

On the role of the  $z^5$ -term  
in the metric strain coefficient  
for the holographic description  
of magnetic catalysis in QGP

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# References

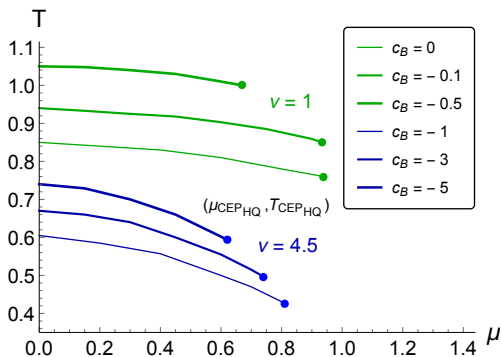
Irina Ya. Aref'eva, Alexey Ermakov, Ali Hajilou, K.R., Pavel Slepov  
Steklov Mathematical Institute of RAS

- Aref'eva, Ermakov, K.R., Slepov “*Holographic model for light quarks in anisotropic hot dense QGP with external magnetic field*”  
Eur.Phys.J.C **83** 79 (2023) arXiv:2203.12539 [hep-th]
- Aref'eva, Hajilou, K.R., Slepov “*Magnetic Catalysis in Holographic Model with two Types of Anisotropy for Heavy Quarks*” (2023)  
arXiv:2305.06345 [hep-th]
- K.R. “*Holographic Model with two Types of Anisotropy for Heavy Quarks: Magnetic Catalysis via  $z^5$ -term*” in progress

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# Magnetic Catalysis

$$b(z) = e^{-cz^2/2 - 2(p - c_B q_3)z^4}$$



*arXiv:2305.06345 [hep-th]*

# Twice Anisotropic Background

$$\mathcal{L} = R - \frac{f_0(\phi)}{4} F_0^2 - \frac{f_1(\phi)}{4} F_1^2 - \frac{f_3(\phi)}{4} F_3^2 - \frac{1}{2} \partial_\mu \phi \partial^\mu \phi - V(\phi)$$

$$A_\mu^0 = A_t(z) \delta_\mu^0 \quad F_1 = q_1 dx^2 \wedge dx^3 \quad F_3 = q_3 dx^1 \wedge dx^2$$

$$A_t(0) = \mu \quad g(0) = 1 \quad \text{Dudal et al., (2019)}$$

$$A_t(z_h) = 0 \quad g(z_h) = 0 \quad \phi(z_0) = 0 \rightarrow \sigma_{\text{string}}$$

$$ds^2 = \frac{L^2}{z^2} \mathbf{b}(z) \left[ -g(z) dt^2 + dx_1^2 + \left(\frac{z}{L}\right)^{2-\frac{2}{\nu}} dx_2^2 + e^{c_B z^2} \left(\frac{z}{L}\right)^{2-\frac{2}{\nu}} dx_3^2 + \frac{dz^2}{g(z)} \right]$$

*I.A., A.G. (2014), Giataganas (2013)*

*Gürsoy, Järvinen et al., (2019)*

$$\mathbf{b}(z) = e^{2\mathcal{A}(z)} \rightarrow \text{quarks mass}$$

“Bottom-up approach”

$$\mathcal{A}(z) = -cz^2/4 \rightarrow \text{heavy quarks background } (\mathbf{b}, \mathbf{t}) \quad \text{Andreev, Zakharov (2006)}$$

$$\mathcal{A}(z) = -a \ln(bz^2 + 1) \rightarrow \text{light quarks background } (\mathbf{d}, \mathbf{u}) \quad \text{Li, Yang, Yuan (2020)}$$

# “Heavy” Quarks Warp Factor

$$\mathcal{A}(z) = - cz^2/4$$

*Aref'eva, K.R., Slepov*  
*JHEP 07 161 (2021)*  
*arXiv:2011.07023 [hep-th]*



$$\mathcal{A}(z) = - cz^2/4 - (p - c_B q_3)z^4$$

*Aref'eva, Hajilou, K.R., Slepov*  
*arXiv:2305.06345 [hep-th]*

$$\mathcal{A}(z) = - az^2 - dB^2 z^5$$

*Bohra, Dudal, Hajilou, Mahapatra*  
*PRD 103 086021 (2021)*  
*arXiv:2010.04578 [hep-th]*

$$f_0 = e^{-(c+q_3^2)z^2} \frac{z^{-2+\frac{2}{\nu}}}{\sqrt{\mathfrak{b}}}$$

$$a = 0.15 \text{ GeV}^2, \quad c = 1.16 \text{ GeV}^2$$

$$d > 0.05$$

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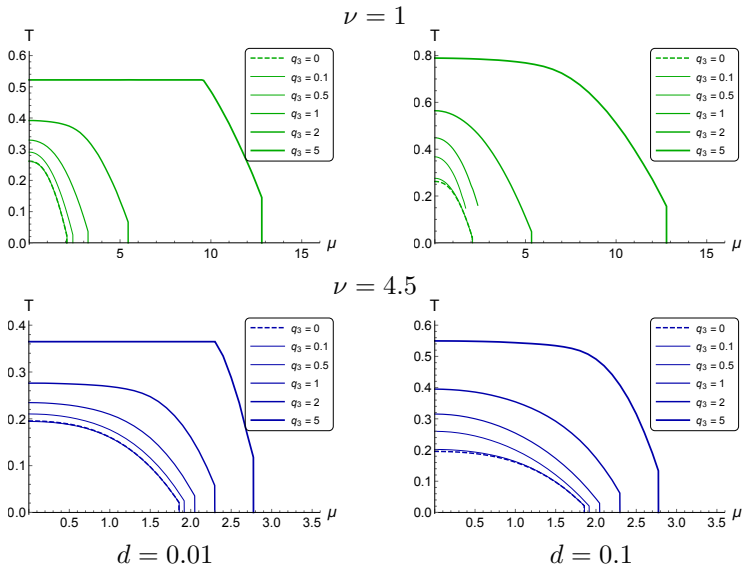
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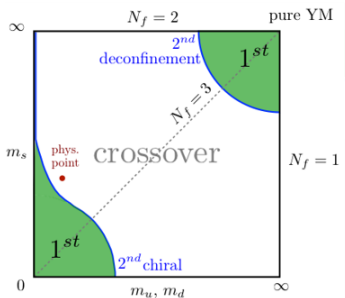
Magnetic Catalysis:  $T(z_h, q_3)$  for fixed  $c_B < 0, \forall d$

# Phase Diagram $T(\mu)$ , $c_B = -0.01$



# QCD Phase Diagram: Lattice

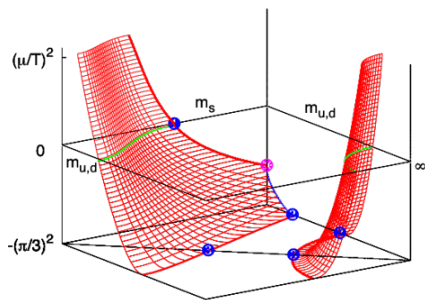
Phase diagram  
on quark mass



Columbia plot

*Brown et al., PRL (1990)*

Main problem with  $\mu \neq 0$   
Imaginary chemical potential method

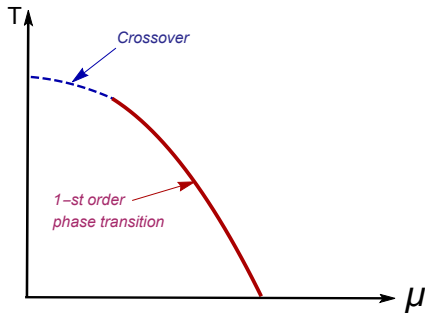


*Philipsen, Pinke, PRD (2016)*

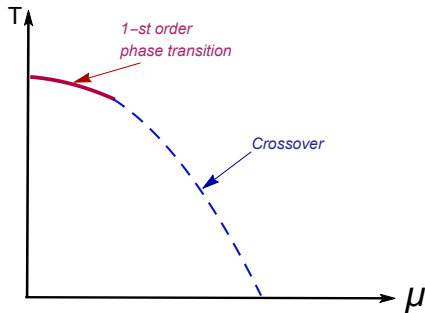


# “Light” and “Heavy” Quarks from Columbia Plot

Light quarks

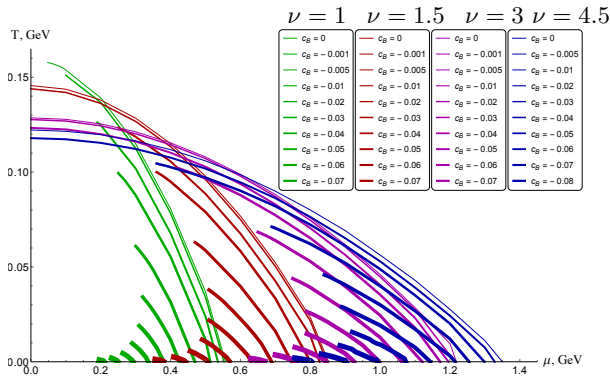


Heavy quarks



# “Light” Quarks: Inverse Magnetic Catalysis

$$b(z) = e^{-a \ln(bz^2+1)}$$



*Eur.Phys.J.C* **83** 79 (2023)

# Conclusions

Terms  $z^4$  and  $z^5$  in the warp-factor give a wide opportunity to fit Lattice results and experimental data for large chemical potential

- The coefficient value in  $z^5$ -term doesn't seem to determine MC/IMC behavior (no  $d > 0.05$  limit found)
- Stable solution with MC effect needs fixed  $c_B < 0$
- Increasing  $d$  value rises PT temperature
- Increasing  $d$  value has weak influence on  $\mu_{max}$ :  $T(\mu_{max}) = 0$
- Primary anisotropy lowers PT temperature and stabilises  $\mu_{max}$  value

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## What to do next

- Temporal Wilson loops
- Cornell potential and string tension
- Drag forces and energy losses
- Other characteristics (susceptibility, transport coefficients,  $\eta/s$ , direct-photon spectra, jet quenching, thermalization time, etc)

Thank you  
for your attention

# BACKUP. Relations between 5-dim backgrounds and 4-dim models

- Relations between parameters of the 5-dim background (black hole) and thermodynamical parameters are the following:
  - $T_{BH} = T_{QCD}$ , where  $T_{BH}$  is the temperature of the 5-dim black hole;
  - $A_0(z) = \mu_B - \rho_B z^2 + \mathcal{O}(z)$ , where  $A_0(z)$  is the 0-component of the electromagnetic field  $A_\mu(z)$ ,  $\mu_B$  is the baryonic chemical potential,  $\rho_B$  is the density and  $z$  is the 5-dimensional coordinate;
  - $S_{BH} = s$ , where  $S_{BH}$  is the entropy of the black hole, which as usual is defined by the square of the black hole horizon,  $s$  is the thermodynamical entropy;
  - $F_{BH} = -p$ , where  $F_{BH}$  is the free energy of the black hole,  $p$  is the thermodynamical pressure.