstruction

- Hadronic tagging + reconstructed  $e$  or  $\mu$
- Neutrino characterised as missing energy
- Hadronic system  $X$  characterised from rest-of-event

## Background suppression

- Continuum suppression via a NN using Event Geometry variables
- $X_{c\ell\nu}$  suppression via a NN using the worse reconstruction of  $B \rightarrow X_{c\ell\nu}$  decays and low momentum  $\pi$  properties to reject  $B \rightarrow D^*\ell\nu$  decays + kaon veto



Analysis based on available kinematic constants:  
3 main kinematical variables to suppress  $X_{c\ell\nu}$ :

- $E_\ell(B)$  - lepton energy (in  $B_{\text{sig}}$  rest-frame)
- $M_X$  - mass of hadronic system
- $q^2$  - lepton neutrino system 4-momentum squared

Binned template fit with 3 components:  $X_{u\ell\nu}$ ,  $X_{c\ell\nu}$  – main background, others backgrounds – fake/secondary leptons + continuum

Simultaneous Fit with the control sample, to correct the shape of the  $X_{c\ell\nu}$  background

# $V_{ub}$ : results

Phase Space	Fit Variables
$E_\ell^B > 1 \text{ GeV}$	$E_\ell^B: q^2$
$E_\ell^B > 1 \text{ GeV}$ $M_X < 1.7 \text{ GeV}$	$E_\ell^B: q^2$
$E_\ell^B > 1 \text{ GeV}$ $M_X < 1.7 \text{ GeV}$ $q^2 > 8 \text{ GeV}^2$	$E_\ell^B$

3 different fits in the 3 different phase spaces to extract the signal strength

For **broadest phase-space** region with **most reliable theoretical prediction**:

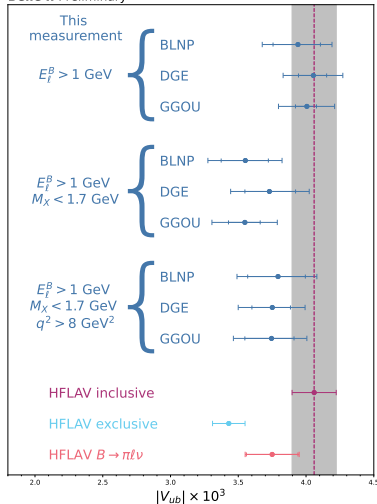
$$\Delta\mathcal{B}(B \rightarrow X_u \ell \nu) = (1.54 \pm 0.08 \pm 0.12) \times 10^{-3}$$

The obtained value of  $|V_{ub}|$  using a partial decay rate predicted by the GGOU framework is

$$|V_{ub}| = (4.01 \pm 0.11 \pm 0.16_{-0.07}^{+0.09}) \times 10^{-3}$$

Measurement is **competitive** with other measurements

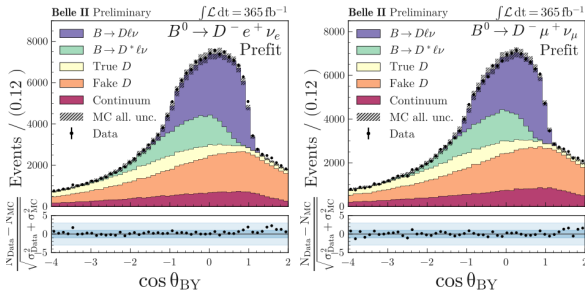
Belle II Preliminary



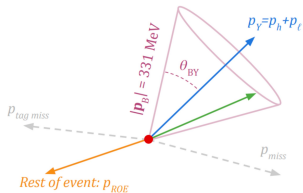
# Determination of $|V_{cb}|$ using $B \rightarrow D\ell\nu_\ell$ Decays at Belle II

# $V_{cb}$ : reconstruction

- Candidate  $B \rightarrow D\ell\nu$  formed from  $\ell(e, \mu)$  and  $D(\rightarrow K\pi, \rightarrow K\pi\pi)$
- Reduce experimental uncertainties due to isospin symmetry and separate analysis of  $B^0$  and  $B^+$  decays
- Inclusive reconstruction of neutrino momentum



Analysis based on available kinematic constants:



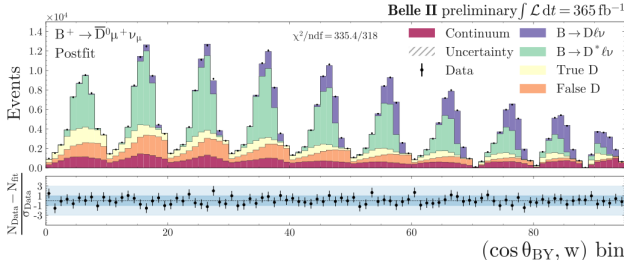
$$\cos \theta_{BY} = \frac{2E_{\text{Beam}} E_Y - m_B^2 - m_Y^2}{2|\vec{p}_B||\vec{p}_Y|}$$

$$w = \frac{m_B^2 + m_D^2 - q^2}{2m_B m_D}$$

Backgrounds:  $B \rightarrow D^* \ell \nu$ ; continuum events  
 $e^+ e^- \rightarrow q \bar{q}$ , ( $q = u, d, s, c$ )



# $V_{cb}$ : results

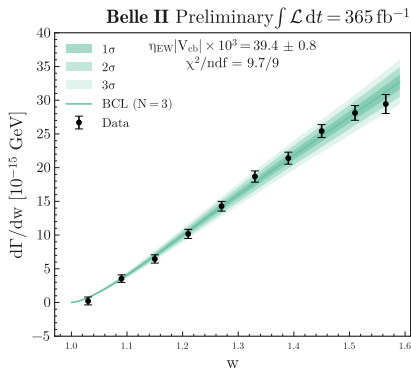


Branching fractions of each mode measured with fit on  $\cos \theta_{BY}$  in bins of  $w$

- $\mathcal{B}(B^0 \rightarrow D^- \ell^+ \nu_\ell) = (2.06 \pm 0.05(\text{stat.}) \pm 0.10(\text{sys.}))\%$
- $\mathcal{B}(B^+ \rightarrow \bar{D}^0 \ell^+ \nu_\ell) = (2.31 \pm 0.04(\text{stat.}) \pm 0.09(\text{sys.}))\%$

Fit differential decay rates using Bourrely-Caprini-Lellouch (BCL) form factor parameterization:  $|V_{cb}|_{\text{BCL}} = (39.2 \pm 0.4_{\text{stat.}} \pm 0.6_{\text{sys.}} \pm 0.5_{\text{th.}}) \times 10^{-3}$

Most precise measurement with  $B \rightarrow D \ell \nu_\ell$  data



# Conclusion

- Study of semileptonic decays is an important way to constraint and check SM parameters
- Many semileptonic B decay results from Belle (II)
  - $R(D^{(*)})$  LFU tests consistent with SM
  - Long-standing  $|V_{xb}|$  puzzle still remains
- Urge for further analysis
- Belle II starts new data taking in November 2025

# Additional slides

# $V_{cb}$ : charged mode reconstruction

