

CONSTRAINTS ON MODIFIED THEORIES OF GRAVITY FROM THE LATEST LIGO-VIRGO RINGDOWN OBSERVATIONS

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CONTENTS

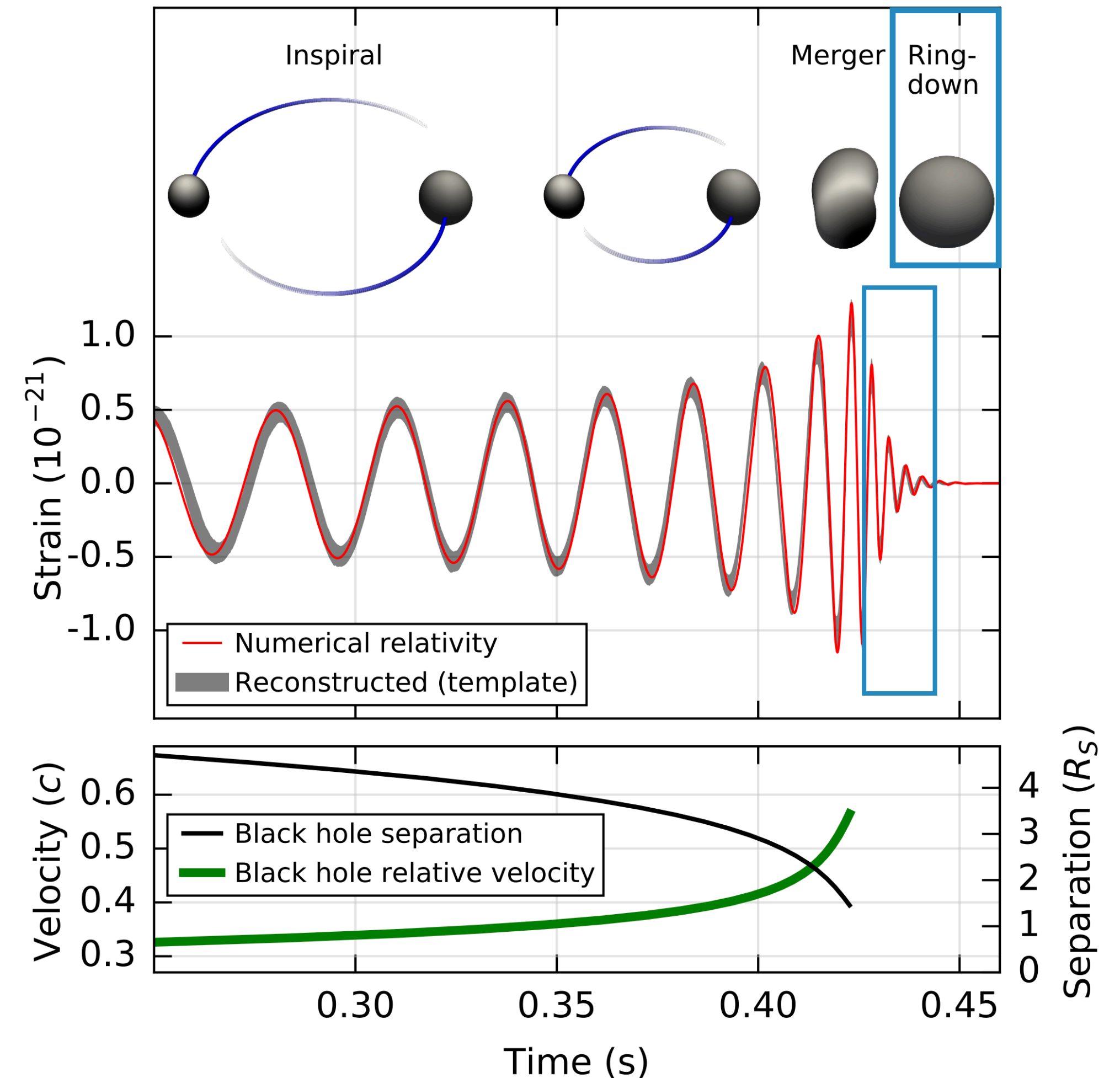
- Current status of **Observational black hole spectroscopy**;
- The “**So what?**” test
- Beyond the LVC parametrisation: **ParSpec**
- ParSpec constraints on **modified gravity** from black holes spectra
- **Comparison** to other **experimental bounds**
- A **non-perturbative** beyond-Kerr case: Kerr-Newman black holes

BLACK HOLE RINGDOWN

- Binary black holes **remnant** approaches equilibrium emitting damped **normal-modes** (“*spacetime signature*”).
- **Spectrum** predicted by **perturbation theory**:

$$h_+ - i h_\times = -\frac{M}{r} \sum_{l,m,n} \mathcal{A}_{lmn} S(\theta, \phi) e^{i\omega_{lmn}t} e^{-t/\tau_{lmn}}$$

- “Simple” prediction (“easy” to incorporate *beyond-GR* effects)
- Sensitive to \sim *light ring* physics.



SCIENCE GOALS

- **Testing** the emission:
 - Remnant compact object **nature**;
Are we really observing black holes?
 - General Relativity predictions for **spectral emission**;
Is General Relativity a correct description of gravity at high curvatures?
 - Black Hole **Uniqueness Theorems**;
Do non-extremal black holes have additional hairs?
 - Possible **quantum horizon** effects and classical **BH thermodynamics**.
Is our classical description of black holes valid?

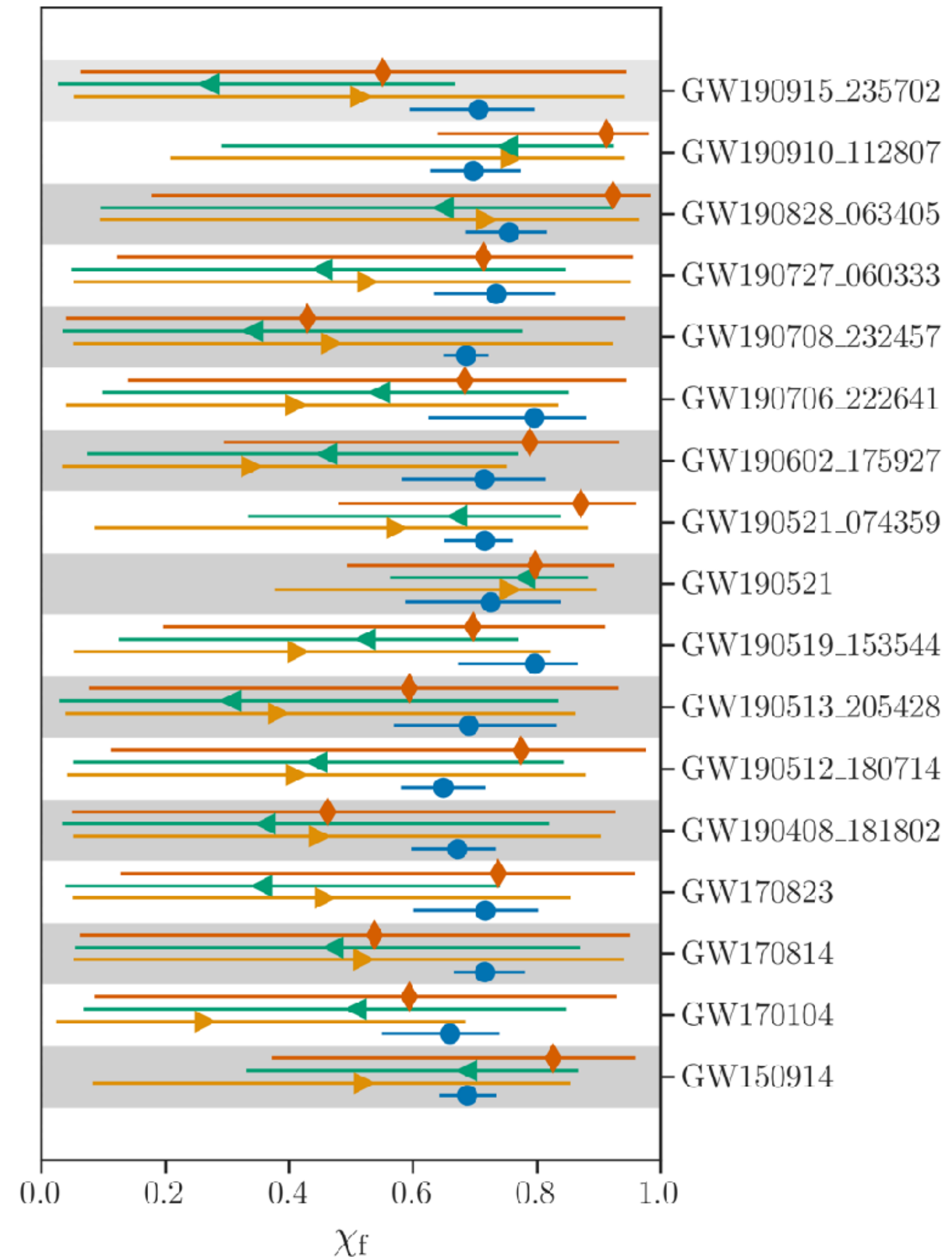
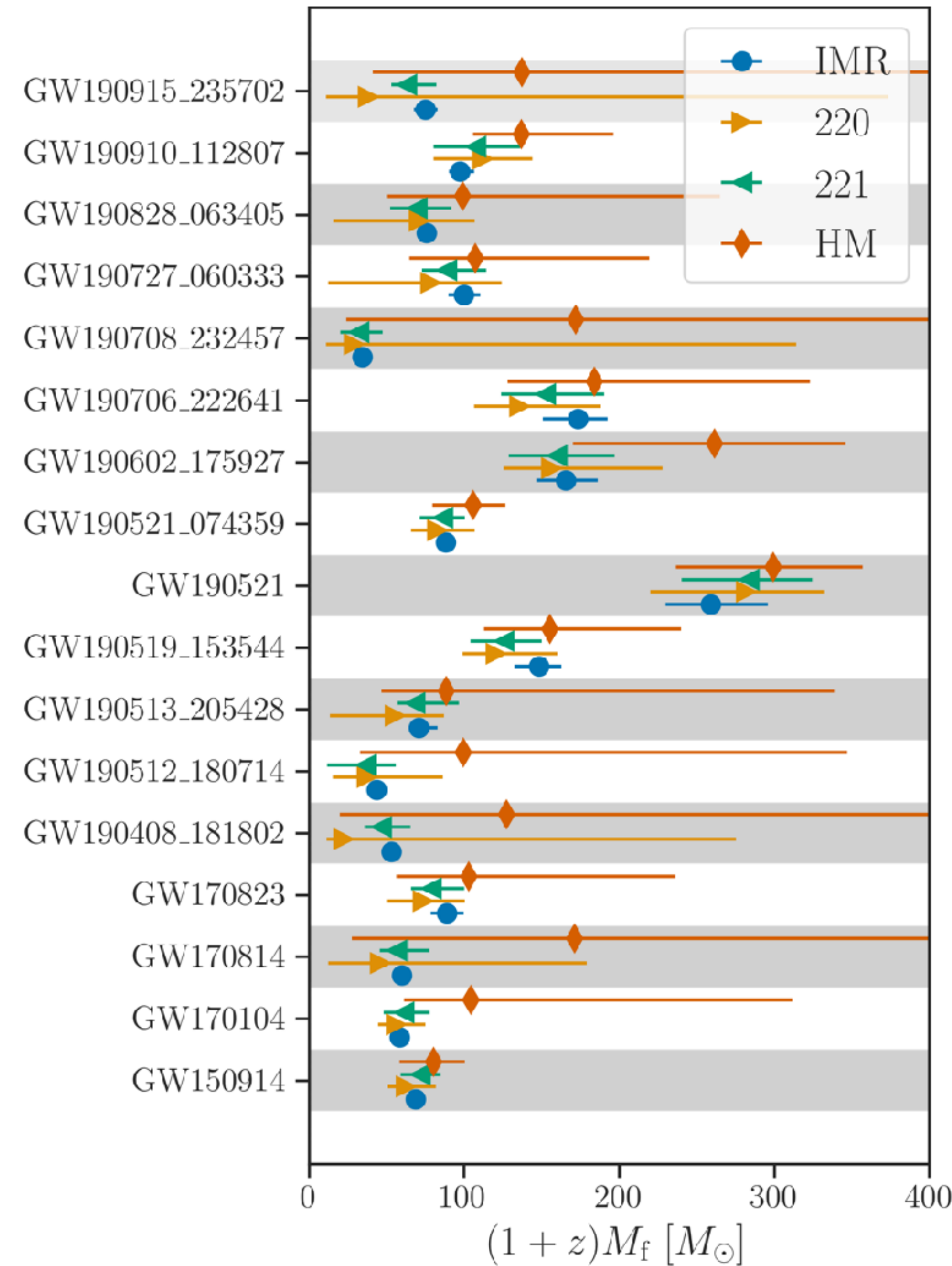
MISSING PHYSICS?

- Why GW merger-ringdown observations compared to **other experiments?**
(Solar System, Binary Pulsars, X-ray binaries)
- **Largest curvature** regime experimentally accessible;
- **Gauge** the contribution of **missing physics** for precision tests:
 - ~~Cosmological expansion~~
 - ~~Dark matter~~
 - ~~Accretion, magnetic fields, electric charge~~
- GW ringdown tests are **clean!**

BLACK HOLE RINGDOWN CATALOG

- First **catalog** of ringdown-only observations:

Image credit: LIGO-Virgo/Rico Lo



Higher modes	Overtones	
$\log_{10} \mathcal{B}_{220}^{\text{HM}}$	$\log_{10} \mathcal{B}_{220}^{221}$	$\log_{10} \mathcal{O}_{\text{GR}}^{\text{modGR}}$
0.03	0.63	-0.34
0.26	-0.20	-0.23
0.04	-0.19	-0.11
0.02	-0.98	-0.07
-0.05	-1.02	-0.02
0.09	-0.42	0.03
0.09	-0.54	-0.05
0.21	-0.00	-0.11
0.12	-0.86	-0.50
-0.04	1.29	-0.27
0.61	-1.56	0.32
-0.06	-0.64	-0.45
-0.11	-0.17	-0.02
-0.02	-1.65	-0.40
0.05	-0.72	-0.05
-0.10	-0.64	-0.40
0.06	-0.37	-0.04

BLACK HOLE RINGDOWN CATALOG

- First **catalog** of ringdown-only observations:



TESTS OF GENERAL RELATIVITY

- **Bounds on deviations** from the GR spectrum.

Data consistent with GR.

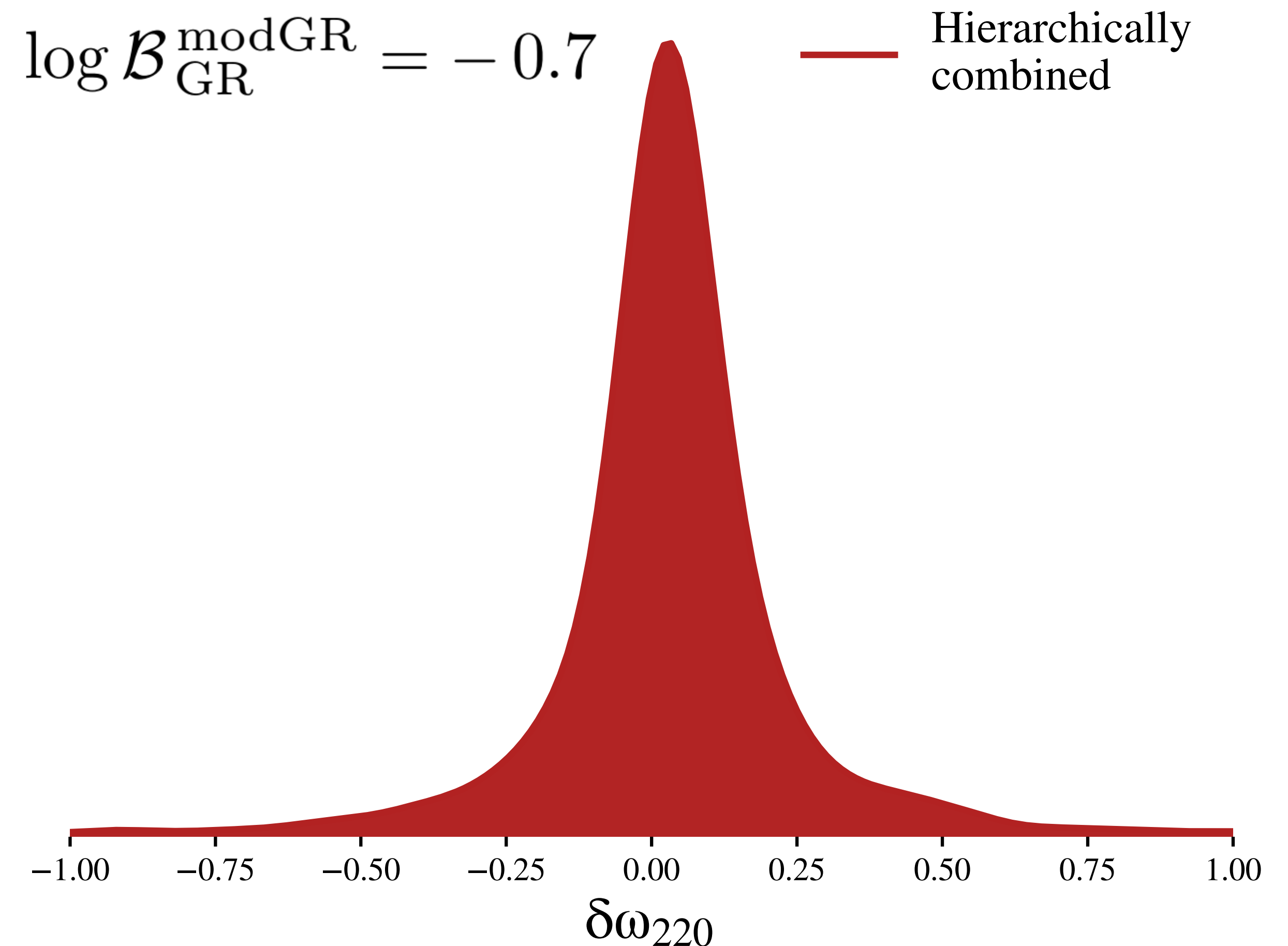
- **Deviations** parameterized as:

$$\omega = \omega^{Kerr} \cdot (1 + \delta\omega)$$

$$\tau = \tau^{Kerr} \cdot (1 + \delta\tau)$$

$$\delta\omega_{220} = 0.03^{+0.38}_{-0.35}$$

See also: Ghosh+, arXiv:2104.01906



THE “SO WHAT?” TEST

- Do these results pass the “**So what?**” test?
 - Take an **urn** full of a gaussian mixture of **theoretical particle physicists** and **general relativists**, with a possibly non-null intersection.
 - Draw them at random and have **them look** separately at **these results**.
 - **Count** how many people say: “So what?”
 - If it's more than **42%** of them, the test is **failed**.



LOST IN TRANSLATION

- **Implications** of **LVK** results to specific **alternative theories** of gravity **not immediate** (unlike, e.g. graviton mass);
- Why doesn't the **LVK constrain** specific and well-motivated **beyond-GR theories**?
 - Most theories are **not proven to be well-posed**.
Difficult to rigorously justify certain approximations or understand merger-ringdown in a specified theory.
 - **Huge amount of possibilities** and of effects to take into account
(isospectrality breaking, parity violations, additional modes, scalar-fields dynamics...)
- **Policy** of the Testing GR group: **do not consider** specific theories for which a **rigorous framework** has **not** been **established**.

- **Consistent framework** for perturbative **constraints** valid on **specific modified theories** of gravity:

$$\omega_K = \frac{1}{M} \sum_{j=0}^{N_{max}} \chi^j \omega_K^{(j)}$$

Expand each QNM parameter in a polynomial expansion in the remnant spin.

$$\tau_K = M \sum_{j=0}^{N_{max}} \chi^j \tau_K^{(j)}$$

Extract the mass and spin structure in polynomial form.

- **Consistent framework** for perturbative **constraints** valid on **specific modified theories** of gravity:

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Numerical constants

- **Consistent framework** for perturbative **constraints** valid on **specific modified theories** of gravity:

$$\omega_K = \frac{1}{M} \sum_{j=0}^{N_{max}} \chi^j \omega_K^{(j)} (1 + \gamma \delta \omega_K^{(j)}) ,$$

$$\tau_K = M \sum_{j=0}^{N_{max}} \chi^j \tau_K^{(j)} (1 + \gamma \delta \tau_K^{(j)}) .$$

Proportional to action coupling(s):

$$\gamma := \left(\frac{\ell c^2 (1+z)}{G M} \right)^p$$


Add deviations at each given order.

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Proportional to action coupling(s):

$$\gamma := \left(\frac{\ell c^2 (1+z)}{G M} \right)^p$$

Add deviations at each given order.

Also numerical constants!

Independent of specific signal.

- **Consistent framework** for perturbative **constraints** valid on **specific modified theories** of gravity:

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GR values!



Proportional to action coupling(s):

$$\gamma := \left(\frac{\ell c^2 (1+z)}{G M} \right)^p$$

- **Advantages:**
 - Applicable to large classes of **beyond-GR** theories;
 - **Source-independent** parameters: optimal constraints when combining events;
 - Perturbative expansion: can retain **GR remnant mass and spin** parameters;
 - Direct connection with **parameters** appearing in the **action**.
- Consequence: much **smaller number** of signals (or smaller SNR) to **detect** modifications from GR predictions.

THEORY PARAMETER SPACE

- **p=0** (e.g. certain **scalar-tensor** or **Lorentz-violating**)

$$S_{\text{\AE}} = \frac{1}{16\pi G_{\text{\AE}}} \int \sqrt{-g} \left(R - M^{\alpha\beta}{}_{\mu\nu} \nabla_{\alpha} u^{\mu} \nabla_{\beta} u^{\nu} \right) d^4x$$

- **p=2** (e.g. **Kerr-Newman** or Dark photon)

$$\mathcal{L} = \sqrt{-g} \left(\frac{R}{16\pi} - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} - \frac{1}{4} B_{\mu\nu} B^{\mu\nu} + 4\pi e j_{\text{em}}^{\mu} A_{\mu} + 4\pi e_h j_h^{\mu} B_{\mu} + 4\pi \epsilon e j_h^{\mu} A_{\mu} \right)$$

- **p=4** (e.g. **Einstein-scalar-Gauss-Bonnet** or **dynamical Chern-Simons**)

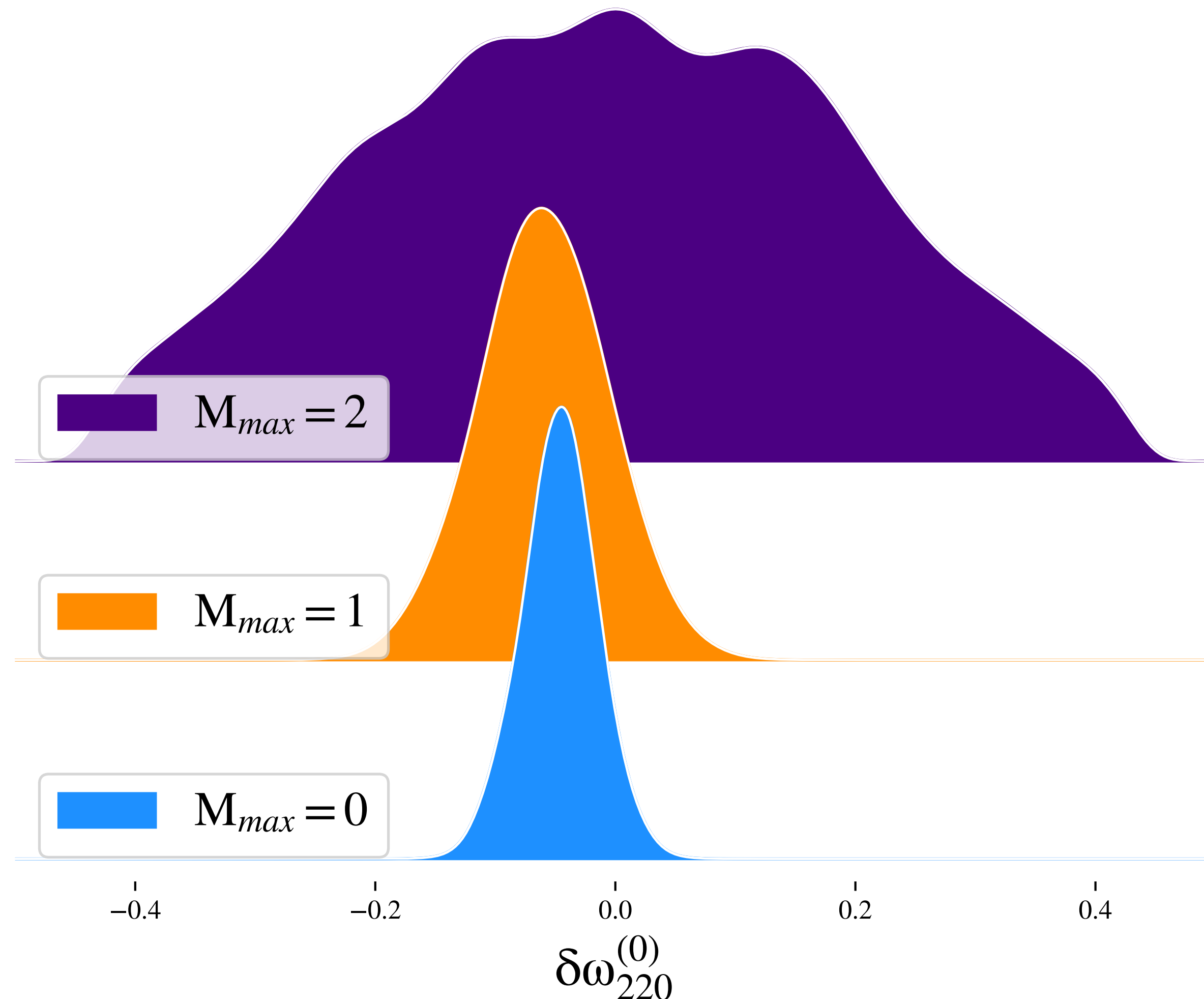
$$S \equiv \int \frac{m_{\text{pl}}^2}{2} d^4x \sqrt{-g} \left[R - \frac{1}{2} (\partial\vartheta)^2 + 2\alpha_{\text{GB}} f(\vartheta) \mathcal{R}_{\text{GB}} \right], \quad S \equiv \int d^4x \sqrt{-g} \left(\frac{m_{\text{pl}}^2}{2} R - \frac{1}{2} (\partial\vartheta)^2 - \frac{m_{\text{pl}}}{8} \ell^2 \vartheta {}^*RR \right)$$

- **p=6** (e.g. **Effective Field Theories**)

$$S_{\text{eff}} = \int d^4x \sqrt{-g} 2M_{\text{pl}}^2 \left(R - \frac{\mathcal{C}^2}{\Lambda^6} - \frac{\tilde{\mathcal{C}}^2}{\tilde{\Lambda}^6} - \frac{\tilde{\mathcal{C}}\mathcal{C}}{\Lambda_-^6} \right)$$

RESULTS FOR SCALAR DEVIATIONS

- Constraints on theories with scalar coupling in the action:



$$\delta\omega_{220}^0 = -0.05^{+0.05}_{-0.05}$$

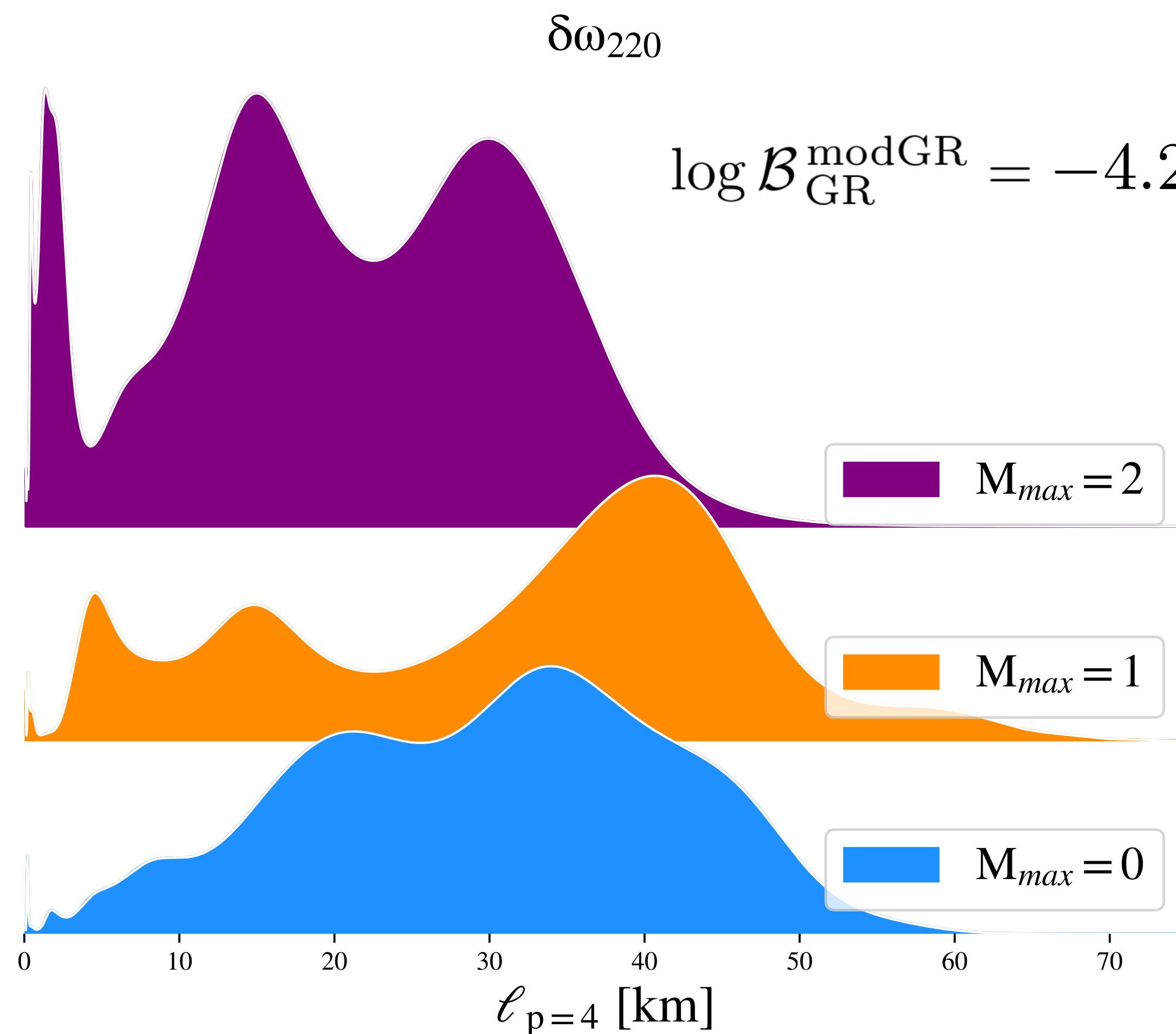
$$\log \mathcal{B}_{\text{GR}}^{\text{modGR}} = -14.55$$

Improvement of a **factor of ~ 2** wrt
LVC parametrization.

Reduction **factor of ~ 4** in N_{events}
to detect a violation.

RESULTS FOR QUADRATIC GRAVITY

- Constraints on theories introducing quadratic curvature terms in the action:



$$\ell_{\text{p}=4} \lesssim 35 \text{ km}$$

dCS: (NICER+LVC) $\ell \lesssim 30 - 50 \text{ km}$

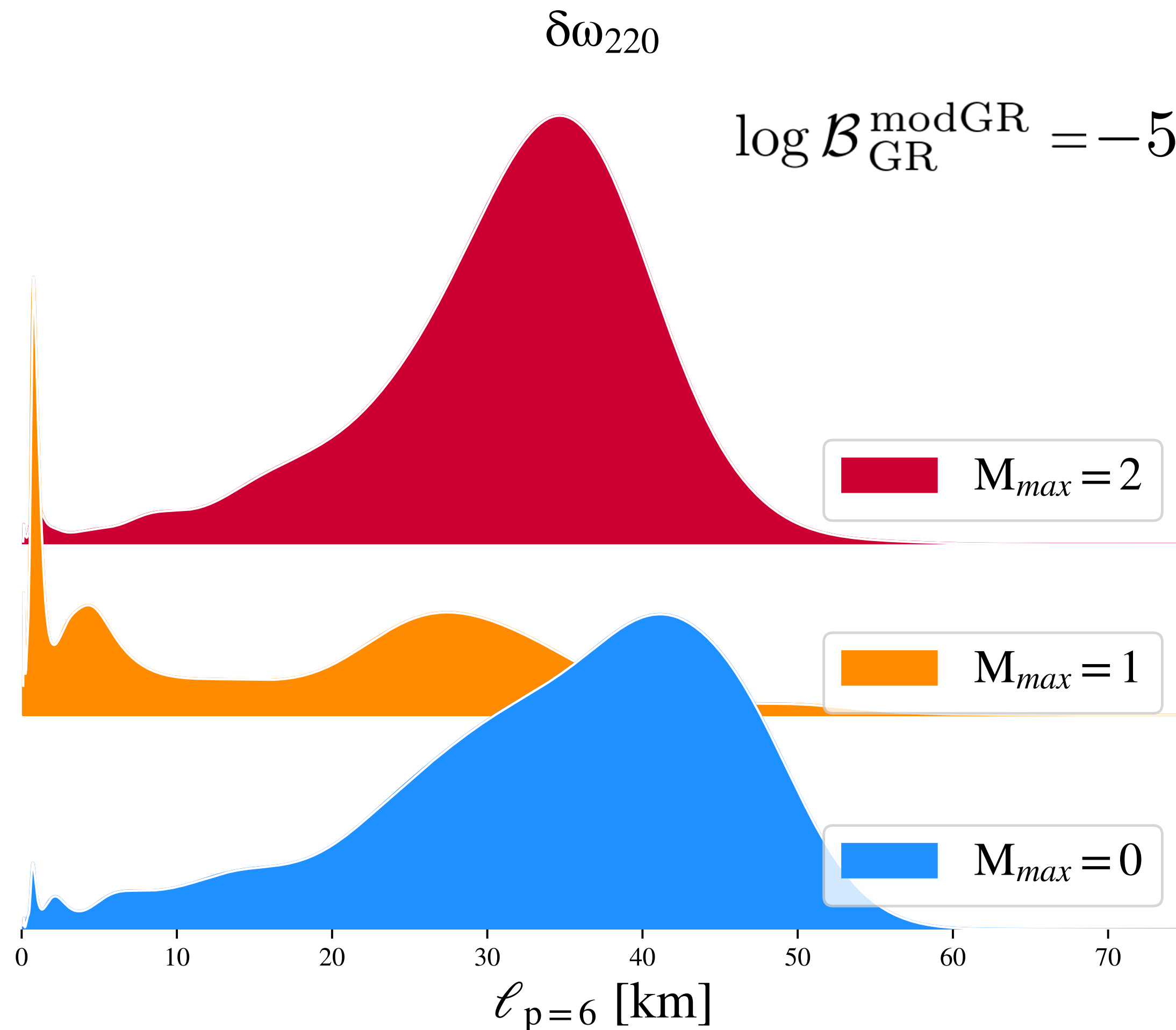
EsGB: (X-rays) $\ell \lesssim 6 - 10 \text{ km}$

New best non-perturbative constraint:

GW190814: (if BBH) $\ell \lesssim 3.3 \text{ km}$

RESULTS FOR EFFECTIVE FIELD THEORIES

- Constraints on viable Effective Field Theories of beyond-GR gravity:



$$\ell_{\text{p}=6} \lesssim 42 \text{ km}$$

Previous best bound from GW inspiral:

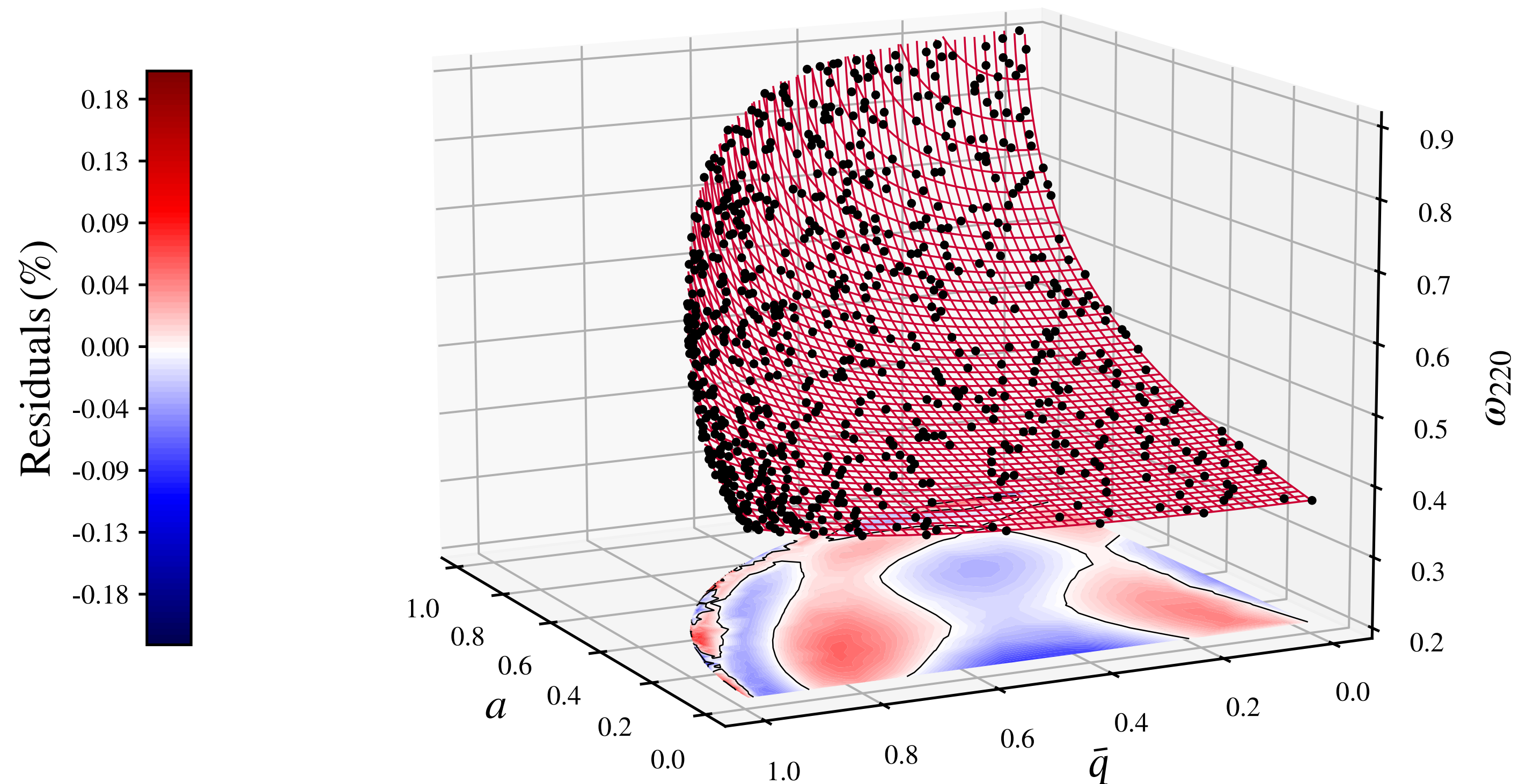
$$\ell \lesssim 150 \text{ km}$$

(Now probing finite-size effects)

KERR-NEWMAN SPECTRUM

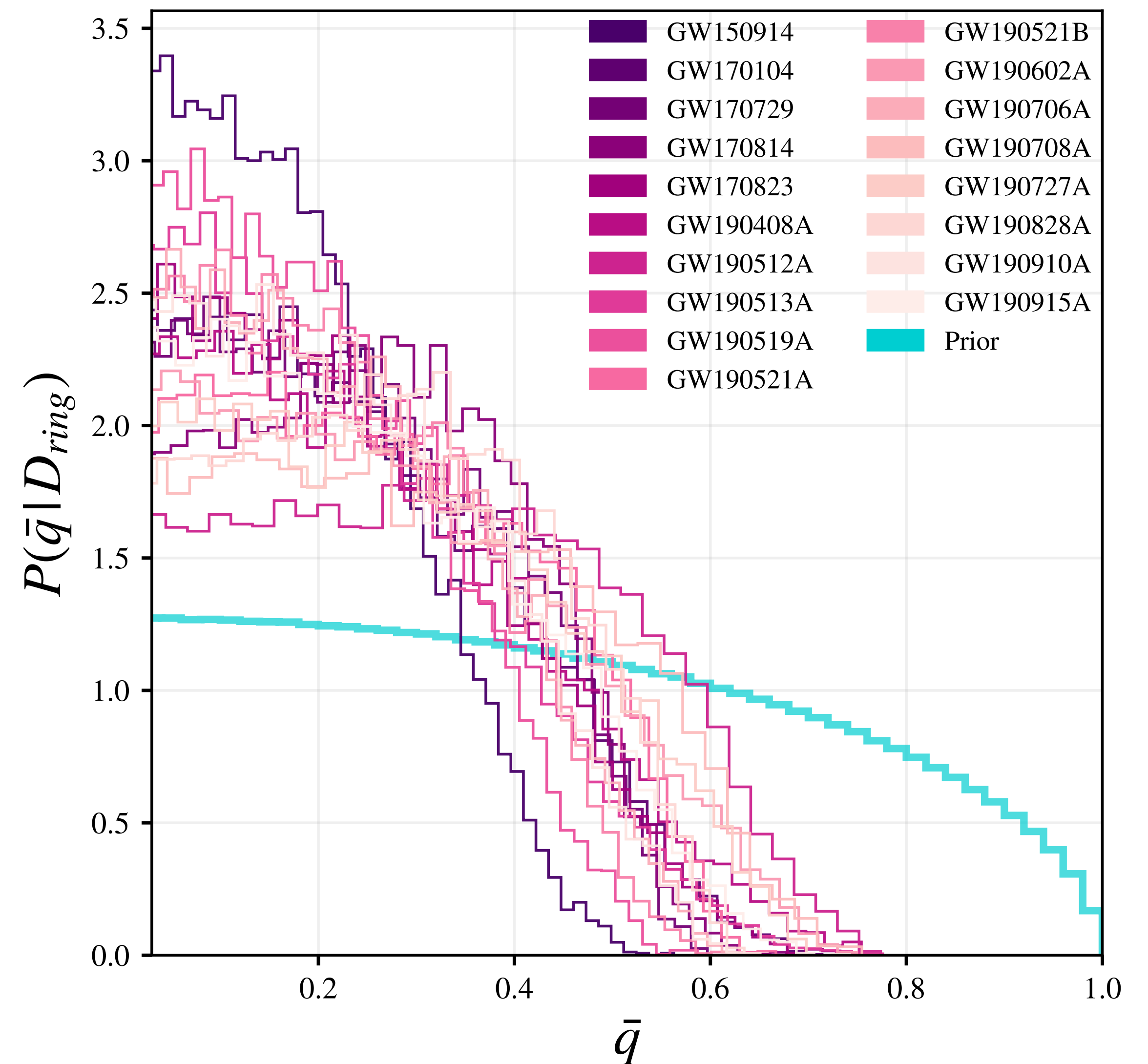
- Application to **charged BHs**: the **Kerr-Newman (KN)** case.
- Kerr spectrum deviations known for arbitrary spin: valuable **test-bed** for **beyond-GR** effects.
- Non-standard scenarios: minicharged **dark matter**, **magnetic monopoles**, scalar-tensor-vector gravity, ...

Carullo, Del Pozzo, Dias, Godazgar, Johnson-McDaniel, Laghi, Santos, Veitch (In prep.)



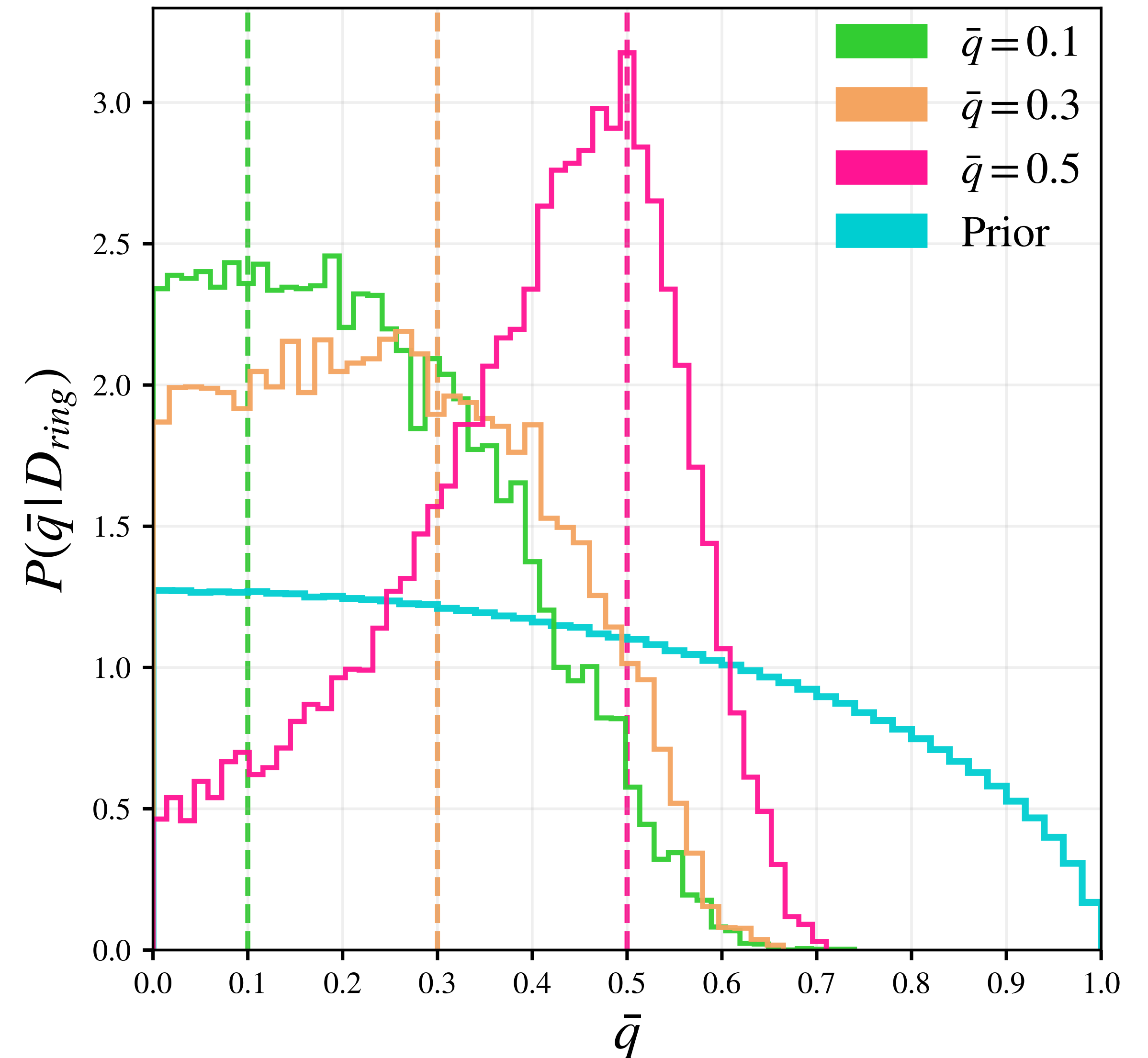
KERR-NEWMAN CONSTRAINTS

- “Standard” parameter estimation **uninformative**, due to **strong correlation** between spin and charge.
- **Null** test: maximum amount of charge compatible with current observations
- Best event (GW150914) gives:
 $\bar{q} < 0.33$
- **No evidence** for/against the presence of charge from Bayes’ Factors



KERR-NEWMAN FUTURE CONSTRAINTS

- Can future observations from current detector network **discriminate** the presence of a **charge**?
- Simulate KN signals in LIGO-Virgo data at design sensitivity
- Recover using KN templates
- Charge confidently measured **only** for **high values**
- Need more info to break **spin-charge correlations**



CONCLUSIONS AND PROSPECTS

- **Black hole perturbations** have unquestionably transitioned from a mathematical problem to an **observational reality**.
- The analysis of **gravitational** black holes **spectra** is a powerful tool to test our current **gravity paradigm** and search for signs of **new physics**.
- LIGO-Virgo ringdown observations can already probe high-curvature **unexplored regimes** of beyond-GR theories or place **competitive bounds** on beyond-GR extensions.
- Future detections promise to quickly overcome other experimental bounds.

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Credits to: Jani, Ghonge

