

SEARCHING FOR AXIAL NEUTRAL CURRENT NON-STANDARD INTERACTIONS OF NEUTRINOS BY DUNE-LIKE EXPERIMENTS

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IPM, Tehran



Outline of my talk

- [Part 1](#): Introduction and present bound
- [Part 2](#): Search for axial NSI by DUNE
- [Part 3](#): Bounds from MINOS and MINOS+

Neutral current Non-Standard Interaction (NSI)

$$\frac{G_F}{\sqrt{2}} [\bar{\nu}_\alpha \gamma^\mu (1 - \gamma_5) \nu_\beta] \left[\bar{f} \gamma_\mu \left(\epsilon_{\alpha\beta}^{Vf} + \epsilon_{\alpha\beta}^{Af} \gamma_5 \right) f \right] \quad \text{where } f \in \{e, u, d, s\},$$

Neutrino propagation in matter: Oscillation pattern

Coherent Elastic neutrino Nucleus Scattering $CE\nu NS$

Neutral current Non-Standard Interaction (NSI)

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Coherent Elastic neutrino Nucleus Scattering $CE\nu NS$

Neutral current Non-Standard Interaction (**NSI**)

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High energy scattering experiments
such as **CHARM** and **NuTeV**

Bounds from scattering experiments

From NuTeV : $|\epsilon_{\mu\mu}^{Au}| < 0.006$, $|\epsilon_{\mu\mu}^{Ad}| < 0.018$, $|\epsilon_{\mu\tau}^{Au}|, |\epsilon_{\mu\tau}^{Ad}| < 0.01$,

From CHARM : $|\epsilon_{ee}^{Au}| < 1$, $|\epsilon_{ee}^{Ad}| < 0.9$, $|\epsilon_{e\tau}^{Au}|, |\epsilon_{e\tau}^{Ad}| < 0.5$.

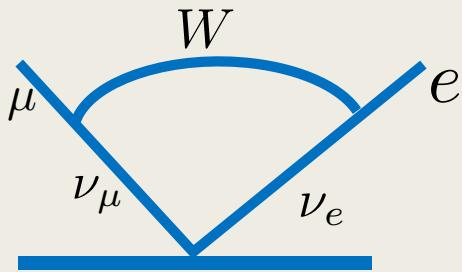
S. Davidson, C. Pena-Garay, N. Rius, and A. Santamaria,
JHEP 03, 011 (2003), arXiv:hep-ph/0302093.

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Heavy mediator

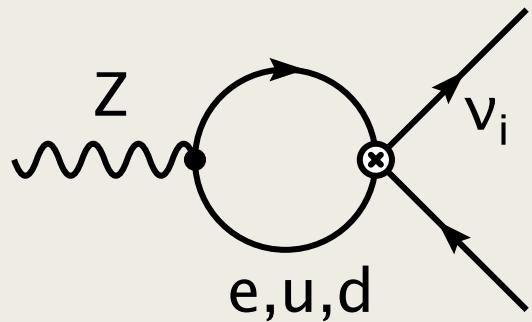


$$R_{\mu e} \equiv \frac{\sigma(\mu^- Ti \rightarrow e^- Ti)}{\sigma(\mu^- Ti \rightarrow \text{capture})} < 4.3 \times 10^{-12} ,$$

S. Davidson, C. Pena-Garay, N. Rius, and A. Santamaria,
JHEP 03, 011 (2003), arXiv:hep-ph/0302093.

$$|\epsilon_{e\mu}^{qR}|, |\epsilon_{e\mu}^{qL}| < 7.7 \times 10^{-4} , \quad q \in \{u, d\}.$$

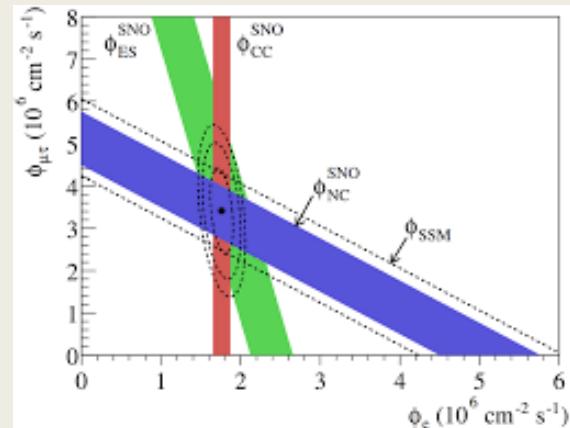
Invisible decay mode of Z bosons



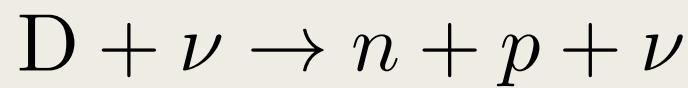
S. Davidson, C. Pena-Garay, N. Rius, and A. Santamaria,
JHEP 03, 011 (2003), arXiv:hep-ph/0302093.

$$|\epsilon_{\tau\tau}^{qA}| < \mathcal{O}(1) , \quad q \in \{u, d\}.$$

New solution found in SNO data



2019-2006



Deuterium dissociation

$$\frac{G_F}{\sqrt{2}} [\bar{\nu}_\alpha \gamma^\mu (1 - \gamma_5) \nu_\beta] \left[\overline{f} \gamma_\mu \left(\epsilon_{\alpha\beta}^{Vf} + \epsilon_{\alpha\beta}^{Af} \gamma_5 \right) f \right]$$

$$\frac{G_F}{\sqrt{2}} [\bar{\nu}_\alpha \gamma^\mu (1 - \gamma_5) \nu_\beta] \left(\epsilon_{\alpha\beta}^{An} \bar{n} \gamma^\mu \gamma_5 n + \epsilon_{\alpha\beta}^{Ap} \bar{p} \gamma^\mu \gamma_5 p \right),$$

$$\epsilon_{\alpha\beta}^{Ap} = \Delta_u \epsilon_{\alpha\beta}^{Au} + \Delta_d \epsilon_{\alpha\beta}^{Ad},$$

$$\epsilon_{\alpha\beta}^{An} = \Delta_u \epsilon_{\alpha\beta}^{Ad} + \Delta_d \epsilon_{\alpha\beta}^{Au}.$$

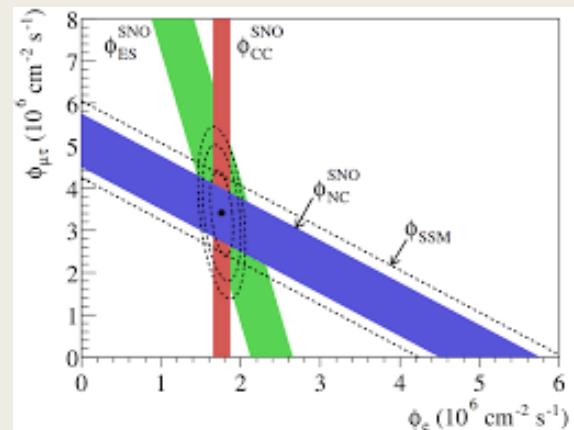
$$\Delta_d = -0.43$$

$$\Delta_u = 0.84$$

M. Cirelli, E. Del Nobile, and P. Panci, JCAP 10, 019 (2013),

$$\epsilon_{\alpha\beta}^{An} - \epsilon_{\alpha\beta}^{Ap} = (\Delta_u - \Delta_d) (\epsilon_{\alpha\beta}^{Au} - \epsilon_{\alpha\beta}^{Ad}) = 1.27 (\epsilon_{\alpha\beta}^{Au} - \epsilon_{\alpha\beta}^{Ad}).$$

New solution found in SNO data



$$-2.1 < \epsilon_{\tau\tau}^{Au} - \epsilon_{\tau\tau}^{Ad} < -1.8$$

P. Coloma, M. C. Gonzalez-Garcia, M. Maltoni,
J. a. P. Pinheiro, and S. Urrea, [JHEP 08, 032 \(2023\)](#)

	Allowed ranges at 90% CL (1-parameter)	
	GLOB-OSC	
$\varepsilon_{ee}^{u,A}$	$[-2.1, -1.8] \oplus [-0.19, +0.13]$	$-\varepsilon_{ee}^{d,A}$
$\varepsilon_{\mu\mu}^{u,A}$	$[-2.2, -1.7] \oplus [-0.26, +0.18]$	$-\varepsilon_{\mu\mu}^{d,A}$
$\varepsilon_{\tau\tau}^{u,A}$	$[-2.1, -1.8] \oplus [-0.20, +0.15]$	$-\varepsilon_{\tau\tau}^{d,A}$
$\varepsilon_{e\mu}^{u,A}$	$[-1.5, -1.2] \oplus [-0.16, +0.12] \oplus [+1.4, +1.7]$	$-\varepsilon_{e\mu}^{d,A}$
$\varepsilon_{e\tau}^{u,A}$	$[-1.5, -1.3] \oplus [-0.13, +0.10] \oplus [+1.4, +1.7]$	$-\varepsilon_{e\tau}^{d,A}$
$\varepsilon_{\mu\tau}^{u,A}$	$[-0.085, +0.11] \oplus [+1.6, +1.9]$	$-\varepsilon_{\mu\tau}^{d,A}$

P. Coloma, M. C. Gonzalez-Garcia, M. Maltoni,
J. a. P. Pinheiro, and S. Urrea, [JHEP 08, 032 \(2023\)](#)

A model for Axial NSI

- S. Abbaslu and Y. F.,
- “A model for Axial Non-Standard Interactions of neutrinos with quarks,”
- arXiv:2407.13834
- *Nucl.Phys.B* 1018 (2025) 117070

Model building

New U(1) gauge symmetry

$$Q_1 = \begin{pmatrix} u_L \\ d_L \end{pmatrix} \rightarrow \exp^{i\alpha} Q_1 , \quad Q_2 = \begin{pmatrix} c_L \\ s_L \end{pmatrix} \rightarrow \exp^{i\alpha} Q_2 , \quad \text{and} \quad Q_3 = \begin{pmatrix} t_L \\ b_L \end{pmatrix} \rightarrow \exp^{i\alpha} Q_3 .$$

$$u_R \rightarrow \exp^{-i\alpha} u_R \quad \text{and} \quad d_R \rightarrow \exp^{-i\alpha} d_R .$$

Axial coupling to first generation quarks

$$g_Z Z'_\mu (\bar{u} \gamma^\mu \frac{1 - \gamma_5}{2} u + \bar{d} \gamma^\mu \frac{1 - \gamma_5}{2} d - \bar{u} \gamma^\mu \frac{1 + \gamma_5}{2} u - \bar{d} \gamma^\mu \frac{1 + \gamma_5}{2} d) = -g_Z Z'_\mu (\bar{u} \gamma^\mu \gamma_5 u + \bar{d} \gamma^\mu \gamma_5 d) .$$

To cancel the $U(1) - SU(2) - SU(2)$ anomaly,

$$L_\tau = \begin{pmatrix} \nu_\tau \\ \tau_L \end{pmatrix} \rightarrow e^{-9i\alpha} L_\tau \quad \text{under } U(1)$$

$$\epsilon_{\tau\tau}^{Au} = \epsilon_{\tau\tau}^{Ad} = \frac{9\sqrt{2}g_{Z'}^2}{m_{Z'}^2 G_F}.$$

■Part Two

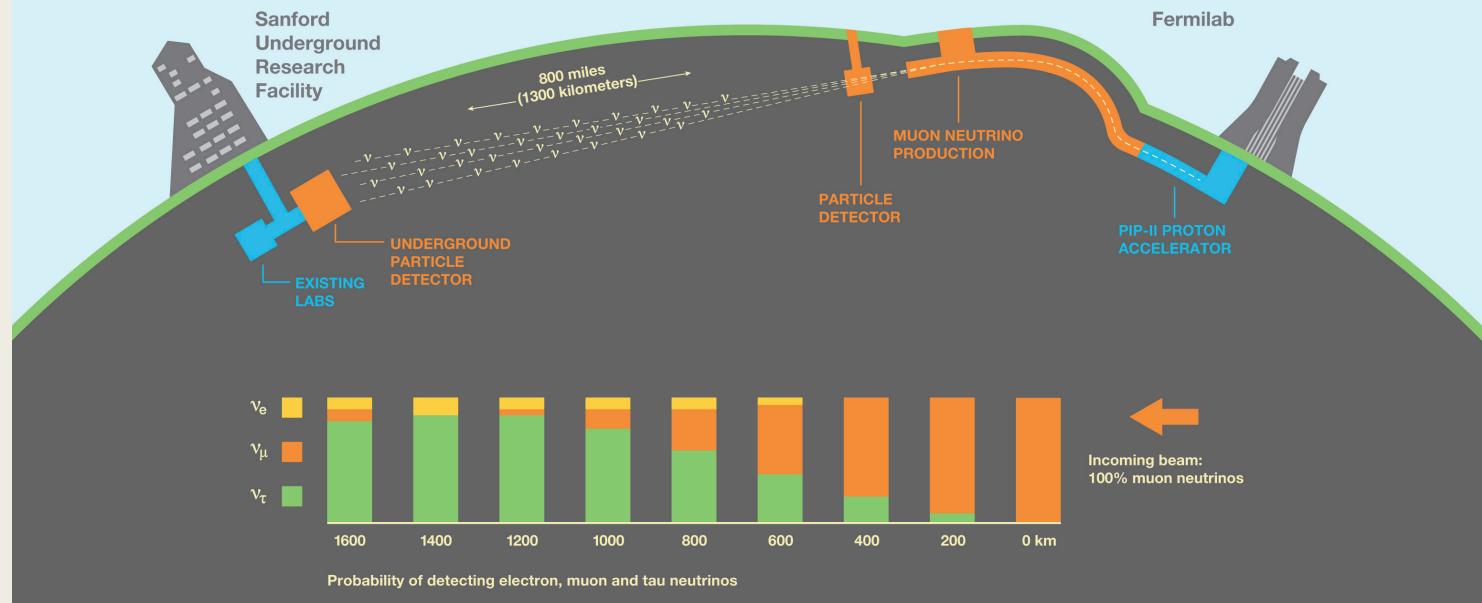
Based on

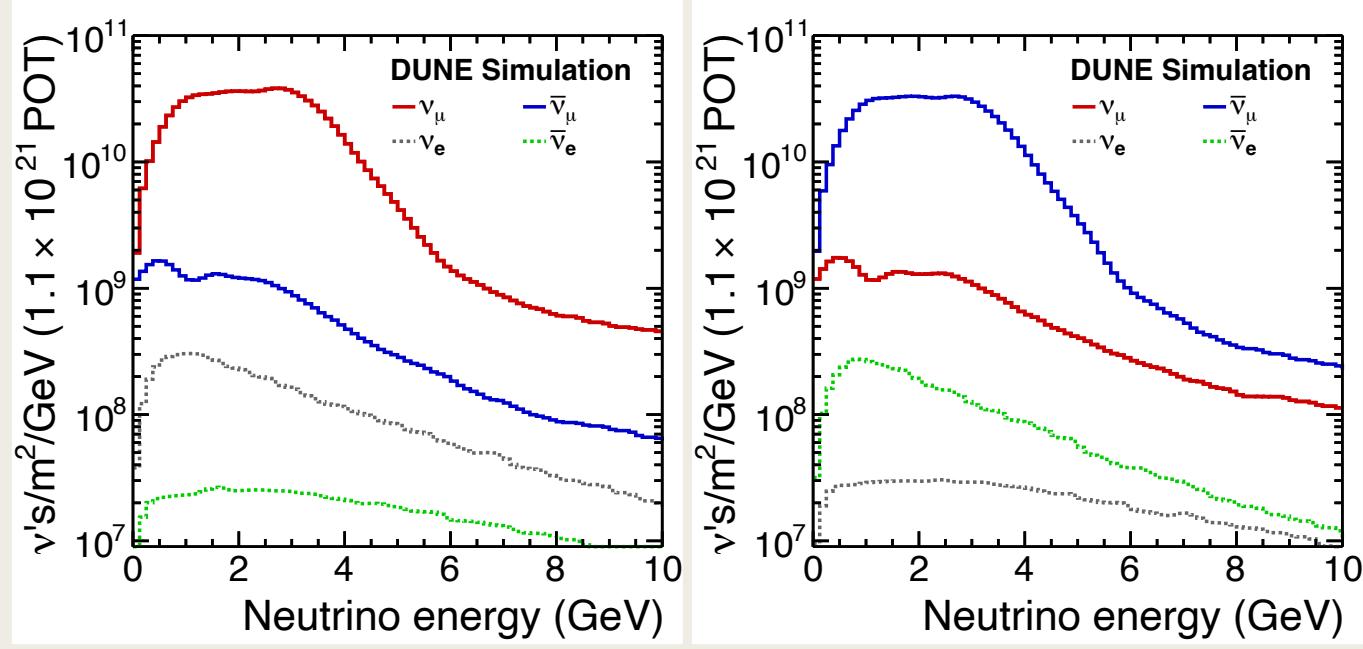
Searching for axial neutral current non-standard interactions of
neutrinos by DUNE-like experiments

Saeed Abbaslu, Mehran Dehpour, YF., Sahar Safari

JHEP 04 (2024) 038

Deep Underground Neutrino Experiment





Deep Inelastic Scattering (DIS) in the presence of NSI

$$\mathcal{L}_{\text{tot}}^{\text{NC}} = -\frac{G_F}{\sqrt{2}} \sum_{\alpha, \beta, q} [\bar{\nu}_\alpha \gamma^\mu (1 - \gamma_5) \nu_\beta] \left[\bar{q} \gamma_\mu \left(f_{\alpha\beta}^{Vq} + f_{\alpha\beta}^{Aq} \gamma_5 \right) q \right],$$

$$f_{\alpha\beta}^{Vq} = \epsilon_{\alpha\beta}^{Vq} + g^{Vq} \delta_{\alpha\beta} \quad \text{and} \quad f_{\alpha\beta}^{Aq} = \epsilon_{\alpha\beta}^{Aq} + g^{Aq} \delta_{\alpha\beta}.$$

$$\epsilon_{\alpha\beta}^{V/Aq} = \epsilon_{\alpha\beta}^{Lq} \pm \epsilon_{\alpha\beta}^{Rq} \text{ and } g_{\alpha\beta}^{V/Aq} = g^{Lq} \pm g^{Rq}.$$

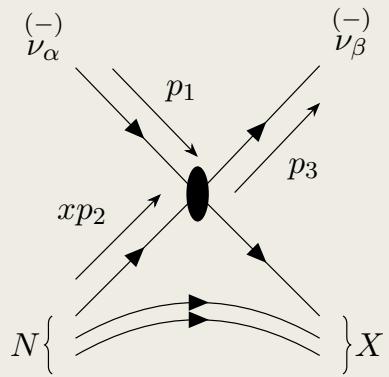
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$$\mathcal{L}_{\text{tot}}^{\text{NC}} = -\frac{G_F}{\sqrt{2}} \sum_{\alpha, \beta, q} [\bar{\nu}_\alpha \gamma^\mu (1 - \gamma_5) \nu_\beta] \left[\bar{q} \gamma_\mu \left(f_{\alpha\beta}^{Vq} + f_{\alpha\beta}^{Aq} \gamma_5 \right) q \right],$$

	Up type quarks (u, c, t)	Down type quarks (d, s, b)	Charged leptons (e, μ, τ)	Neutral leptons (ν_e, ν_μ, ν_τ)
g^L	$\frac{1}{2} - \frac{2}{3} \sin^2 \theta_W$	$-\frac{1}{2} + \frac{1}{3} \sin^2 \theta_W$	$-\frac{1}{2} + \sin^2 \theta_W$	$\frac{1}{2}$
g^R	$-\frac{2}{3} \sin^2 \theta_W$	$\frac{1}{3} \sin^2 \theta_W$	$\sin^2 \theta_W$	0
g^V	$\frac{1}{2} + \frac{4}{3} \sin^2 \theta_W$	$-\frac{1}{2} + \frac{2}{3} \sin^2 \theta_W$	$-\frac{1}{2} + 2 \sin^2 \theta_W$	$\frac{1}{2}$
g^A	$\frac{1}{2}$	$-\frac{1}{2}$	$-\frac{1}{2}$	$\frac{1}{2}$

$$\nu_\alpha(p_1) + N(p_2) \rightarrow \nu_\beta(p_3) + X(p') \quad \text{where} \quad N = n, p,$$

$$\bar{\nu}_\alpha(p_1) + N(p_2) \rightarrow \bar{\nu}_\beta(p_3) + X(p') \quad \text{where} \quad N = n, p,$$



$$p_1^\mu = (p_1^0, \vec{p}_1), \text{ where } |\vec{p}_1| = p_1^0 = E_\nu,$$

$$p_3^\mu = (p_3^0, \vec{p}_3), \text{ where } |\vec{p}_3| = p_3^0 = E'_\nu,$$

$$p_2^\mu = (p_2^0, \vec{p}_2) = (M_N, 0, 0, 0).$$

$$q^\mu = (p_1 - p_3)^\mu$$

$$x = \frac{-q^2}{2p_2 \cdot q} = \frac{Q^2}{2M_N(E_\nu - E'_\nu)}, \quad y = 1 - \frac{E'_\nu}{E_\nu},$$

$$0 \leq x \leq 1 \quad \text{and} \quad 0 \leq y \leq \frac{1}{1 + M_N x / (2E_\nu)}.$$

$$\begin{aligned} \frac{d^2\sigma_{\rm NC}(\stackrel{(-)}{\nu_\alpha}N\rightarrow\stackrel{(-)}{\nu_\beta}+X)}{dxdy}=\sigma_{\rm NC}^0\Bigg\{&\frac{1}{2}\left(xy^2+2x-2xy-\frac{M_N}{E_\nu}x^2y\right)\\ &\times\left[\sum_qf_N^q(x)\left(\left|f^{Vq}_{\alpha\beta}\right|^2+\left|f^{Aq}_{\alpha\beta}\right|^2\right)+\sum_{\overline{q}}f_N^{\overline{q}}(x)\left(\left|f^{Vq}_{\alpha\beta}\right|^2+\left|f^{Aq}_{\alpha\beta}\right|^2\right)\right]\\ &\pm2xy\left(1-\frac{y}{2}\right)\left[\sum_qf_N^q(x)\Re\left[f^{Vq}_{\alpha\beta}(f^{Aq}_{\alpha\beta})^*\right]-\sum_{\overline{q}}f_N^{\overline{q}}(x)\Re\left[f^{Vq}_{\alpha\beta}(f^{Aq}_{\alpha\beta})^*\right]\right]\Bigg\}, \end{aligned}$$

$$\sigma_{\rm NC}^0 = \frac{G_{\rm F}^2}{\pi} \left(M_N E_\nu\right).$$

$$f_n^d(x)=f_p^u(x)\equiv u(x),\quad f_n^{\overline{d}}(x)=f_p^{\overline{u}}(x)\equiv \overline{u}(x),$$

$$f_n^u(x)=f_p^d(x)\equiv d(x),\quad f_n^{\overline{u}}(x)=f_p^{\overline{d}}(x)\equiv \overline{d}(x),$$

$$f_n^s(x)=f_p^s(x)\equiv s(x),\quad f_n^{\overline{s}}(x)=f_p^{\overline{s}}(x)\equiv \overline{s}(x).$$

$$\begin{aligned} \sigma_p(\overset{(-)}{\nu_\alpha} + p \rightarrow \overset{(-)}{\nu_\beta} + X) &\simeq \sigma_{\text{NC}}^0 \int_0^1 dx \\ &\times \left\{ \frac{2}{3} \left[1 - \frac{3}{2} \frac{M_p x}{2E_\nu} + \frac{9}{4} \left(\frac{M_p x}{2E_\nu} \right)^2 \right] x \left[[u(x) + \bar{u}(x)] (|f_{\alpha\beta}^{Vu}|^2 + |f_{\alpha\beta}^{Au}|^2) \right. \right. \\ &+ [d(x) + \bar{d}(x)] (|f_{\alpha\beta}^{Vd}|^2 + |f_{\alpha\beta}^{Ad}|^2) + [s(x) + \bar{s}(x)] (|f_{\alpha\beta}^{Vs}|^2 + |f_{\alpha\beta}^{As}|^2) \Big] \\ &\pm \frac{2}{3} \left[1 - \frac{3}{2} \frac{M_p x}{2E_\nu} + \frac{3}{2} \left(\frac{M_p x}{2E_\nu} \right)^2 \right] x \left[[u(x) - \bar{u}(x)] \Re [f_{\alpha\beta}^{Vu} (f_{\alpha\beta}^{Au})^*] \right. \\ &+ [d(x) - \bar{d}(x)] \Re [f_{\alpha\beta}^{Vd} (f_{\alpha\beta}^{Ad})^*] + [s(x) - \bar{s}(x)] \Re [f_{\alpha\beta}^{Vs} (f_{\alpha\beta}^{As})^*] \Big] \Big\}, \end{aligned}$$

- CT18 next-to-next to-leading order (CT18NNLO)

T.-J. Hou et al., [Phys. Rev. D 103, 014013 \(2021\)](#)

The [CT18 PDF](#) set is obtained by the [CTEQ-TEA collaboration](#) implementing a comprehensive range of high-precision Large Hadron Collider ([LHC](#)) data, plus the combined [HERA I+II Deep Inelastic Scattering \(DIS\) data](#), along with the [CT14 global QCD analysis](#).

Q=2 GeV	Integral	<i>u</i>	<i>d</i>	<i>s</i>
	$\int_0^1 dx x [q(x) + \bar{q}(x)]$	0.349 ± 0.007	0.193 ± 0.007	0.033 ± 0.008
	$\int_0^1 dx x^2 [q(x) + \bar{q}(x)]$	0.090 ± 0.002	0.037 ± 0.001	0.002 ± 0.0008
	$\int_0^1 dx x^3 [q(x) + \bar{q}(x)]$	0.034 ± 0.0009	0.012 ± 0.0007	0.0005 ± 0.0005
	$\int_0^1 dx x [q(x) - \bar{q}(x)]$	0.290 ± 0.008	0.120 ± 0.003	0.0
	$\int_0^1 dx x^2 [q(x) - \bar{q}(x)]$	0.084 ± 0.002	0.030 ± 0.001	0.0
	$\int_0^1 dx x^3 [q(x) - \bar{q}(x)]$	0.033 ± 0.0009	0.010 ± 0.0007	0.0

$$|\nu_{\text{far}}(E_\nu)\rangle = \sum_i \sum_\beta e^{im_{Mi}^2 L/(2E_\nu)} (U_{\mu i}^M)^* U_{\beta i}^M |\nu_\beta\rangle \equiv \sum_\beta \mathcal{A}_\beta |\nu_\beta\rangle \quad (\text{neutrino mode})$$

and

$$|\bar{\nu}_{\text{far}}(E_\nu)\rangle = \sum_i \sum_\beta e^{i\overline{m}_{Mi}^2 L/(2E_\nu)} (\overline{U}_{\mu i}^M)^* \overline{U}_{\beta i}^M |\bar{\nu}_\beta\rangle \equiv \sum_\beta \overline{\mathcal{A}}_\beta |\bar{\nu}_\beta\rangle \quad (\text{antineutrino mode})$$

$$|\mathcal{A}_\beta|^2 = P(\nu_\mu \rightarrow \nu_\beta)$$

$$\sum_\alpha |\mathcal{A}_\alpha|^2 = 1 \quad \text{and} \quad \sum_\alpha |\overline{\mathcal{A}}_\alpha|^2 = 1.$$

$$\mathcal{M}(\nu_{\rm far}+q \rightarrow \nu_\alpha + q) = \sum_\beta \mathcal{A}_\beta \mathcal{M}(\nu_\beta + q \rightarrow \nu_\alpha + q),$$

$$\mathcal{M}(\overline{\nu}_{\rm far}+q \rightarrow \overline{\nu}_\alpha + q) = \sum_\beta \overline{\mathcal{A}}_\beta \mathcal{M}(\overline{\nu}_\beta + q \rightarrow \overline{\nu}_\alpha + q).$$

Change of basis

$$\alpha \in \{\text{far}, \perp, T\}$$

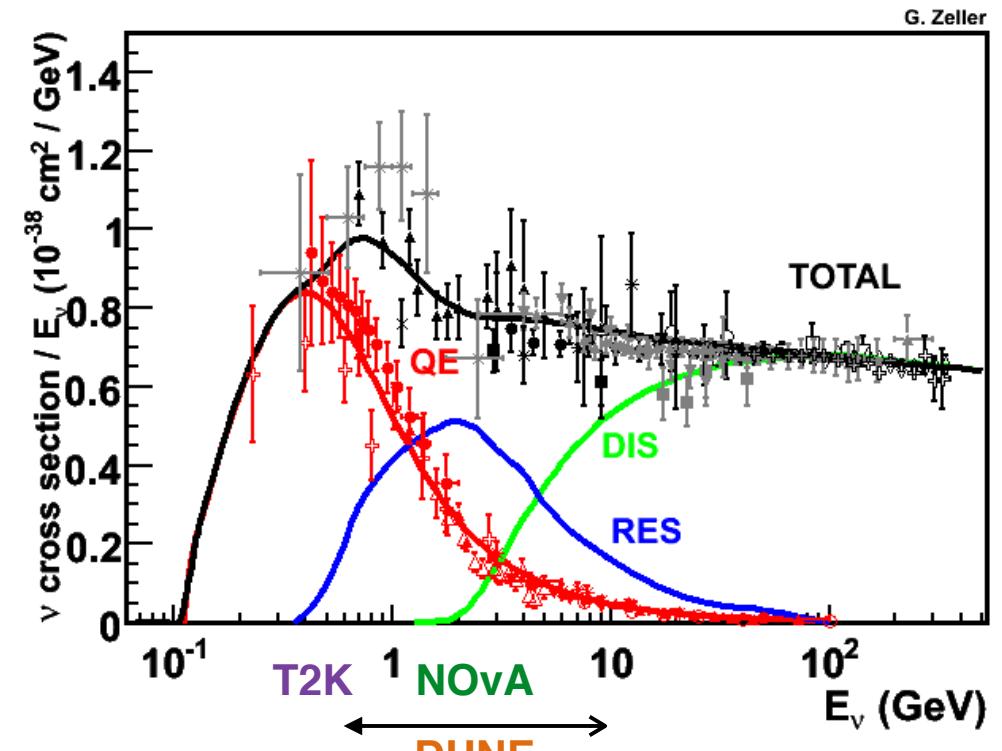
$$\begin{bmatrix} \nu_{\text{far}} \\ \nu_{\perp} \\ \nu_T \end{bmatrix} = \begin{bmatrix} \mathcal{A}_e & \mathcal{A}_\mu & \mathcal{A}_\tau \\ 0 & -\mathcal{A}_\tau^*/\mathcal{A} & \mathcal{A}_\mu^*/\mathcal{A} \\ \frac{\mathcal{A}\mathcal{A}_e}{|\mathcal{A}_e|} & -\frac{\mathcal{A}_\mu|\mathcal{A}_e|}{\mathcal{A}} & -\frac{\mathcal{A}_\tau|\mathcal{A}_e|}{\mathcal{A}} \end{bmatrix} \begin{bmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{bmatrix} = U \cdot \begin{bmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{bmatrix},$$

$$\mathcal{A} = \sqrt{|\mathcal{A}_\tau|^2 + |\mathcal{A}_\mu|^2}.$$

$$f_{\alpha\beta}^{Vq} \rightarrow \tilde{f}_{\alpha\beta}^{Vq} = (U \cdot f^{Vq} \cdot U^\dagger)_{\alpha\beta} = f_{\alpha\beta}^{Vq} \quad \text{and} \quad f_{\alpha\beta}^{Aq} \rightarrow \tilde{f}_{\alpha\beta}^{Aq} = (U \cdot f^{Aq} \cdot U^\dagger)_{\alpha\beta} \neq f_{\alpha\beta}^{Aq}.$$

DIS : $\nu + N \rightarrow \nu + X$

RES : $\nu + N \rightarrow \nu + \Delta \rightarrow \nu + N + \pi$



J.A. Formaggio, G. Zeller, Reviews of Modern Physics, 84 (2012)

DIS : $\nu + N \rightarrow \nu + X$

RES : $\nu + N \rightarrow \nu + \Delta \rightarrow \nu + N + \pi$

J. Tingey et al.

“Neutrino characterisation

using convolutional neural networks in CHIPS water Cherenkov detectors,”

JINST **18** (2023) no.06, P06032

$$\begin{aligned}\mathcal{N}_\nu^{\text{ND}} &= \int \phi_\nu^{\text{ND}}(E) \left[(\sigma_n)_{\nu_\mu} N_n^{\text{ND}} + (\sigma_p)_{\nu_\mu} N_p^{\text{ND}} \right] dE, \\ \mathcal{N}_{\bar{\nu}}^{\text{ND}} &= \int \phi_{\bar{\nu}}^{\text{ND}}(E) \left[(\sigma_n)_{\bar{\nu}_\mu} N_n^{\text{ND}} + (\sigma_p)_{\bar{\nu}_\mu} N_p^{\text{ND}} \right] dE, \\ \mathcal{N}_\nu^{\text{FD}} &= \int \phi_\nu^{\text{FD}}(E) \left[(\sigma_n)_{\nu_{\text{far}}} N_n^{\text{FD}} + (\sigma_p)_{\nu_{\text{far}}} N_p^{\text{FD}} \right] dE, \\ \mathcal{N}_{\bar{\nu}}^{\text{FD}} &= \int \phi_{\bar{\nu}}^{\text{FD}}(E) \left[(\sigma_n)_{\bar{\nu}_{\text{far}}} N_n^{\text{FD}} + (\sigma_p)_{\bar{\nu}_{\text{far}}} N_p^{\text{FD}} \right] dE,\end{aligned}$$

6.5 years for running in each neutrino and antineutrino mode

1.1×10^{21} POT/year

<https://glaucus.crc.nd.edu/DUNEFluxes/>.

[“CP-optimized”
“ τ -optimized”]

$$\begin{aligned}\mathcal{N}_\nu^{\text{ND}} &= \int \phi_\nu^{\text{ND}}(E) \left[(\sigma_n)_{\nu_\mu} N_n^{\text{ND}} + (\sigma_p)_{\nu_\mu} N_p^{\text{ND}} \right] dE, \\ \mathcal{N}_{\bar{\nu}}^{\text{ND}} &= \int \phi_{\bar{\nu}}^{\text{ND}}(E) \left[(\sigma_n)_{\bar{\nu}_\mu} N_n^{\text{ND}} + (\sigma_p)_{\bar{\nu}_\mu} N_p^{\text{ND}} \right] dE, \\ \mathcal{N}_\nu^{\text{FD}} &= \int \phi_\nu^{\text{FD}}(E) \left[(\sigma_n)_{\nu_{\text{far}}} N_n^{\text{FD}} + (\sigma_p)_{\nu_{\text{far}}} N_p^{\text{FD}} \right] dE, \\ \mathcal{N}_{\bar{\nu}}^{\text{FD}} &= \int \phi_{\bar{\nu}}^{\text{FD}}(E) \left[(\sigma_n)_{\bar{\nu}_{\text{far}}} N_n^{\text{FD}} + (\sigma_p)_{\bar{\nu}_{\text{far}}} N_p^{\text{FD}} \right] dE,\end{aligned}$$

$M_{\text{fid}}^{\text{ND}} = 67.2$ ton and $M_{\text{fid}}^{\text{FD}} = 40$ kton

B. Abi, R. Acciarri, et al., arXiv:2103.04797 [hep-ex].

LAr detector at the near site

Including the GAr detector and SAND would yield slightly more statistics and therefore better results.

$$N_p^{\text{ND/FD}} = \frac{18}{40} \frac{M_{\text{fid}}^{\text{ND/FD}}}{M_p} \quad \text{and} \quad N_n^{\text{ND/FD}} = \frac{22}{40} \frac{M_{\text{fid}}^{\text{ND/FD}}}{M_p}.$$

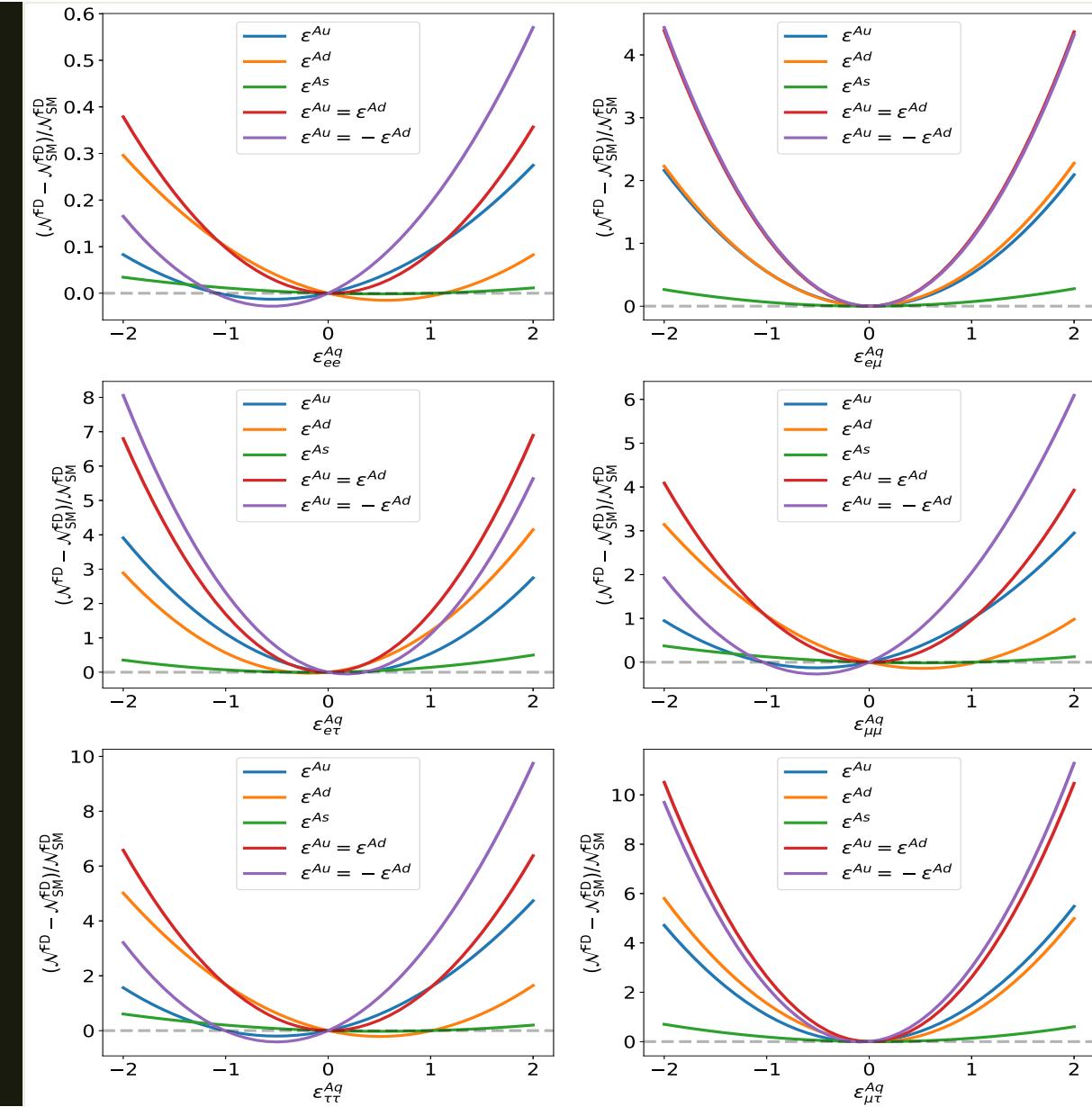
Total number of NC DIS events at ND and FD

6.5+6.5 years

$$\mathcal{N}^{\text{ND}} \equiv \mathcal{N}_{\nu}^{\text{ND}} + \mathcal{N}_{\bar{\nu}}^{\text{ND}}$$

$$\mathcal{N}^{\text{FD}} \equiv \mathcal{N}_{\nu}^{\text{FD}} + \mathcal{N}_{\bar{\nu}}^{\text{FD}}$$

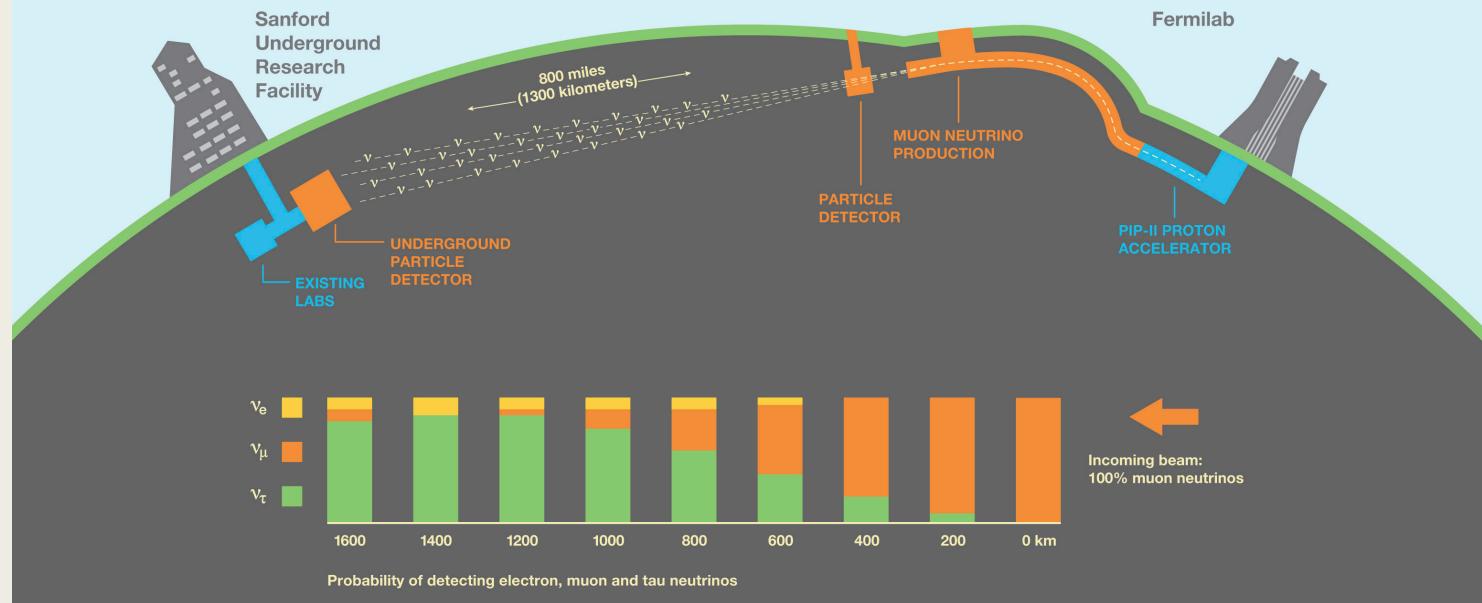
$$\mathcal{N}_{\text{SM}}^{\text{ND,FD}} \equiv \mathcal{N}^{\text{ND,FD}}(\epsilon_{\alpha\beta}^{Aq} = 0)$$



$$\int_0^1 dx x s(x) / \int_0^1 dx x u(x) \sim 0.1$$

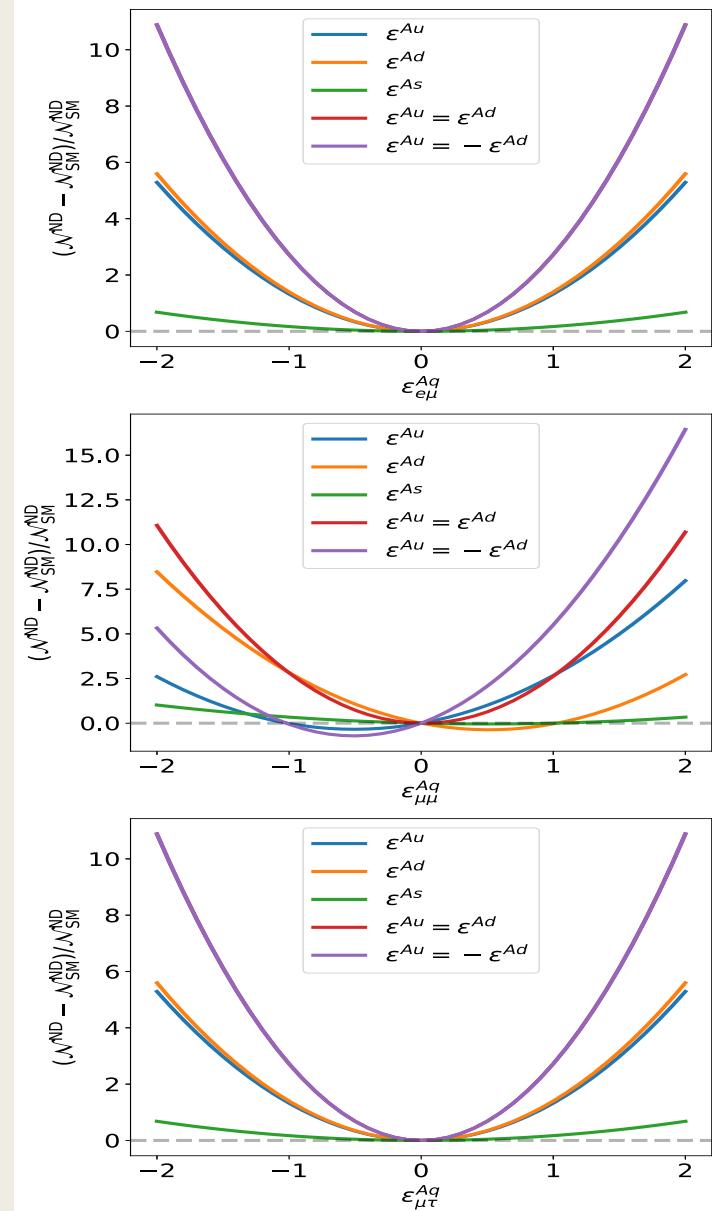
$$|\langle \nu_e | \nu_{far} \rangle|^2 \ll |\langle \nu_\mu | \nu_{far} \rangle|^2 \sim |\langle \nu_\tau | \nu_{far} \rangle|^2$$

Deep Underground Neutrino Experiment



Near detector

No sensitivity to ϵ_{ee}^{Aq} , $\epsilon_{e\tau}^{Aq}$ and $\epsilon_{\tau\tau}^{Aq}$



Forecasting bounds from DUNE

Benchmarks:

$$\epsilon^{Au} \neq 0, \epsilon^{Ad} = 0, \epsilon^{As} = 0$$

$$\epsilon^{Au} = 0, \epsilon^{Ad} \neq 0, \epsilon^{As} = 0$$

$$\epsilon^{Au} = 0, \epsilon^{Ad} = 0, \epsilon^{As} \neq 0$$

$$\epsilon^{Au} = \epsilon^{Ad} \neq 0, \epsilon^{As} = 0$$

Isospin symmetric benchmark

$$\epsilon^{Au} = \epsilon^{Ad} \neq 0, \epsilon^{As} = 0$$

This benchmark is unconstrained by SNO;

$$\epsilon_{\alpha\beta}^{An} - \epsilon_{\alpha\beta}^{Ap} = (\Delta_u - \Delta_d) (\epsilon_{\alpha\beta}^{Au} - \epsilon_{\alpha\beta}^{Ad}) = 1.27 (\epsilon_{\alpha\beta}^{Au} - \epsilon_{\alpha\beta}^{Ad}).$$

Background

$$\mathcal{B}_{\nu/\bar{\nu}}^{\text{ND/FD}} = \epsilon_{\text{CC}}(\mathcal{N}_{\text{CC}}^{\text{ND/FD}})_{\nu/\bar{\nu}} + \epsilon_{\text{Res}}(\mathcal{N}_{\text{Res}}^{\text{ND/FD}})_{\nu/\bar{\nu}},$$

$$\epsilon_{\text{CC}} \sim 10\%.$$

$$\epsilon_{\text{Res}} \sim 10\%.$$

P. Coloma, D. V. Forero, and S. J. Parke,
[JHEP 07, 079 \(2018\)](#)

J. Tingey et al., [JINST 18, P06032 \(2023\)](#)

Mode	Flux	\mathcal{N}^{ND}	\mathcal{B}^{ND}	\mathcal{N}^{FD}	\mathcal{B}^{FD}	
ν	CP	198334815	128917629	18835	12242	6.5+6.5 years
	τ	528621779	343604156	46059	29938	
$\bar{\nu}$	CP	88543625	57553356	8244	5358	
	τ	209747742	136336032	18145	11794	

Background

$$\mathcal{B}_{\nu/\bar{\nu}}^{\text{ND/FD}} = \epsilon_{\text{CC}}(\mathcal{N}_{\text{CC}}^{\text{ND/FD}})_{\nu/\bar{\nu}} + \epsilon_{\text{Res}}(\mathcal{N}_{\text{Res}}^{\text{ND/FD}})_{\nu/\bar{\nu}},$$

$$\epsilon_{\text{CC}} \sim 10\%.$$

$$\epsilon_{\text{Res}} \sim 10\%.$$

P. Coloma, D. V. Forero, and S. J. Parke,
[JHEP 07, 079 \(2018\)](#)

J. Tingey et al., [JINST 18, P06032 \(2023\)](#)

6.5+6.5 years

$$\mathcal{N}^{\text{ND}} \sim \mathcal{B}^{\text{ND}} \sim O(10^8)$$

$$\mathcal{N}^{\text{FD}} \sim \mathcal{B}^{\text{FD}} \sim O(10^4)$$

$$\chi^2 = \left[\sum_{Y=\nu,\bar{\nu}} \left(\frac{\left[\xi \mathcal{N}_Y^{\text{FD}}(\epsilon_{\text{test}}^{Aq}) - \epsilon \mathcal{N}_Y^{\text{FD}}(\epsilon^{Aq} = 0) + \omega_Y \mathcal{B}_Y^{\text{FD}} \right]^2}{\epsilon \mathcal{N}_Y^{\text{FD}}(\epsilon^{Aq} = 0) + \mathcal{B}_Y^{\text{FD}}} + \frac{\omega_Y^2}{\sigma_\omega^2} \right) + \frac{(\xi - \epsilon)^2}{\sigma_\epsilon^2} \right]_{\min},$$

$$\epsilon=90\%$$

Coloma, D. V. Forero, and S. J. Parke, JHEP 07, 079 (2018),

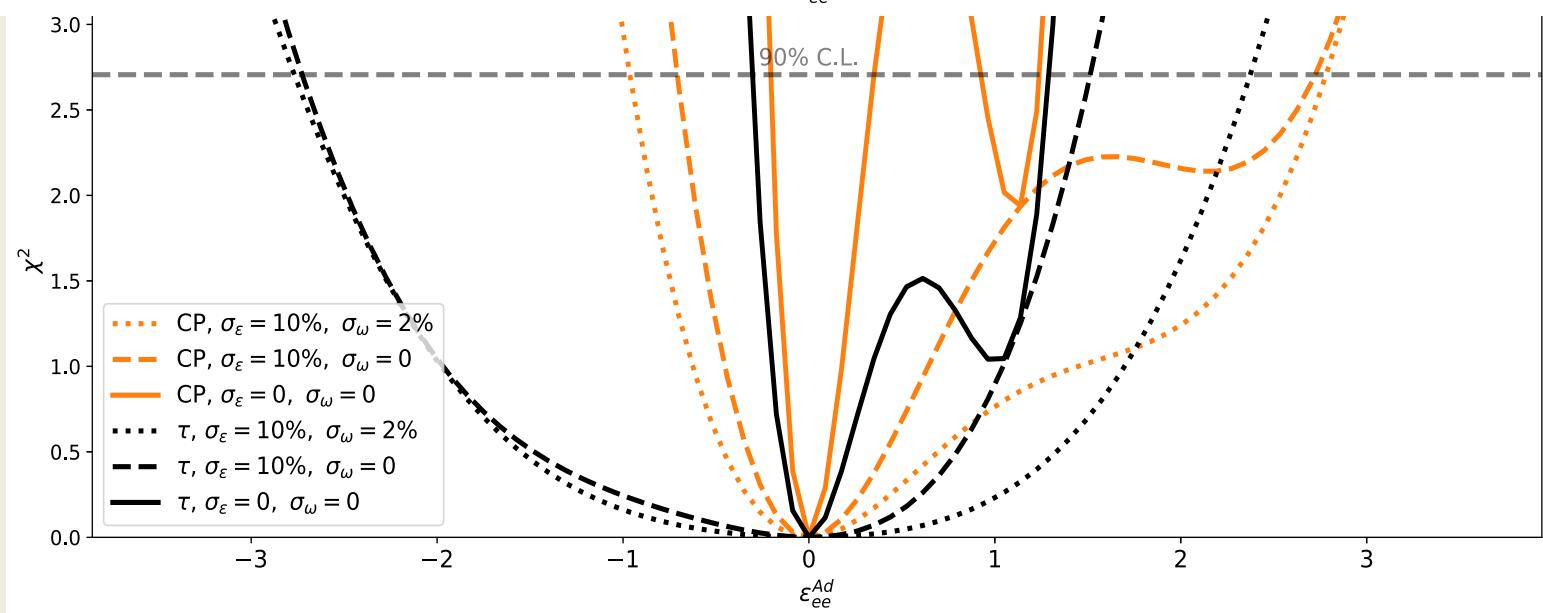
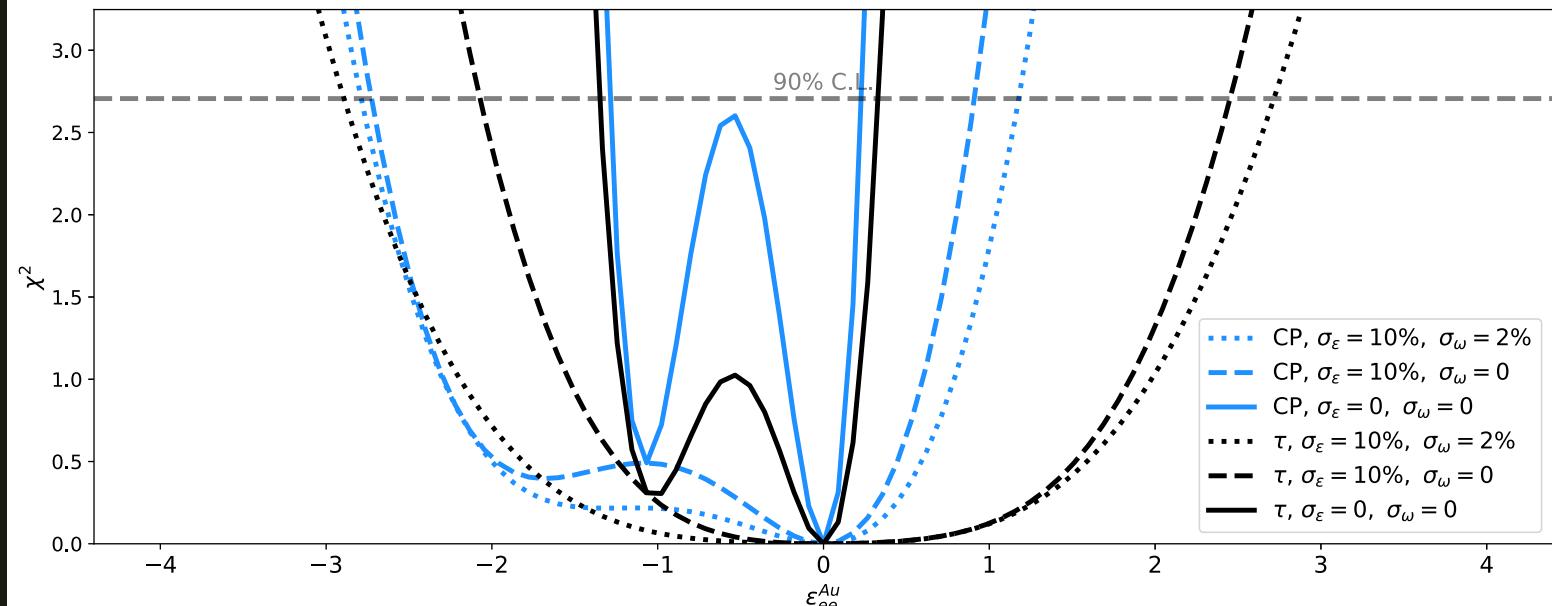
$$\chi^2 = \left[\sum_{Y=\nu, \bar{\nu}} \left(\frac{\left[\xi \mathcal{N}_Y^{\text{FD}}(\epsilon_{\text{test}}^{Aq}) - \epsilon \mathcal{N}_Y^{\text{FD}}(\epsilon^{Aq} = 0) + \omega_Y \mathcal{B}_Y^{\text{FD}} \right]^2}{\epsilon \mathcal{N}_Y^{\text{FD}}(\epsilon^{Aq} = 0) + \mathcal{B}_Y^{\text{FD}}} + \frac{\omega_Y^2}{\sigma_\omega^2} \right) + \frac{(\xi - \epsilon)^2}{\sigma_\epsilon^2} \right]_{\min},$$

No energy binning

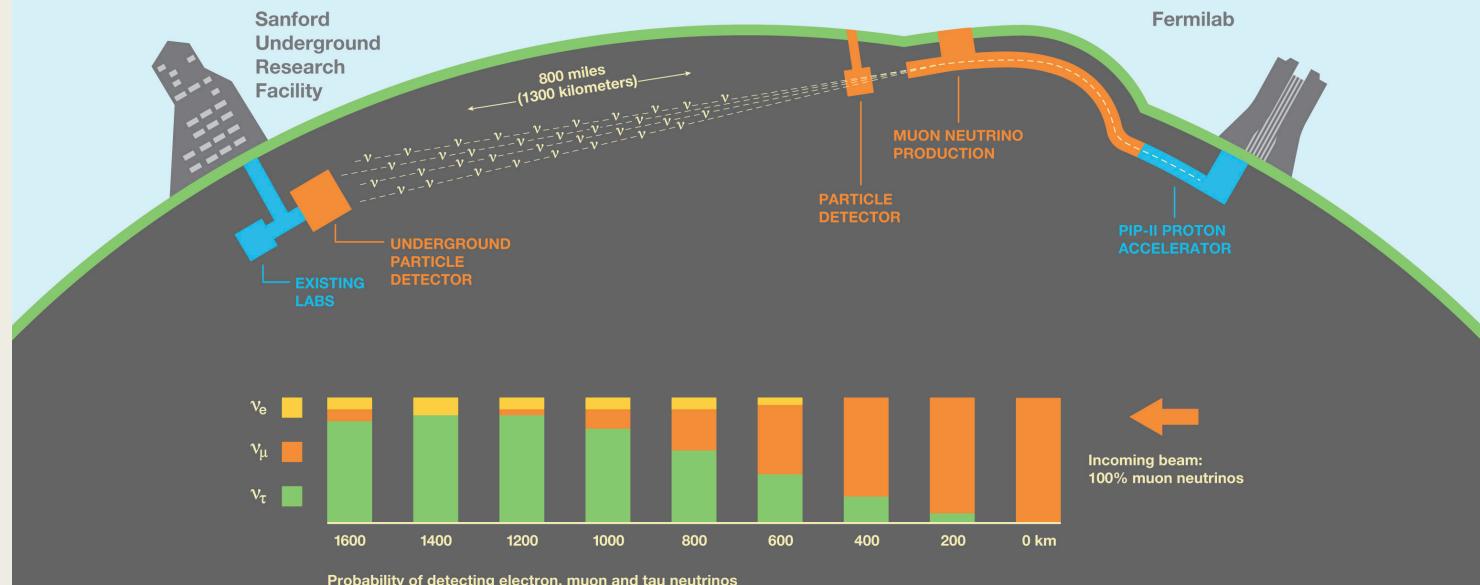
Missing energy in NC

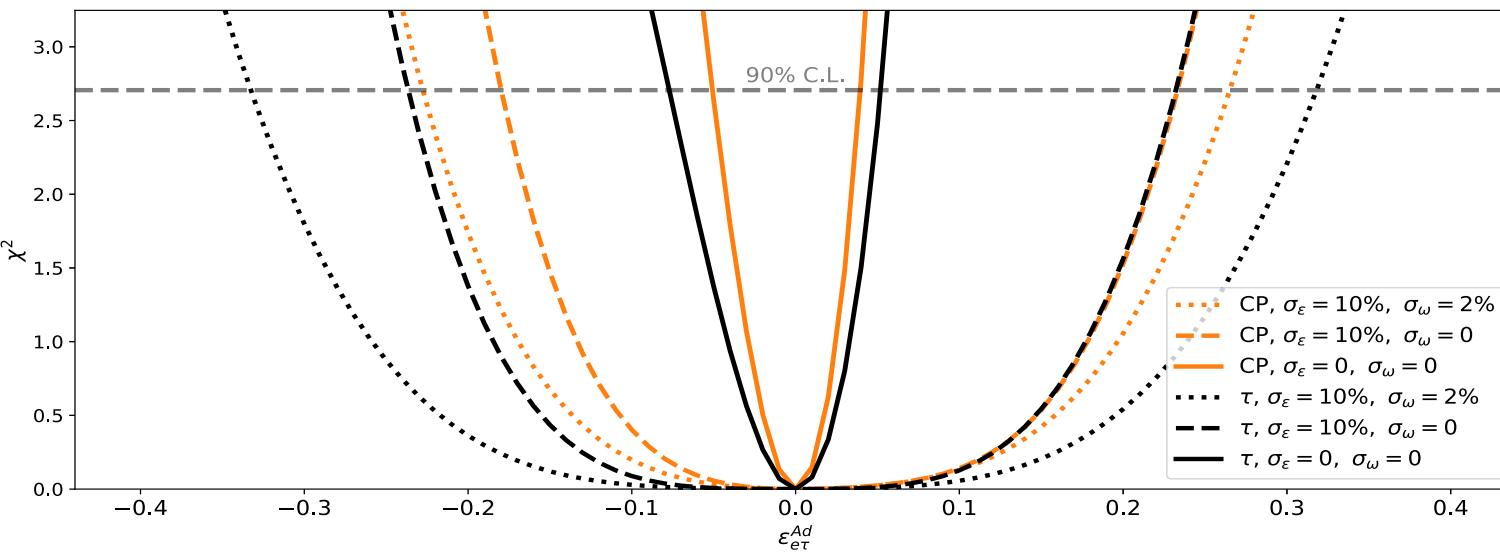
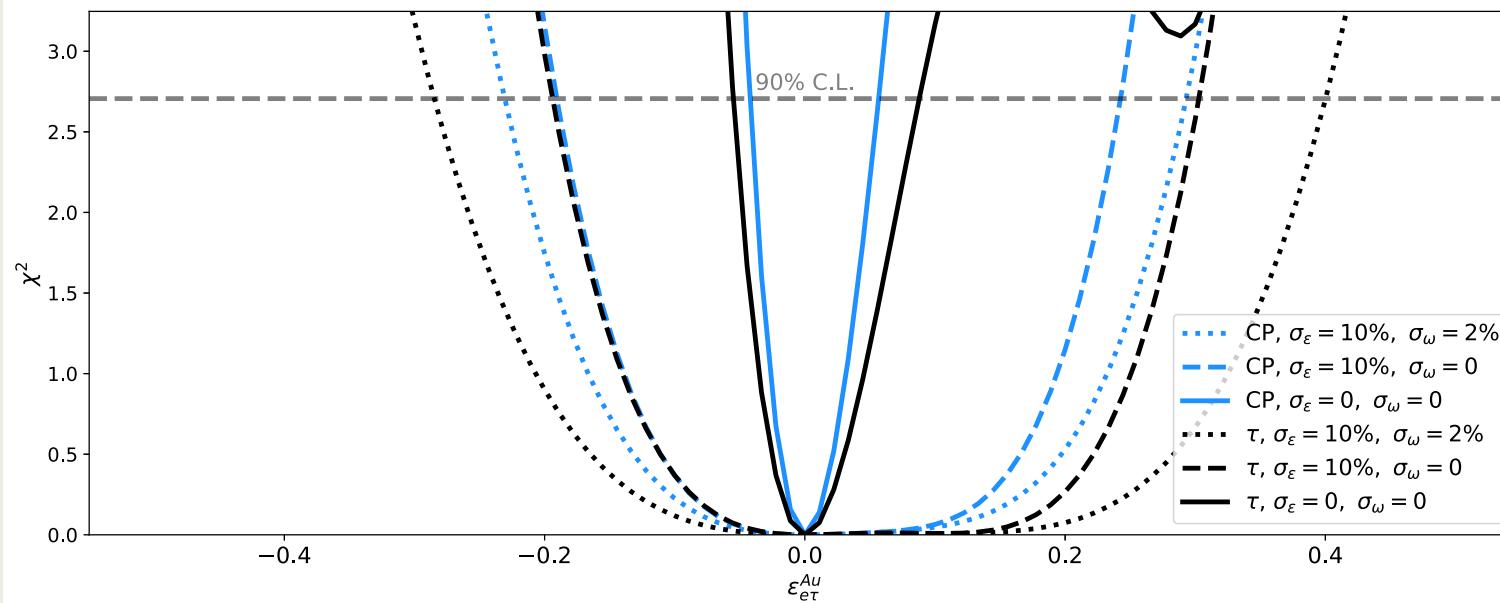
Migration matrices?

Far detector

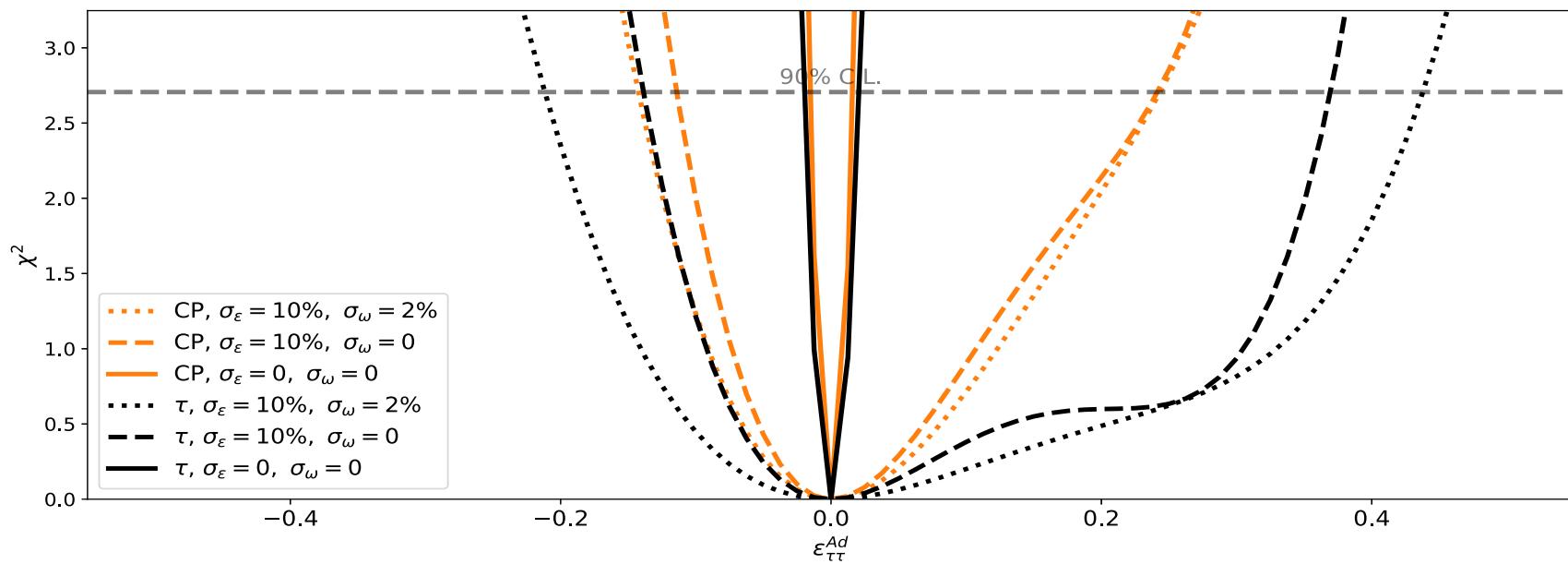
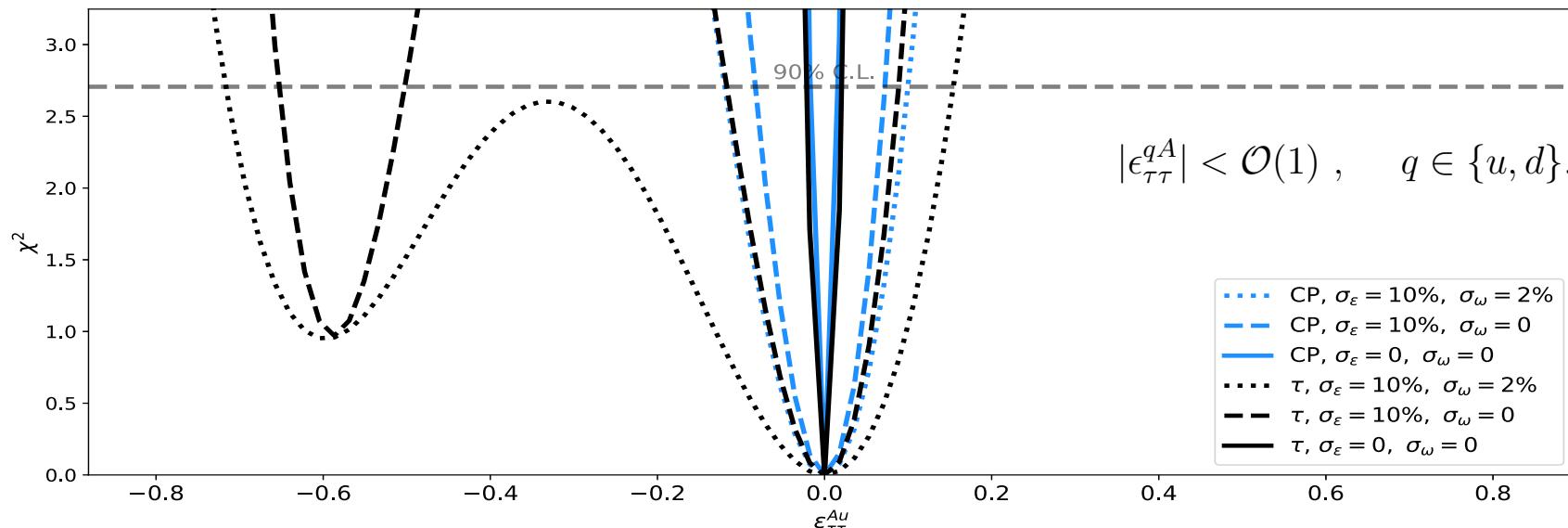


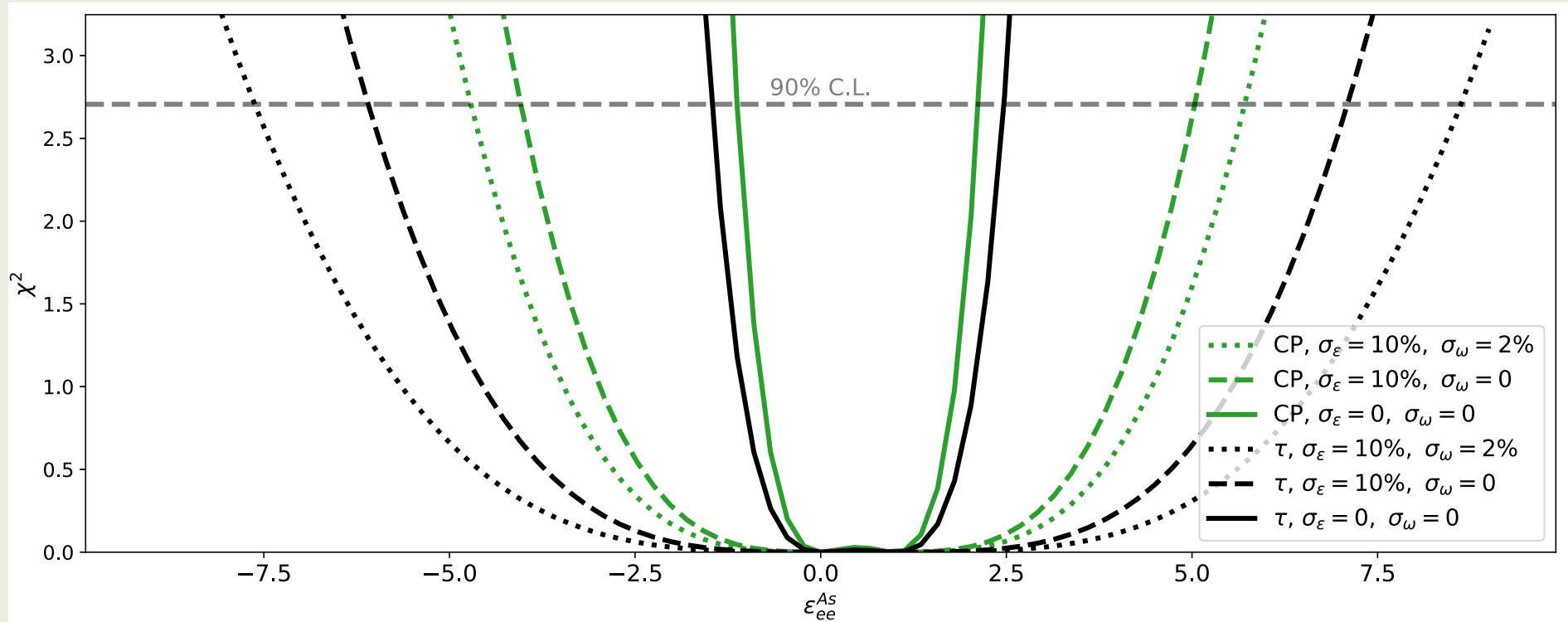
Deep Underground Neutrino Experiment

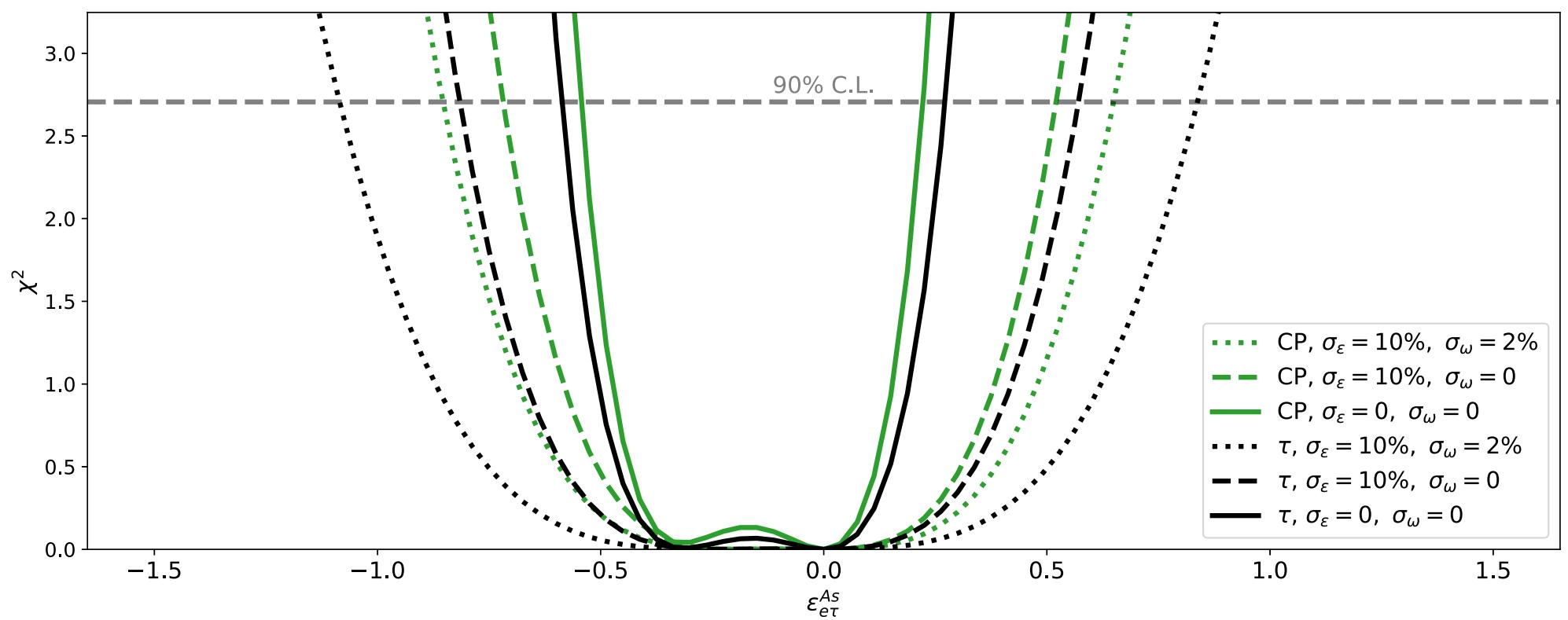


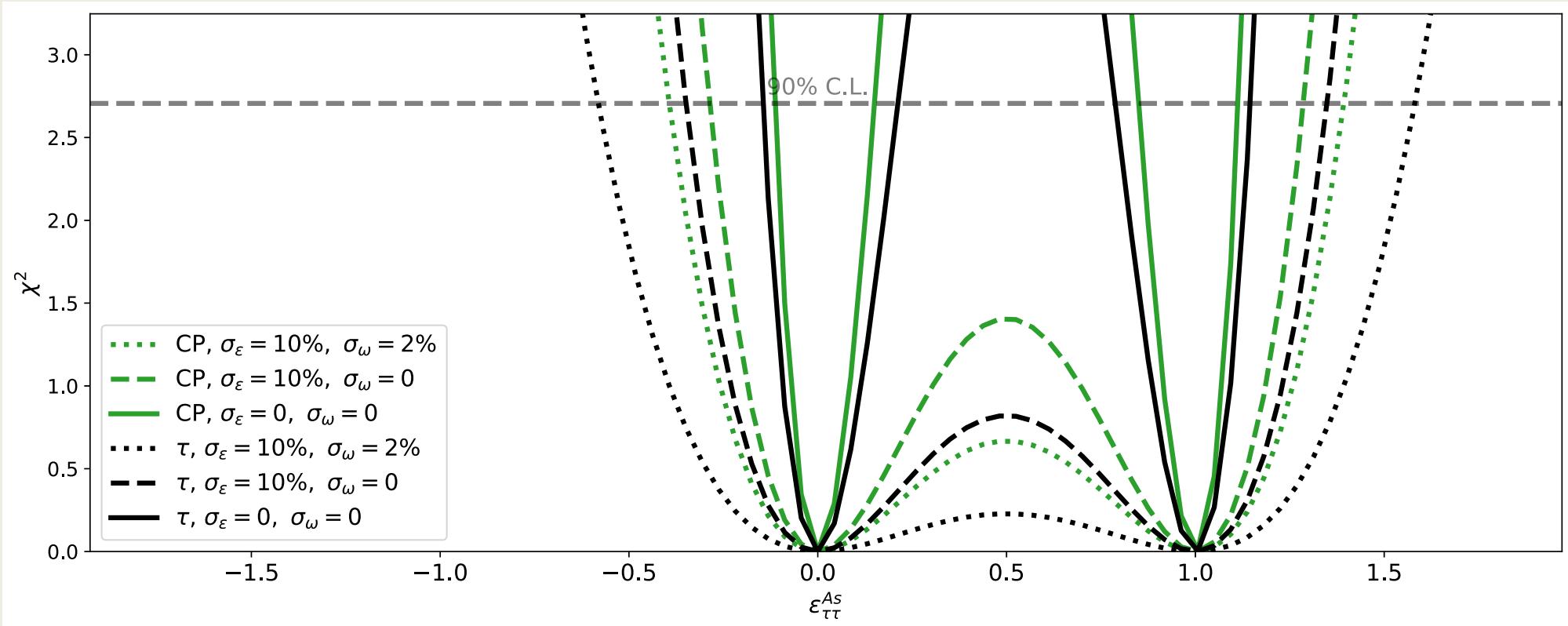


$|\varepsilon_{e\tau}^{Au}|, |\varepsilon_{e\tau}^{Ad}| < 0.5.$

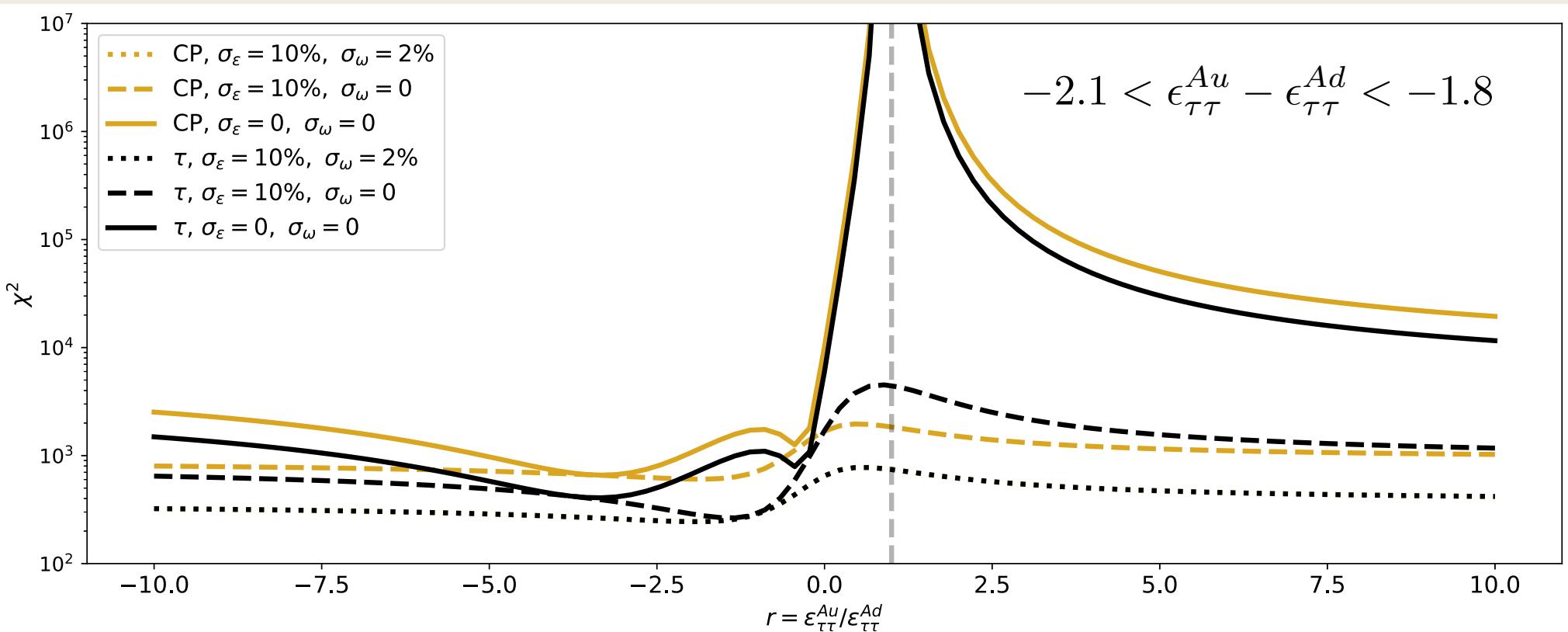


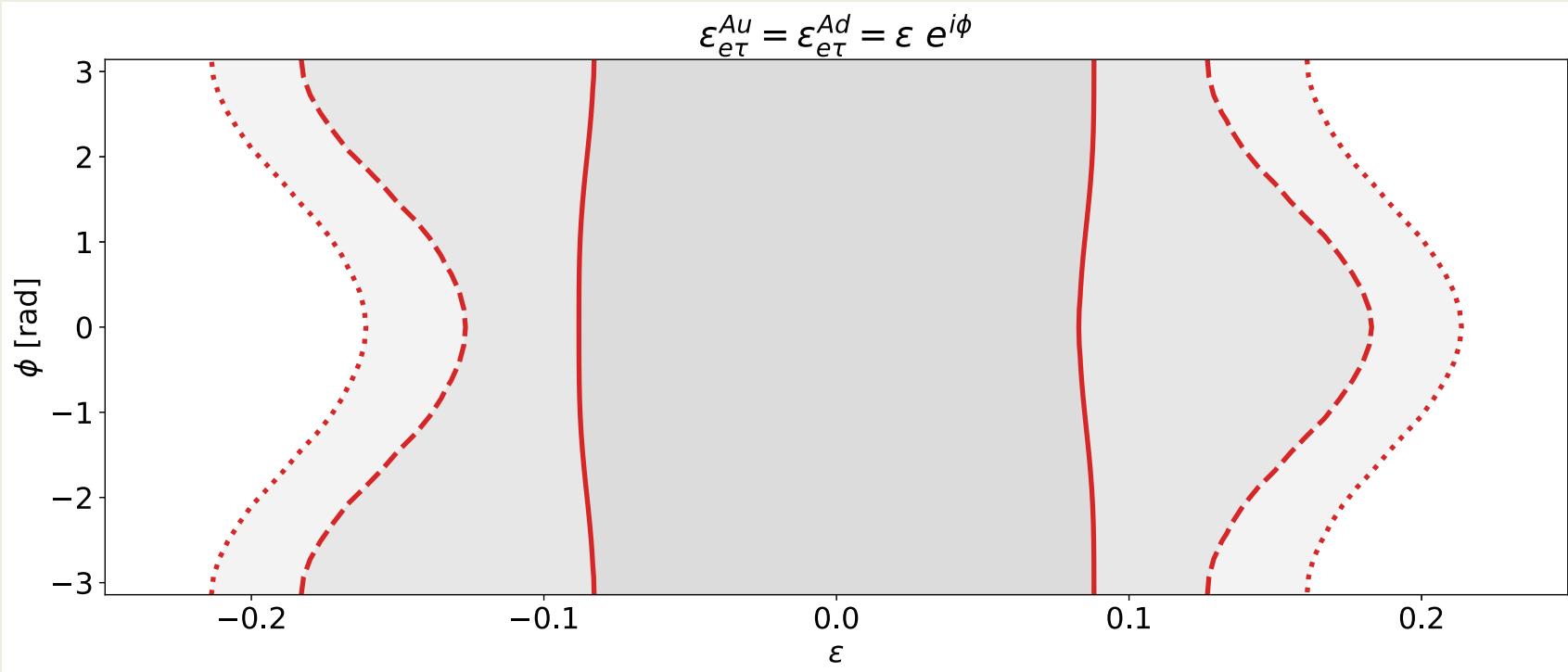




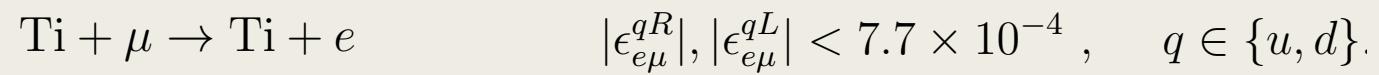
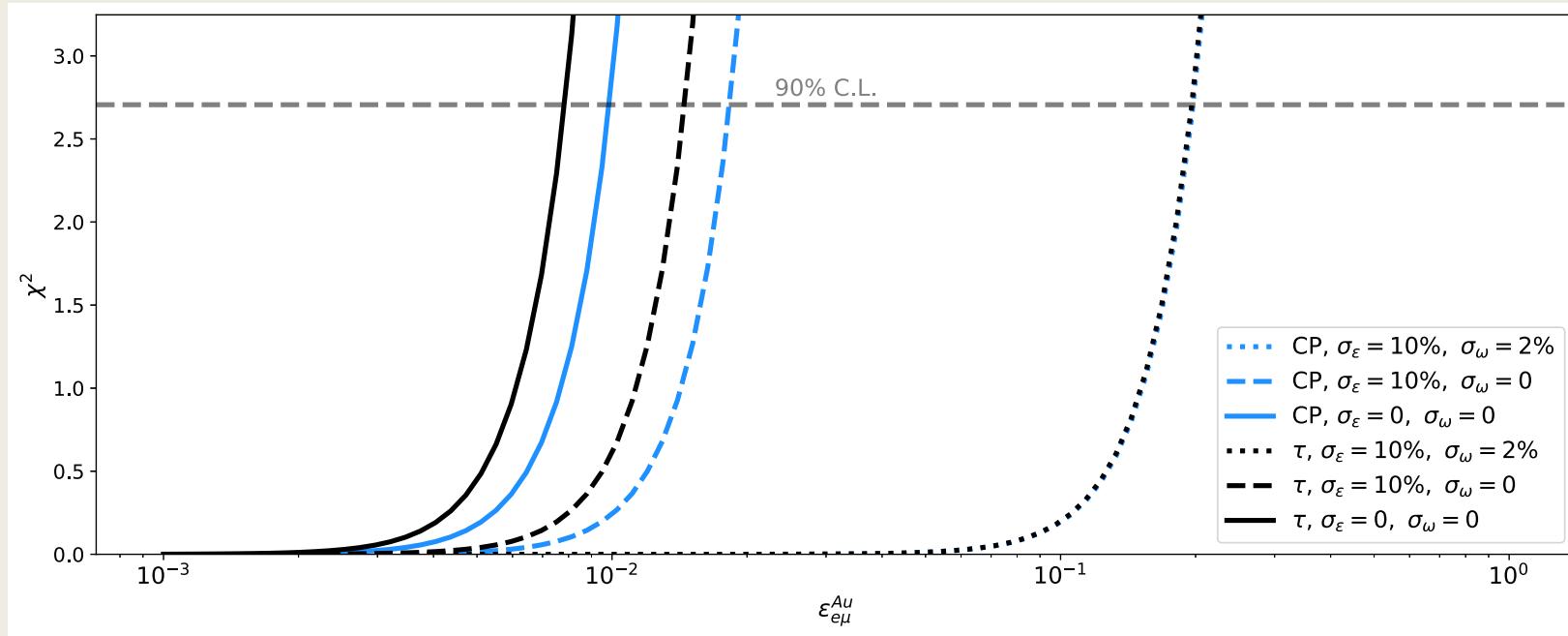


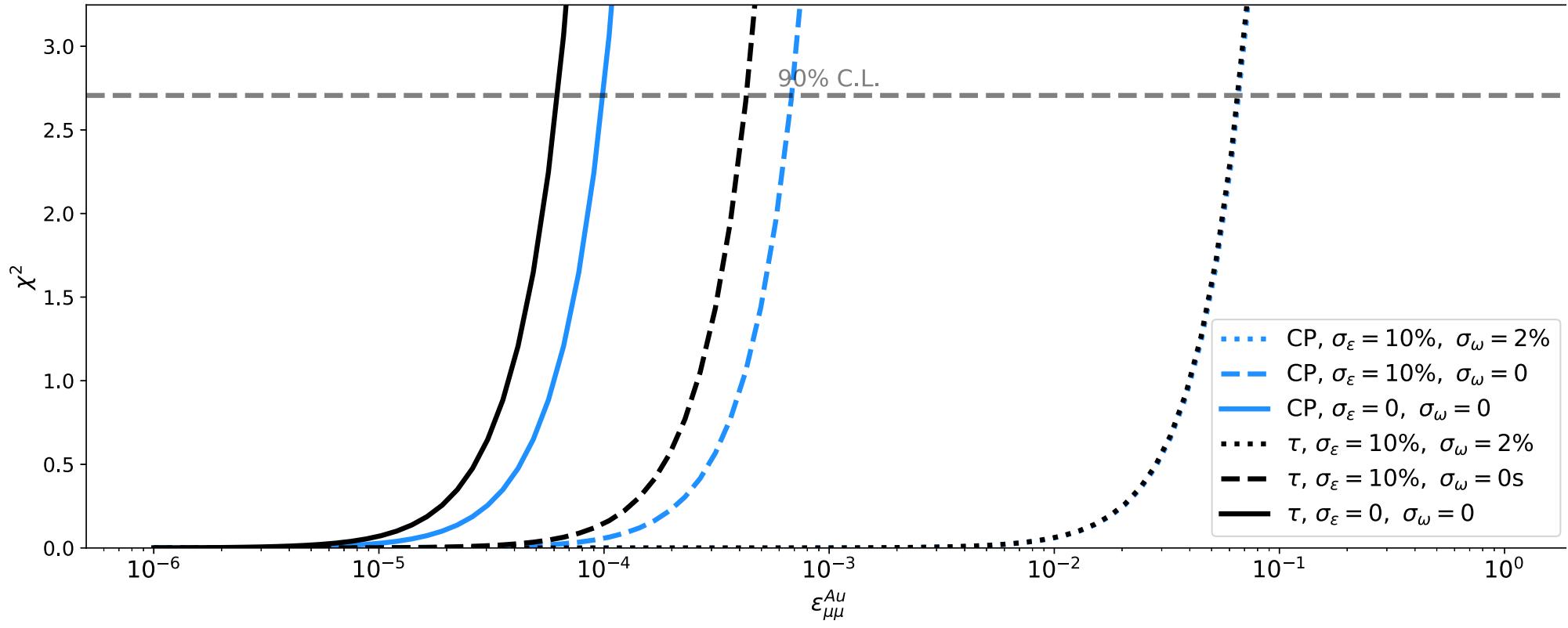
Non-trivial solution of SNO





Near Detector





$$|\epsilon_{\mu\mu}^{Au}| < 0.006, \quad |\epsilon_{\mu\mu}^{Ad}| < 0.018,$$

S. Davidson, C. Pena-Garay, N. Rius, and A. Santamaria,
JHEP 03, 011 (2003),

From NuTeV : $|\epsilon_{\mu\mu}^{Au}| < 0.006$, $|\epsilon_{\mu\mu}^{Ad}| < 0.018$,

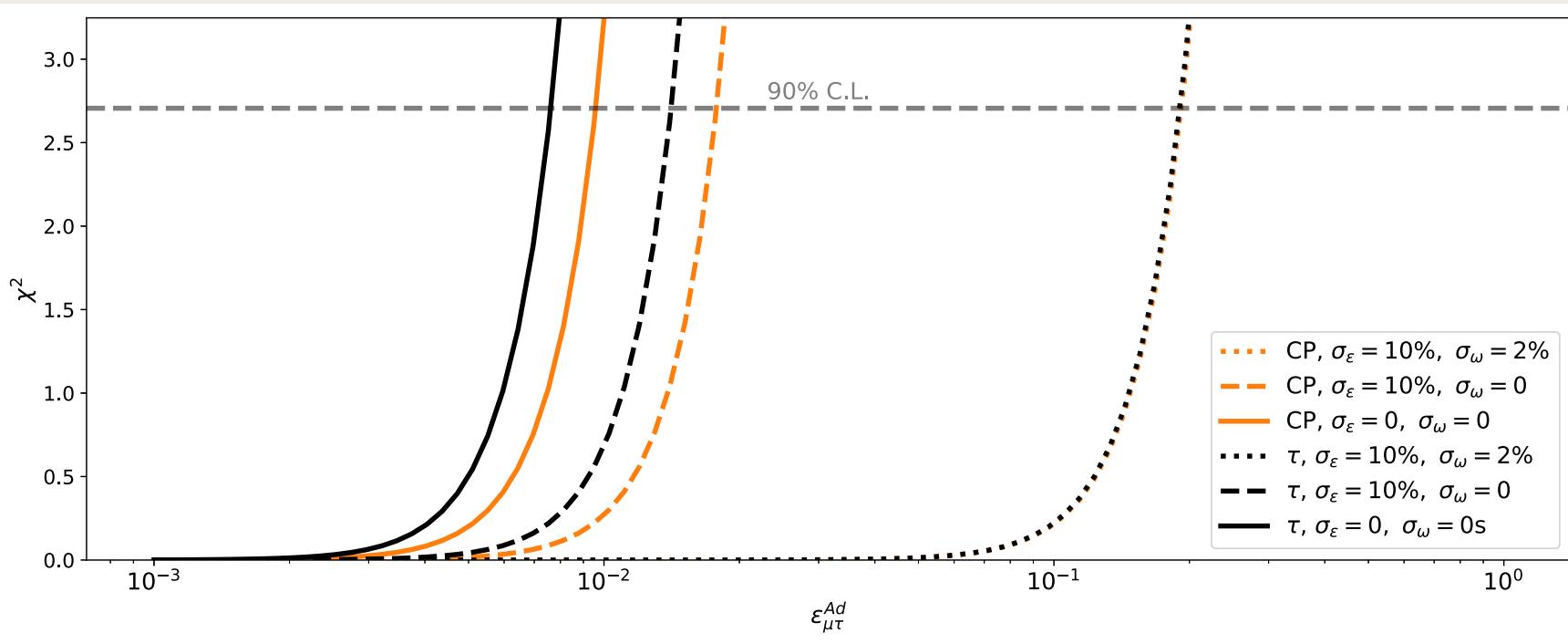
Ratio of NC/CC

For an **isospin symmetric** target is independent of PDFs

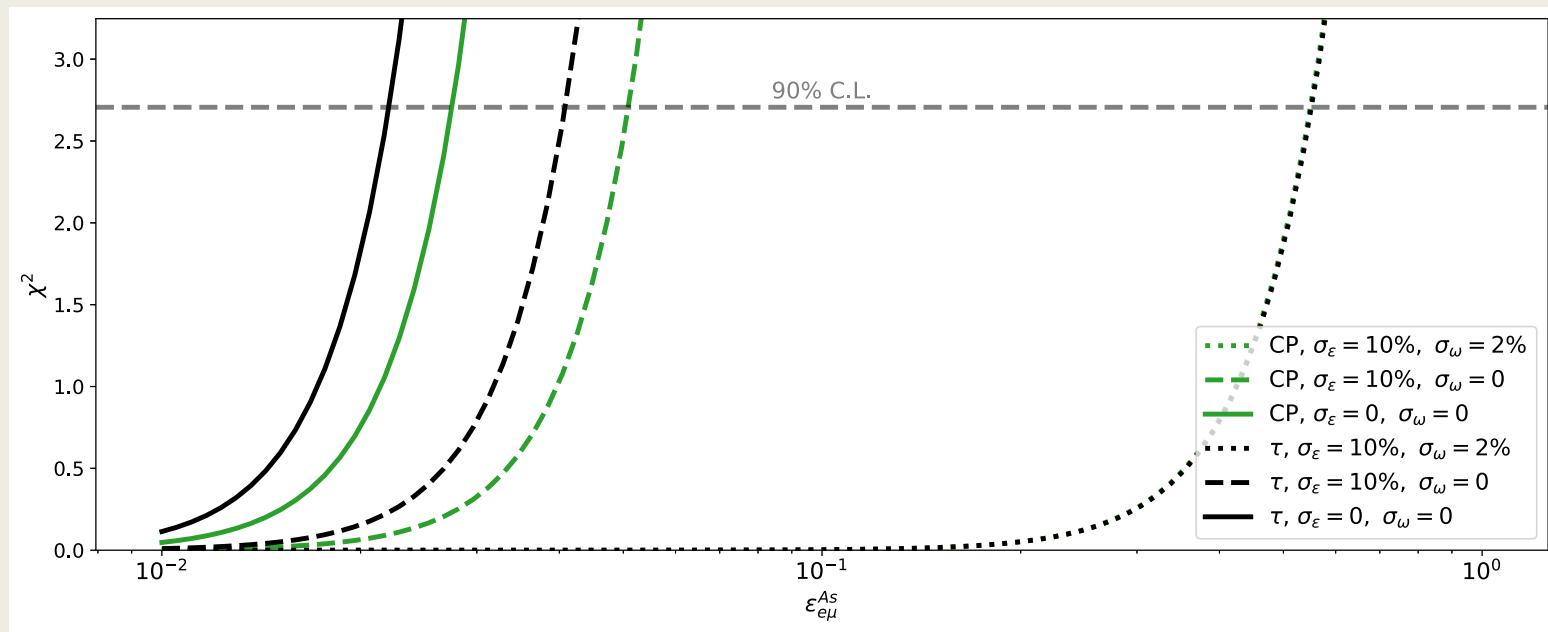
How accurate is this symmetry?

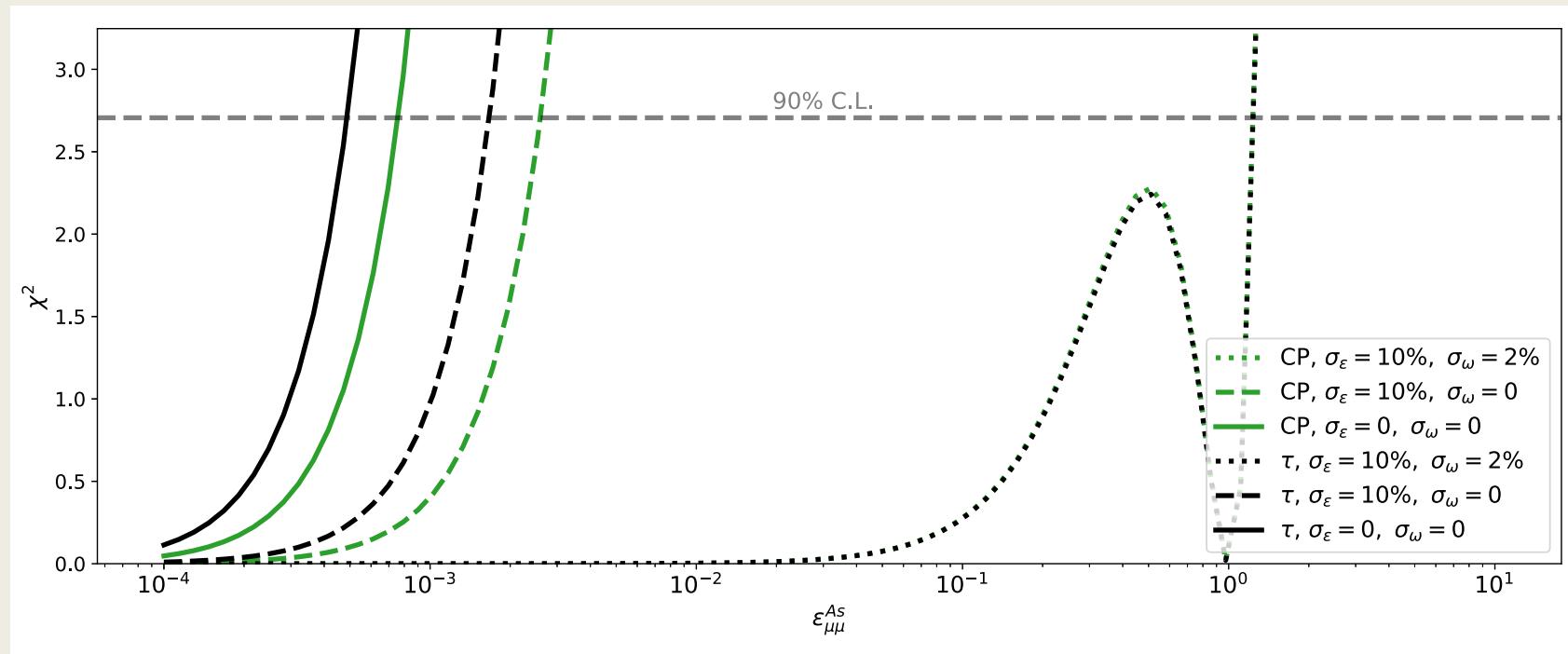
cannot be better than 3 %.

$\mathcal{O}(15\%)$



$$|\epsilon_{\mu\tau}^{Au}|, |\epsilon_{\mu\tau}^{Ad}| < 0.01,$$





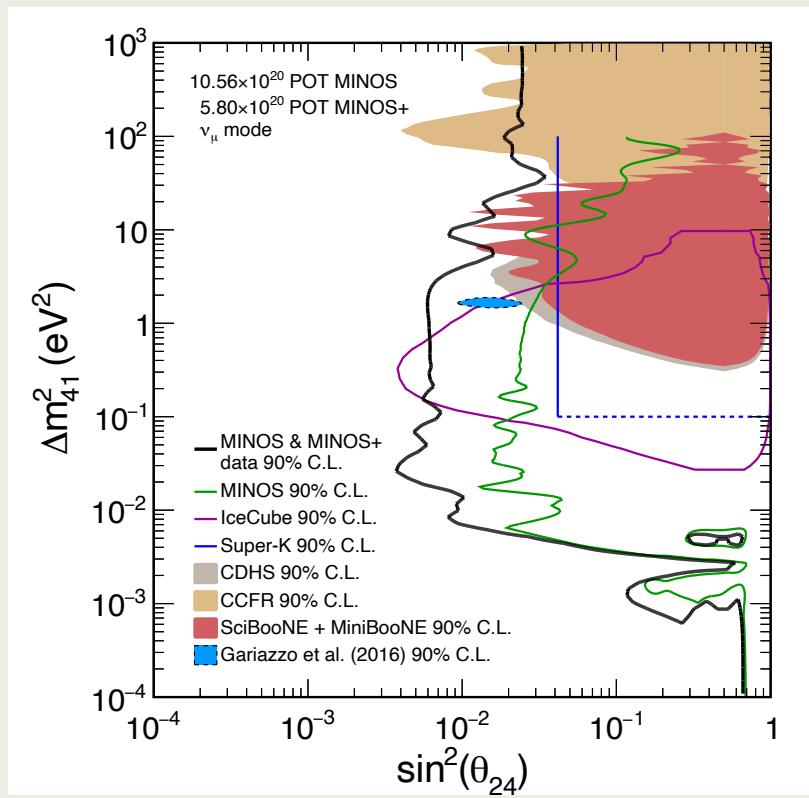
Summary of part 2

- The bound on Axial NSI can be improved by **neutral current measurements** at DUNE.
- The amount of improvements depends on how much the **systematic** errors are under control.
- While the **tau mode** is better for probing the **mu** components at near detector, the **CP mode** is more efficient in probing **ee**, **e tau** and **tau tau** components at the far detector.

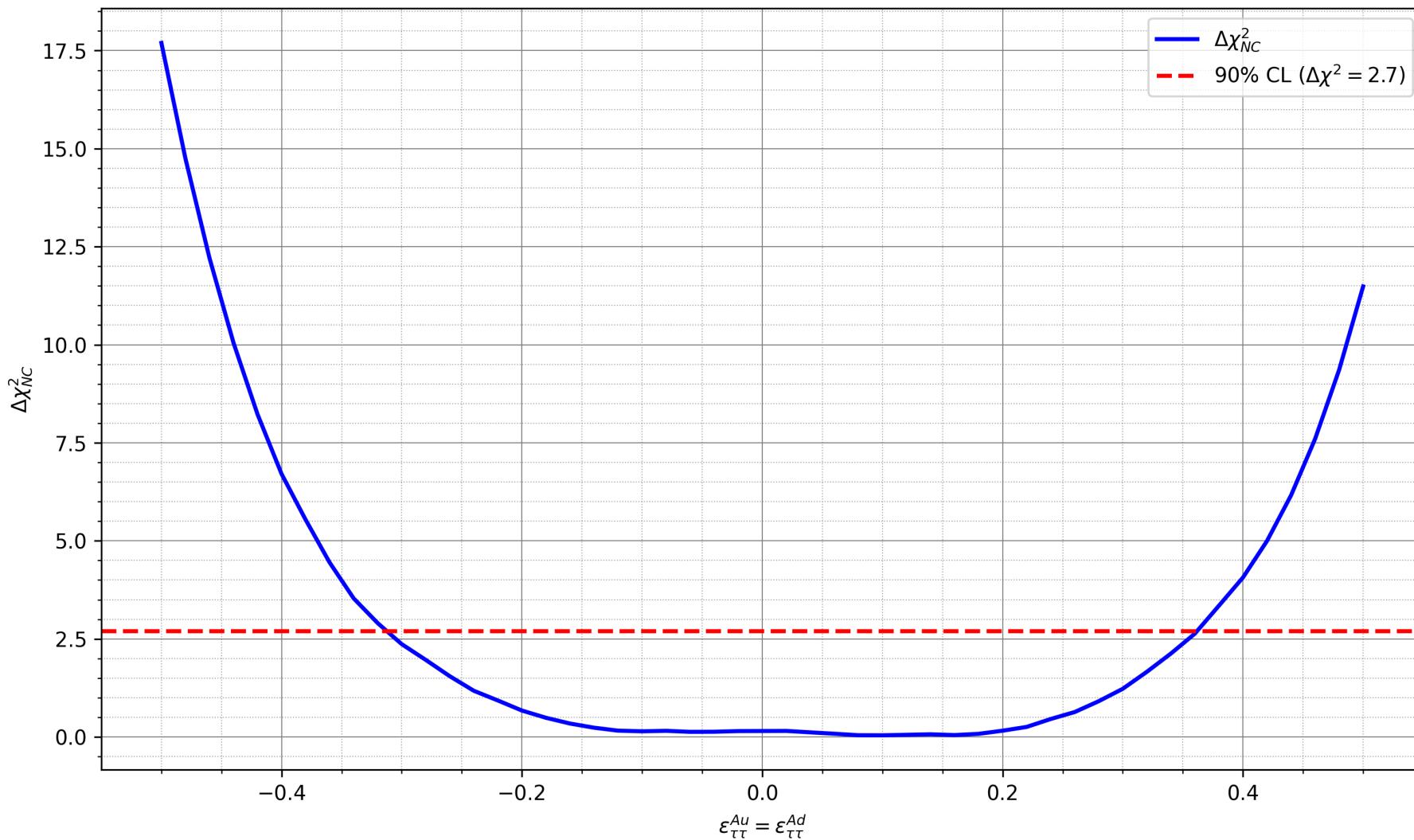
MINOS and MINOS+



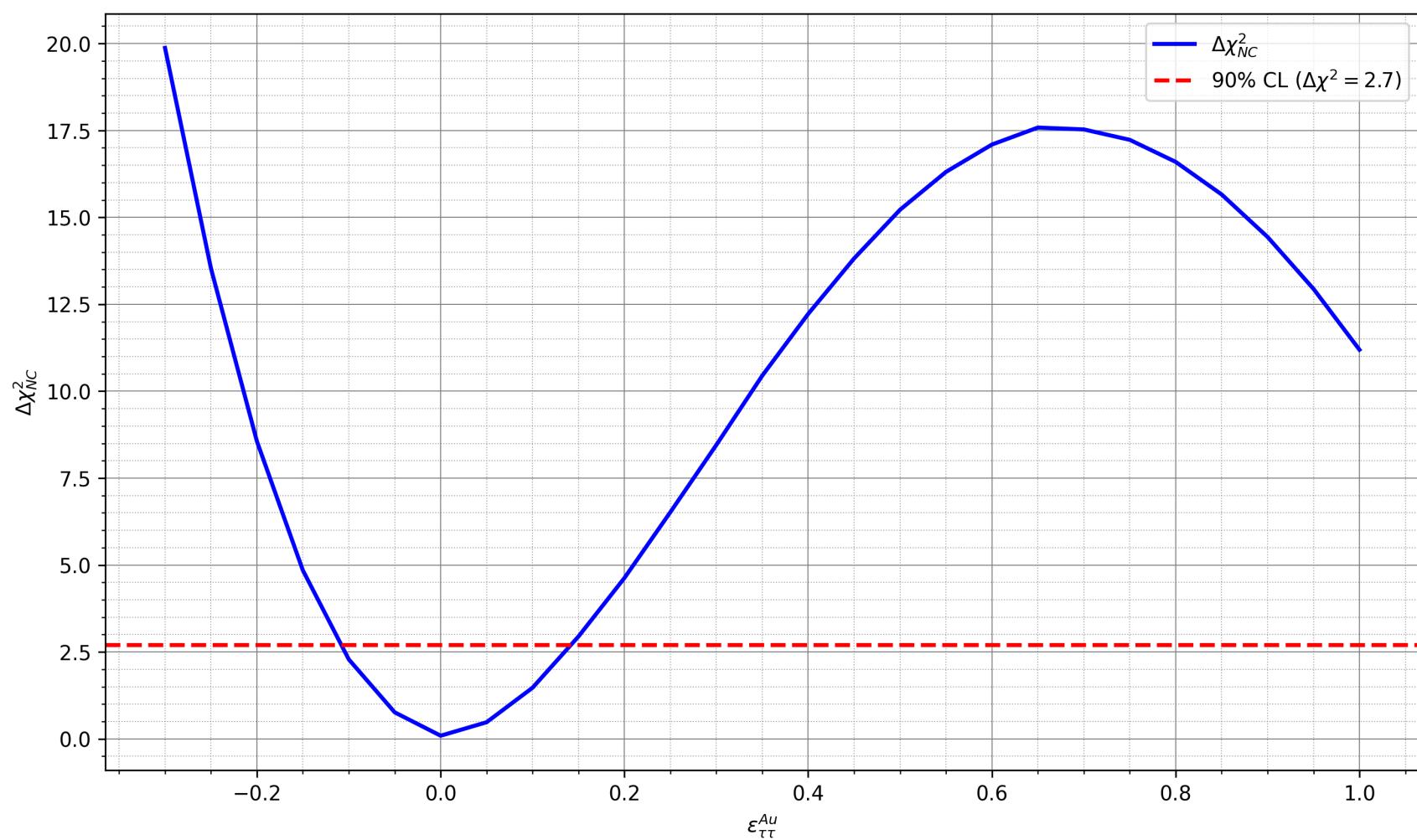
NC events of MINOS and MINOS+



MINOS+ collaboration,
Phys.Rev.Lett. 122 (2019) 9, 091803



Saeed Abbaslu and YF, work in progress



Saeed Abbaslu and YF, work in progress

Summary of part 3

- Stay tuned!
- Bounds from existing the MINOS and MINOS+ data on

$$|\epsilon_{\tau\tau}^{Aq}| \text{ and } |\epsilon_{e\tau}^{Aq}| < 0.2 - 0.3$$