

# Update and progress with B-Flavour Anomalies

Joaquim Matias    Universitat Autònoma de Barcelona



**Universitat Autònoma  
de Barcelona**



# Goal of this talk

Messages to take home of this talk:

For the first time we see **Coherence** on a large set of **deviations/anomalies**

Nature seems to point **towards**  
first signals of **violation of lepton flavour universality**

...SM predicts LFU: interactions between gauge bosons and leptons  
being the same for different lepton families.

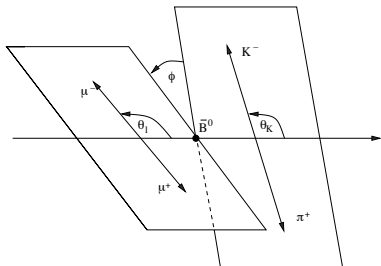
... soon we will have more observables to confirm it.

**Not** my goal HERE to focus on a specific UV completion  
...but to **SHOW** that there is a **SIGNAL**.

# The path to the anomalies

# The starting point: Angular distribution of $B \rightarrow K^*(\rightarrow K\pi)\mu\mu$

4-body angular distribution  $\mathbf{B}_d \rightarrow \mathbf{K}^{*0}(\rightarrow \mathbf{K}^-\pi^+)\mathbf{l}^+\mathbf{l}^-$  with three angles, invariant mass of lepton-pair  $q^2$ .



$\theta_\ell$ : Angle of emission between  $\bar{K}^{*0}$  and  $\mu^-$  in di-lepton rest frame.

$\theta_K$ : Angle of emission between  $\bar{K}^{*0}$  and  $K^-$  in di-meson rest frame.

$\phi$ : Angle between the two planes.

$q^2$ : dilepton invariant mass square.

large  $K^*$ -recoil/low- $q^2$ :  $E_{K^*} \gg \Lambda_{QCD}$  or  $4m_\ell^2 \leq q^2 < 9 \text{ GeV}^2$ :

low  $K^*$ -recoil/large- $q^2$ :  $E_{K^*} \sim \Lambda_{QCD}$  or  $14 < q^2 \leq (m_B - m_{K^*})^2$

$$\frac{d^4\Gamma(\bar{B}_d)}{dq^2 d\cos\theta_\ell d\cos\theta_K d\phi} = \frac{9}{32\pi} \sum_i J_i(q^2) f_i(\theta_\ell, \theta_K, \phi)$$

$J_i(q^2)$  function of transversity (helicity) amplitudes of  $K^*$ :  $A_{\perp,\parallel,0}^{L,R}$  but also  $A_t, A_s$

$$A_{\perp,\parallel,0}^{L,R} \rightarrow C_i \text{ (short)} \times \text{Hadronic quantities (long)}$$

The amplitude of  $B \rightarrow K^* \mu^+ \mu^-$

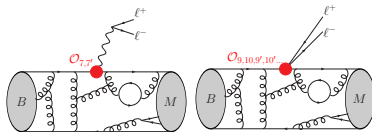
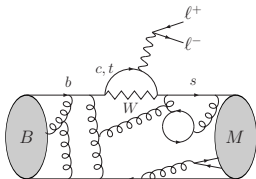
# The framework: $b \rightarrow s \ell \ell$ effective Hamiltonian, **Wilson Coefficients**

$$b \rightarrow s \gamma^{(*)} : \mathcal{H}_{\Delta F=1}^{SM} \propto \sum V_{ts}^* V_{tb} \mathcal{C}_i \mathcal{O}_i + \dots$$

separate short and long distances ( $\mu_b = m_b$ )

- ▶  $\mathcal{O}_7 = \frac{e}{16\pi^2} m_b (\bar{s} \sigma_{\mu\nu} P_R b) F^{\mu\nu}$
- ▶  $\mathcal{O}_9 = \frac{e^2}{16\pi^2} (\bar{s} \gamma_\mu P_L b) (\bar{\ell} \gamma^\mu \ell)$
- ▶  $\mathcal{O}_{10} = \frac{e^2}{16\pi^2} (\bar{s} \gamma_\mu P_L b) (\bar{\ell} \gamma^\mu \gamma_5 \ell)$

$$\mathcal{C}_7^{SM} = -0.29, \mathcal{C}_9^{SM} = 4.1, \mathcal{C}_{10}^{SM} = -4.3$$



NP changes short-distance  $\mathcal{C}_i = \mathcal{C}_i^{SM} + \mathcal{C}_i^{NP}$  for SM or involve additional operators

- ▶ Chirally flipped ( $W \rightarrow W_R$ )
- ▶ (Pseudo)scalar ( $W \rightarrow H^+$ )
- ▶ Tensor operators ( $\gamma \rightarrow T$ )

$$\mathcal{O}_{7'} \propto (\bar{s} \sigma^{\mu\nu} P_L b) F_{\mu\nu}, \mathcal{O}_{9'} \propto (\bar{s} \gamma_\mu P_R b) (\bar{\ell} \gamma^\mu \ell) \dots$$

$$\mathcal{O}_S \propto (\bar{s} P_R b) (\bar{\ell} \ell), \mathcal{O}_P \propto (\bar{s} P_R b) (\bar{\ell} \gamma_5 \ell)$$

$$\mathcal{O}_T \propto \bar{s} \sigma_{\mu\nu} (1 - \gamma_5) b \bar{\ell} \sigma_{\mu\nu} \ell$$

# Diagnosis of $b \rightarrow s \mu^+ \mu^-$ Anomalies

# $b \rightarrow s \mu^+ \mu^-$ anomalies: $P'_5$

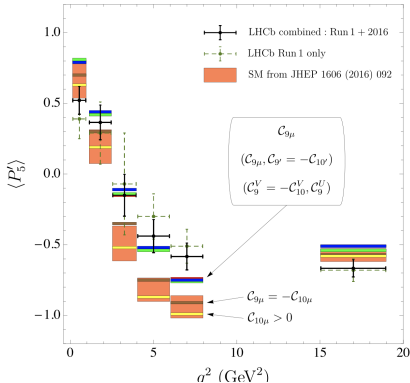
LHCb, Belle, ATLAS measurements deviate from Standard model (SM) predictions:

- Angular observable  $P'_5$  in  $B \rightarrow K^* \mu^+ \mu^-$  (two anomaly bins  $\sim 3 \sigma$  each)

LHCb, arXiv:2003.04831, arXiv:2012.13241

- **Exact** cancellation of soft FF at LO: optimized observable.
- Most tested anomaly, now including charged channel:  $B^+ \rightarrow K^{*+} \mu^+ \mu^-$ .
- Latest LHCb update increased significantly the coherence w.r.t. other observables.

Eur.Phys.J.C 80 (2020) 6, 511 (addendum)



All  $P_i$ 's are constructed to cancel exactly at LO the dependence on SFF:  $7 \text{ FFs } (V, A_i, T_i) \rightarrow \xi_{\perp, \parallel}$  (SFF)

JHEP 04 (2012) 104, JHEP 01 (2013) 048

$$P'_5 = \frac{J_5}{2\sqrt{-J_{2s}J_{2c}}} = \sqrt{2} \frac{\text{Re}[A_0^L A_{\perp}^{L*} - A_0^R A_{\perp}^{R*}]}{\sqrt{|A_0|^2(|A_{\perp}|^2 + |A_{\parallel}|^2)}}$$

It enters the 4-body distribution:

$$\frac{1}{\Gamma'_{full}} \frac{d^4 \Gamma_P}{dq^2 d\Omega} = \frac{9}{32\pi} \left[ \frac{3}{4} \mathbf{F}_T \sin^2 \theta_K + \mathbf{F}_L \cos^2 \theta_K + \dots \right. \\ \left. + \sqrt{\mathbf{F}_T \mathbf{F}_L} P'_5 \sin 2\theta_K \sin \theta_l \cos \phi + \dots \right]$$



# $b \rightarrow s \mu^+ \mu^-$ anomalies

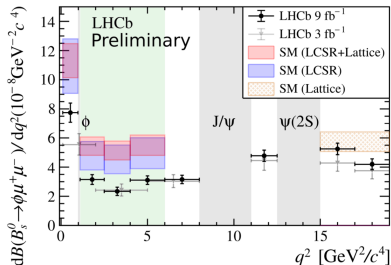
Several other LHCb measurements deviate from Standard model (SM) predictions:

- Branching ratios of  $B \rightarrow K \mu^+ \mu^-$ ,  $B \rightarrow K^* \mu^+ \mu^-$ , and  $B_s \rightarrow \phi \mu^+ \mu^-$  ( $\sim 2 \sigma$ ).

LHCb, arXiv:1403.8044, arXiv:1506.08777, arXiv:1606.04731

BRs like  $S_i$  observables differently from  $P_i$  are very sensitive to the choice and treatment of FFs.

[LHCb-PAPER-2021-014, in preparation]



Bin[1.1,6.0]:

$$\frac{dB(B_s^0 \rightarrow \phi \mu^+ \mu^-)}{dq^2} = (2.88 \pm 0.21) \times 10^{-8} \frac{\text{GeV}^2}{c^4}$$

Tension with SM at  $1.8\sigma$  (LCSR-Zwicky et al.) and  $3.6\sigma$  (LCSR+Lattice)

→ **systematic deficit in muons in all measured channels**

## Hints for LFU violation in $b \rightarrow s \ell^+ \ell^-$ decays

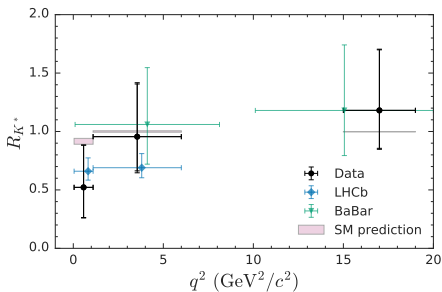
Measurements of lepton flavour universality (LFU) ratios  $R_{K^*}^{[0.045, 1.1]}$ ,  $R_{K^*}^{[1.1, 6]}$  show deviations from SM by about  $2.5\sigma$  each.

LHCb, arXiv:1705.05802

Belle, arXiv:1904.02440

- Cancellation of all uncertainties in SM (up to lepton masses) but strongly FF sensitive in presence of NP.

$$R_{K^*} = \frac{BR(B \rightarrow K^* \mu^+ \mu^-)}{BR(B \rightarrow K^* e^+ e^-)}$$



# Hints for LFU violation in $b \rightarrow s \ell^+ \ell^-$ decays

Measurement of LFU ratio  $R_K^{[1.1,6]}$  shows deviation from SM by  $3.1\sigma$ .

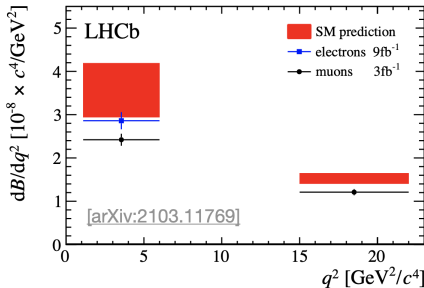
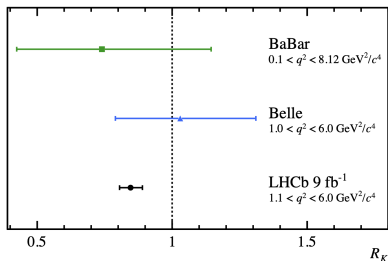
LHCb, arXiv: 2103.11769, Belle, arXiv:1908.01848

- Cancellation of all uncertainties in SM and in presence of NP (up to  $m_\ell$ ).

$$R_K = \frac{BR(B \rightarrow K \mu^+ \mu^-)}{BR(B \rightarrow K e^+ e^-)} : \text{Experimental value } R_K^{\text{LHCb}} = 0.846^{+0.042+0.013}_{-0.039-0.012}$$

$$\int_{q^2=1.1 \text{ GeV}^2}^{q^2=6 \text{ GeV}^2} \frac{d\mathcal{B}(B^+ \rightarrow K^+ e^+ e^-)}{dq^2} dq^2 = (28.6^{+1.5}_{-1.4} \text{ (stat.)} \pm 1.3 \text{ (syst.)}) \times 10^{-9}$$

... Electrons seem more SM-like than muons.



# Hints for LFU violation in $b \rightarrow s \ell^+ \ell^-$ decays

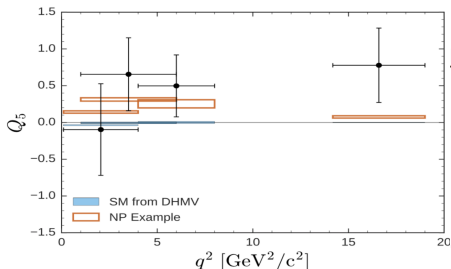
Measurement of LFU observable  $Q_{4,5} = P'_{4,5}{}^{\mu} - P'_{4,5}{}^e$  **by Belle.**

S. Wehle et al (Belle), PRL 118 (2017)

- Cancellation of all uncertainties in SM (up to lepton masses) like other LFUV  $R_{K,K^*}$ , **and** optimized in presence of NP, contrary to the case of  $R_{K^*}$ .
- Isospin averaged but lepton-flavour dependent channels:

$$P_i^{\prime\ell} = \sigma_+ P_i^{\prime\ell}(B^+) + (1 - \sigma_+) P_i^{\prime\ell}(\bar{B}^0) \quad \sigma_+ = 0.5 \pm 0.5$$

- Also electronic and muonic channel analysis, show electrons more SM-like.



$q^2$ in $\text{GeV}^2/c^2$	$Q_4$	$Q_5$
[1.00, 6.00]	$0.498 \pm 0.527 \pm 0.166$	$0.656 \pm 0.485 \pm 0.103$
[0.10, 4.00]	$-0.723 \pm 0.676 \pm 0.163$	$-0.097 \pm 0.601 \pm 0.164$
[4.00, 8.00]	$0.448 \pm 0.392 \pm 0.076$	$0.498 \pm 0.410 \pm 0.095$
[14.18, 19.00]	$0.041 \pm 0.565 \pm 0.082$	$0.778 \pm 0.502 \pm 0.065$

# Combination of $B_{s,d} \rightarrow \mu^+ \mu^-$ measurements

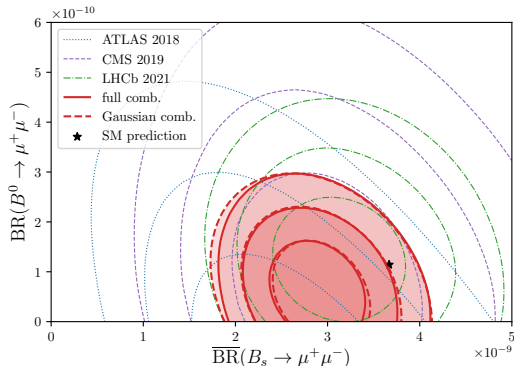
Measurements of  $\text{BR}(B_{s,d} \rightarrow \mu^+ \mu^-)$  by LHCb, CMS, and ATLAS show combined deviation from SM by about  $2\sigma$ .

ATLAS, arXiv:1812.03017

CMS, arXiv:1910.12127

LHCb seminar 23 March 2021

Altmannshofer, PS, arXiv:2103.13370



We take the average of ATLAS, CMS, LHCb (now closer to SM)

$$\mathcal{B}_{B_s \rightarrow \mu^+ \mu^-} = (2.85^{+0.34}_{-0.31}) \times 10^{-9} \quad [\text{Diego Martinez, private communication}]$$

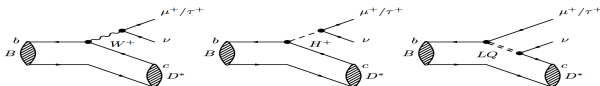
# Hints for LFU violation in $b \rightarrow c \ell \nu$ decays

Measurements of LFU ratios  $R_D$  and  $R_{D^*}$  by BaBar, Belle, and LHCb show combined deviation from SM by about  $3\sigma$ .

BaBar, arXiv:1205.5442, arXiv:1303.0571

LHCb, arXiv:1506.08614, arXiv:1708.08856

Belle, arXiv:1507.03233, arXiv:1607.07923, arXiv:1612.00529, arXiv:1904.08794

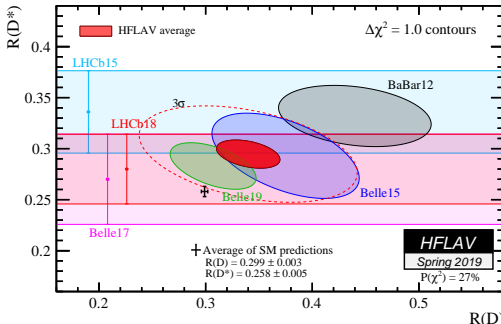


SM

NP

$$R_{D^{(*)}} = \frac{BR(B \rightarrow D^{(*)} \tau \nu)}{BR(B \rightarrow D^{(*)} \ell \nu)}$$

$$\ell \in \{e, \mu\}$$

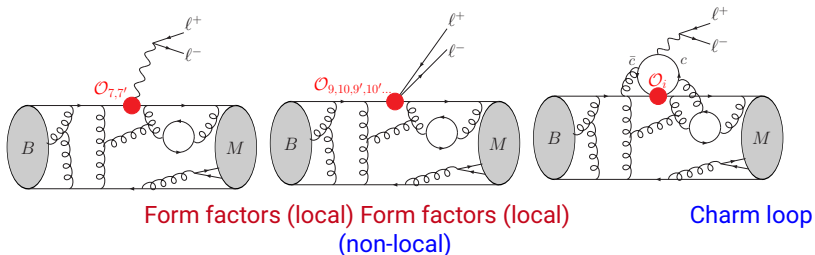


HFLAV, [hflav.web.cern.ch](http://hflav.web.cern.ch)

# Hadronic Uncertainties for exclusive $b \rightarrow s \ell \ell$ decays

# Two sources of hadronic uncertainties

$$A(B \rightarrow M \ell \ell) = \frac{G_F \alpha}{\sqrt{2} \pi} V_{tb} V_{ts}^* [(A_\mu + T_\mu) \bar{u}_\ell \gamma^\mu v_\ell + B_\mu \bar{u}_\ell \gamma^\mu \gamma_5 v_\ell]$$



- Local contributions (more terms if NP in non-SM  $C_i$ ): **form factors**

$$A_\mu = -\frac{2m_b q^\nu}{q^2} C_7 \langle M | \bar{s} \sigma_{\mu\nu} P_R b | B \rangle + C_9 \langle M | \bar{s} \gamma_\mu P_L b | B \rangle$$

$$B_\mu = C_{10} \langle M | \bar{s} \gamma_\mu P_L b | B \rangle$$

- Non-local contributions (charm loops): **hadronic contribs.**

$T_\mu$  contributes like  $\mathcal{O}_{7,9}$ , but depends on  $q^2$  and external states



# Hadronic uncertainties: form factors

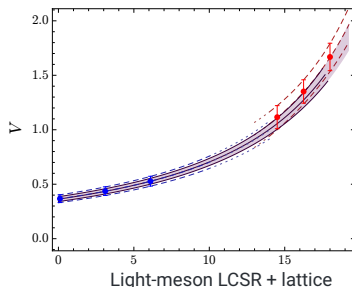
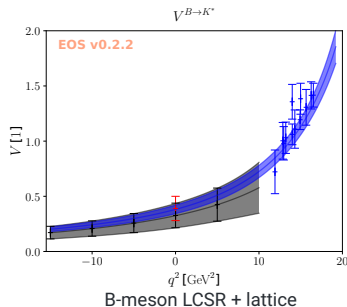
3 form factors for  $K$ , 7 form factors for  $K^*$  and  $\phi$

- ▶ low recoil: **lattice QCD**

[Horgan, Liu, Meinel, Wingate; HPQCD collab]

- ▶ large recoil: **Light-Cone Sum Rules** (B-meson or light-meson DAs)

[Khodjamirian, Mannel, Pivovarov, Wang; Bharucha, Straub, Zwicky; Gubernari, Kokulu, van Dyk]



- ▶ correlations among the form factors needed

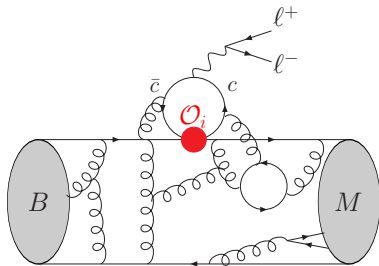
- ▶ recovered from EFT with  $m_b \rightarrow \infty + O(\alpha_s) + O(1/m_b)$

[Capdevila, SDG, Hofer, Matias; Straub, Altmannshoffer; Hurth, Mahmoudi]

- ▶ optimised observables  $P_i$  to reduce the impact of form factor uncertainties

# Hadronic uncertainties: charm loops

- ▶ important for resonance regions (charmonia)
- ▶ SM effect contributing to  $\mathcal{C}_{9\ell}$
- ▶ depends on  $q^2$ , lepton univ.



# Hadronic uncertainties: charm loops

- ▶ important for resonance regions (charmonia)
- ▶ SM effect contributing to  $\mathcal{C}_{9\ell}$
- ▶ depends on  $q^2$ , lepton univ.

Several approaches agree at low- $q^2$

- ▶ LCSR explicit estimates (LO+NLO)

[Khodjamirian, Mannel, Pivovarov, Wang; Gubenari, Van Dyk]

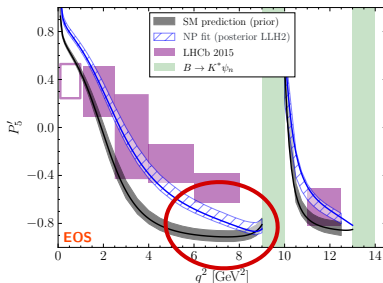
- ▶ We include to LCSR computation a nuisance parameter  $s_i$  to allow for constructive/destructive interference between charm and short-distance for each amplitude widening the uncertainties

[Crivellin, Capdevila, SDG, Hofer, Matias; Straub, Altmannshoffer, Hurth, Mahmoudi]

- ▶ fit of sum of resonances to the data
- ▶ dispersive representation +  $J/\psi, \psi(2S)$  data

[Blake, Egede, Owen, Pomery, Petridis]

[Bobeth, Chrzaszcz, van Dyk, Virto]



Is charm-loop **overestimated** instead of **underestimated**?

# The global $b \rightarrow s\ell\ell$ analysis



*To focus just on one single anomaly ( $R_K$  or  $R_{K^*}$ ) at the very beginning of the analysis make you lose the general view of the forest of anomalies... and may probably lead you to the wrong conclusions....*

# Setup

- Likelihood taking into account experimental and theoretical uncertainties and correlations in Gaussian approximation

[ Algueró, Capdevila, Crivellin, SDG, Masjuan, Matias, Novoa-Brunet, Vito]

$$\text{We fit } C_i = C_i^{\text{SM}} + C_i^{\text{NP}}$$

Two statistical quantities of interest to assess a NP scenario/hypothesis:

- $p$ -value of a given hypothesis:  $\chi_{\min}^2$  considering  $N_{\text{dof}}$  (in %)  
**goodness of fit:** does the hypothesis give an overall good fit ?  
and if not, can we exclude it ?
- $\text{Pull}_{\text{SM}} : \chi^2(C_i = 0) - \chi_{\min}^2$  considering  $N_{\text{dof}}$  (in  $\sigma$  units)  
**metrology:** how well does the hypothesis solve SM deviations ?

# Experimental inputs

- ▶ LFUV:  $R_K, R_{K^*}$  and  $Q_{4,5} = P_{4,5}'^\mu - P_{4,5}'^e$  isospin average\* (large- low-recoil bins)
- ▶  $B \rightarrow K^* \mu \mu$  (Br and ang obs)
- ▶  $B_s \rightarrow \phi \mu \mu$  (Br and ang obs)
- ▶  $B^+ \rightarrow K^+ \mu \mu, B^0 \rightarrow K^0 \mu \mu$  (Br and ang obs)
- ▶  $B \rightarrow X_s \mu \mu, B_s \rightarrow \mu \mu$  (Br, effective  $B_s \rightarrow \mu \mu$  lifetime  $\tau_{\text{eff}}$ )
- ▶  $B \rightarrow K^* e e$  (ang obs)
- ▶  $B \rightarrow X_s \gamma, B_s \rightarrow \phi \gamma, B \rightarrow K^* \gamma$  (Br)

including LHCb, ATLAS, CMS, Babar and Belle data whenever available

**Total:** 246 obs (Global) of which LFUV ( $R_K, R_{K^*}, Q_{4,5}$ ) from LHCb, Belle, ATLAS, CMS

\* It is important not to miss any LFUV observable (like  $Q_i$  observables) for a complete analysis.

# Updates

- **Update:** Experimental value  $R_K^{\text{LHCb}} = 0.846_{-0.039-0.012}^{+0.042+0.013}$  [LHCb 2103.11769]
- **Update:** Exp value  $BR(B_s \rightarrow \mu\mu) = (3.09_{-0.43-0.11}^{+0.46+0.15}) \times 10^{-9}$  [LHCb at LHC Seminar]
- **Update:** Experimental value  $R_K^{\text{Belle}}$  [Belle 1908.01848]
- **New:** Optimised angular distribution  $B^+ \rightarrow K^{*+} \mu\mu$  [LHCb 2012.13241]
- **Update:** Angular analysis at low  $B^0 \rightarrow K^{*0} ee$  [LHCb 2010.06011]
- **New:** Angular analysis  $B^+ \rightarrow K^+ \mu\mu (F_H, A_{FB})$  [CMS 1806.00636]
- **New:** Angular analysis  $B^+ \rightarrow K^{*+} \mu\mu (F_L, A_{FB})$  [CMS 2010.13968]
- **New:**  $BR(B^{0,+} \rightarrow K^{0,+} \mu\mu)$  partners to  $R_K^{\text{Belle}}$  [Belle 1908.01848]



# Theoretical inputs

- ▶ **Form factors:** B-meson DA LCSR + lattice + EFT for correlations
- ▶ **Charm-loop corrections:** Perturbative contribution + magnitude of long-distance contrib inspired by [Khodjamirian, Mannel, Pivovarov, Wang]
- ▶ **Quark-duality violation at high  $q^2$ :** conservative 10% effect at the level of the amplitude  
(explicit estimates [Feldman, Buchalla] at the level of 2%)
- ▶  $Br(B_s \rightarrow \mu\mu)$  modified to include latest corrections from [Misiak ; Beneke, Bobeth, Szafron]
- ▶  $Br(B^+ \rightarrow K^{*+}\ell\ell)$  and  $P_i^+$  include mass and lifetime differences, annihilation graphs, hard spectator interactions with  $\mathcal{O}_8$  and  $\mathcal{O}_{1-6}$

# Results and Outlook

# 1D Scenarios for $\mathcal{C}_{i\mu}$ [2021]

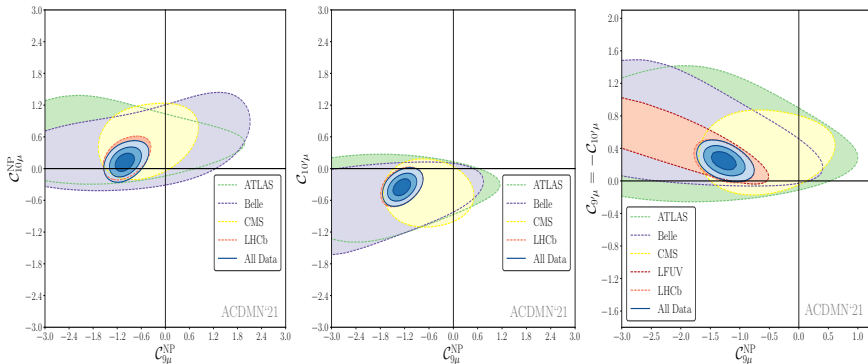
Updated results in: M. Algueró et al. arXiv: 2104.08921

1D Hyp.	Best fit	All			LFUV	
		$1\sigma$	$\text{Pull}_{\text{SM}}$	p-value	$1\sigma$	$\text{Pull}_{\text{SM}}$
$\mathcal{C}_{9\mu}^{\text{NP}}$	-1.06	$[-1.20, -0.91]$	<b>7.0</b>	39.5 %	$[-1.06, -0.60]$	4.0
$\mathcal{C}_{9\mu}^{\text{NP}} = -\mathcal{C}_{10\mu}^{\text{NP}}$	-0.44	$[-0.52, -0.37]$	<b>6.2</b>	22.8 %	$[-0.46, -0.29]$	4.6
$\mathcal{C}_{9\mu}^{\text{NP}} = -\mathcal{C}_{9'\mu}$	-1.11	$[-1.25, -0.96]$	6.5	28.0 %	$[-2.13, -0.96]$	3.0
$\mathcal{C}_{9\mu}^{\text{NP}} = -3\mathcal{C}_{9e}$	-0.89	$[-1.03, -0.75]$	6.7	32.2 %	$[-0.78, -0.44]$	4.0

- ▶ LFUV fit:  $R_K, R_{K^*}, \mathbf{Q}_{4,5}$  (updated isospin average),  $B_s \rightarrow \mu\mu, b \rightarrow s\gamma$
- ▶ All : all  $b \rightarrow s\ell\ell$  and  $b \rightarrow s\gamma$  observables
- ▶  $\text{Pull}_{\text{SM}}$  in  $\sigma$  units increased compare to [2020], scenario  $\mathcal{C}_{10\mu}^{\text{NP}}$  still marginal.  
Time-ev. of  $\text{Pull}_{\text{SM}}(\mathcal{C}_{9\mu}^{\text{NP}})$ : 4.5 [2016], 5.8 [2018], 5.6 [2019], 6.3 [2020], 7.0 [2021].
- ▶ p-value of SM hyp from 11% (2019) to 1.4% (2020) to **1.1%** (2021) for the fit "All"  
12.6% (2020) to **1.4%** (2021) for the fit "LFUV"
- ▶ Tension between All fit preference by  $\mathcal{C}_{9\mu}^{\text{NP}}$  and LFUV-fit by  $\mathcal{C}_{9\mu}^{\text{NP}} = -\mathcal{C}_{10\mu}^{\text{NP}}$ .

Same hierarchy of main scenarios was found by other groups, for instance: Hurth, Mahmoudi, Neshatpour, arXiv:2012.12207

## 2D Scenarios for $C_{i\mu}$ [2021]: Hints for RHC?



- Now  $C_{10\mu}^{\text{NP}}$  compatible with zero at  $1\sigma$  in  $(C_{9\mu}^{\text{NP}}, C_{10\mu}^{\text{NP}})$  due to  $B_s \rightarrow \mu^+ \mu^-$ .
- RHCs appear quite naturally: large increase in scenario  $(C_{9\mu}^{\text{NP}}, C_{10\mu}^{\text{NP}})$  and Hyp. V ( $[C_{9\mu}, C_{9'\mu} = -C_{10'\mu}]$ ) due to  $R_K$  at level of  $3\sigma$  w.r.t. RHCs.

## 2D and 6D Scenarios for $\mathcal{C}_{i\mu}$ [2021]

2D Hyp.	All			LFUV		
	Best fit	Pull <sub>SM</sub>	p-value	Best fit	Pull <sub>SM</sub>	p-value
$(\mathcal{C}_{9\mu}^{\text{NP}}, \mathcal{C}_{10\mu}^{\text{NP}})$	(-1.00,+0.11)	6.8	39.4 %	(-0.12,+0.54)	4.3	65.6 %
$(\mathcal{C}_{9\mu}^{\text{NP}}, \mathcal{C}_{9'\mu})$	(-1.22,+0.56)	7.2	49.8 %	(-1.80,+1.12)	4.1	53.6 %
$(\mathcal{C}_{9\mu}^{\text{NP}}, \mathcal{C}_{10'\mu})$	(-1.26,-0.35)	<b>7.4</b>	55.9 %	(-1.82,-0.59)	4.7	84.1 %
$(\mathcal{C}_{9\mu}^{\text{NP}}, \mathcal{C}_{9'\mu} = -\mathcal{C}_{10'\mu})$	(-1.26,+0.25)	<b>7.4</b>	55.8 %	(-2.08,+0.51)	4.7	86.0 %
$(\mathcal{C}_{9\mu}^{\text{NP}} = -\mathcal{C}_{10\mu}^{\text{NP}}, \mathcal{C}_{9'\mu} = -\mathcal{C}_{10'\mu})$	(-0.48,+0.11)	<b>6.0</b>	24.0 %	(-0.46,+0.15)	4.5	74.5 %

- No change in the hierarchy of scenarios w.r.t. 2020.
- From last two rows: Vector preference in left sector ( $\mathcal{C}_{9\mu}^{\text{NP}}$ ) (vs  $\mathcal{C}_{9\mu}^{\text{NP}} = -\mathcal{C}_{10\mu}^{\text{NP}}$ ) and  $\mathcal{C}_{9'\mu} = -\mathcal{C}_{10'\mu}$  preference in right sector.

	$\mathcal{C}_7^{\text{NP}}$	$\mathcal{C}_{9\mu}^{\text{NP}}$	$\mathcal{C}_{10\mu}^{\text{NP}}$	$\mathcal{C}_{7'}$	$\mathcal{C}_{9'\mu}$	$\mathcal{C}_{10'\mu}$
Bfp	+0.01	-1.21	+0.15	+0.01	+0.37	-0.21
1 $\sigma$	[-0.02, +0.04]	[-1.38, -1.01]	[+0.00, +0.34]	[-0.02, +0.03]	[-0.12, +0.80]	[-0.42, +0.02]
2 $\sigma$	[-0.04, +0.06]	[-1.52, -0.83]	[-0.11, +0.49]	[-0.03, +0.05]	[-0.51, +1.12]	[-0.60, +0.23]

- Pull<sub>SM</sub>:  $5.1\sigma$  [2019]  $\rightarrow$   $5.8\sigma$  [2020]  $\rightarrow$   $6.6\sigma$  [2021] (49.9%)
- 6D Fit shows coherence and stability with time.

# Solution of the tension between All fit and LFUV fit: LFU New Physics

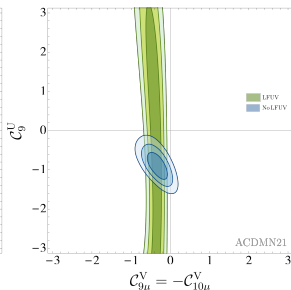
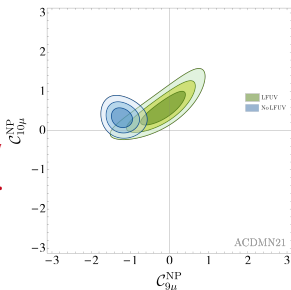
In [Algueró, Capdevila, Descotes-Genon, Masjuan, JM, PRD'19, 1809.08447] it was proposed:  
... to remove hypothesis that NP is purely LFUV

$$\begin{aligned} C_{ie}^{\text{NP}} &= C_i^{\text{U}} \\ C_{i\mu}^{\text{NP}} &= C_{i\mu}^{\text{V}} + C_i^{\text{U}} \end{aligned}$$

- ▶ Common New Physics contribution  $C_i^{\text{U}}$  to charged leptons.
- ▶ Allow to accommodate that LFUV-NP prefers  $SU(2)_L$  and LFU-NP is vectorial.

$[C_{9\mu}, C_{10\mu}]$

**TENSION**  
between LFUV  
and non-LFUV.  
**Pull<sub>SM</sub> = 6.8σ.**



$$[C_{9\mu}^{\text{V}} = -C_{10\mu}^{\text{V}}, C_{9\mu}^{\text{U}}]$$

**PERFECT**  
agreement and  
higher Pull<sub>SM</sub>  
significance of  
**7.3σ.**

(see more LFU scenarios in back-up)

# Solution of the tension between All fit and LFUV fit: LFU New Physics

In [Algueró, Capdevila, Descotes-Genon, Masjuan, JM, PRD'19, 1809.08447] it was proposed:  
... to remove hypothesis that NP is purely LFUV

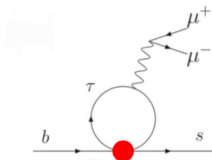
$$\begin{aligned}C_{ie}^{\text{NP}} &= C_i^{\text{U}} \\C_{i\mu}^{\text{NP}} &= C_{i\mu}^{\text{V}} + C_i^{\text{U}}\end{aligned}$$

- ▶ Common New Physics contribution  $C_i^{\text{U}}$  to charged leptons.
- ▶ LFU naturally generated by  $\tau$ -loop linking it to future  $b \rightarrow s\tau\tau$  and  $R_{D,D^*}$  anomalies (discussed later)

[Capdevila, Crivellin, Descotes-Genon, Hofer, Matias, PRL'18, arxiv 1712.01919]

[Crivellin, Greub, Muller, Saturnino, PRL'19, arxiv 1807.02068]

[Algueró et al. EPJC79 (2019) 8,714.]



**Assuming a generic flavour structure and NP at the scale  $\Lambda$ :**

\* Notice that  $C_9^{\text{U}}$  should not be confused with the  $q^2$ – dependent, amplitude and process dependent charm-loop.

# An EFT interpretation: SMEFT

Connect  $b \rightarrow s\ell\ell$  and  $b \rightarrow c\ell\nu$  anomalies within SMEFT ( $\Lambda_{NP} \gg m_{t,W,Z}$ )

$$\mathcal{L}_{SMEFT} = \mathcal{L}_{SM} + \mathcal{L}_{d>4}$$

with higher-dim ops involving only SM fields

[Grzadkowski, Iskrzynski, Misiak, Rosiek ; Alonso, Grinstein, Camalich]

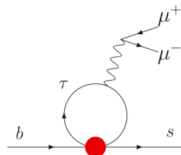
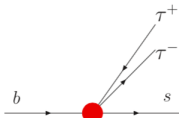
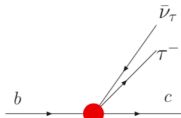
- Two ops. with left-handed doublets

$$\mathcal{O}_{ijkl}^{(1)} = [\bar{Q}_i \gamma_\mu Q_j] [\bar{L}_k \gamma^\mu L_l] \quad \mathcal{O}_{ijkl}^{(3)} = [\bar{Q}_i \gamma_\mu \vec{\sigma} Q_j] [\bar{L}_k \gamma^\mu \vec{\sigma} L_l]$$

- FCCC part of  $\mathcal{O}_{2333}^{(3)}$  can describe  $R_{D^{(*)}}$  (rescaling of  $G_F$  for  $b \rightarrow c\tau\nu$ )

- FCNC part of  $\mathcal{O}_{2333}^{(1,3)}$  with  $C_{2333}^{(1)} = C_{2333}^{(3)}$  [Capdevila, Crivellin, SDG, Hofer, Matias]

- Large NP contribution  $b \rightarrow s\tau\tau$  through  $C_{9\tau}^V = -C_{10\tau}^V$
- Avoids bounds from  $B \rightarrow K^{(*)}\nu\nu, Z$  decays, direct production in  $\tau\tau$
- Through radiative effects, (small) NP contribution to  $C_9^U$



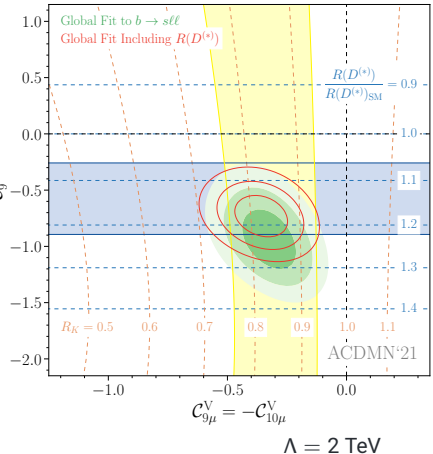


# An EFT interpretation $B$ anomalies in Scenario 8: $\mathcal{C}_9^V = -\mathcal{C}_{10}^V, \mathcal{C}_9^U$

- $\mathcal{C}_{9\mu}^V = -\mathcal{C}_{10\mu}^V$  from small  $\mathcal{O}_{2322} [b \rightarrow s\mu\mu]$
- $\mathcal{C}_9^U$  from radiative corr from large  $\mathcal{O}_{2333} [b \rightarrow c\tau\nu \text{ and } b \rightarrow s\mu\mu]$
- Agreement with  $(R_D, R_{D^*})$  for  $\Lambda = 1 - 10 \text{ TeV}$
- Scenario 8 has  $\text{Pull}_{\text{SM}}$  of  $8.1 \sigma$  once  $R_{D^*}$  included. **Global fit  $b \rightarrow s\ell\ell$  would prefer slightly higher tension in  $R_{D^{(*)}}$  or large  $\Lambda$  scale**
- Huge enhancement of  $b \rightarrow s\tau\tau$  modes  $\mathcal{O}(10^{-4})$  [Capdevila, Crivellin, SDG, Hofer, Matias]

$$\text{Br}(B_s \rightarrow \tau^+ \tau^-)_{\text{LHCb}} \leq 6.8 \times 10^{-3},$$

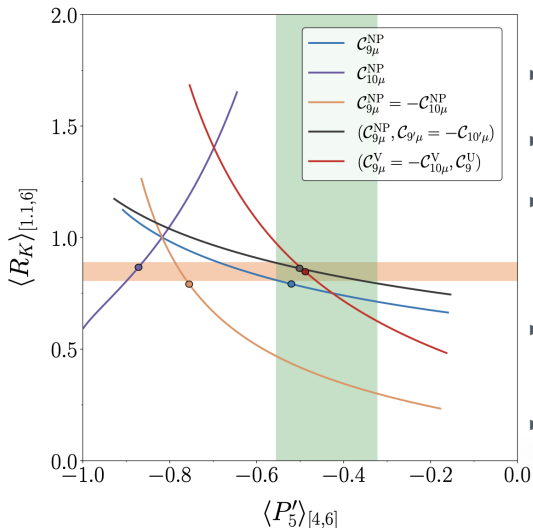
$$\text{Br}(B \rightarrow K\tau^+ \tau^-)_{\text{Babbar}} \leq 2.25 \times 10^{-3}$$



## Scenario 8 LFU fits & $R(D^{(*)})/R(D^{(*)})_{\text{SM}}$

Scenario	Best fit	$1\sigma$	$\text{Pull}_{\text{SM}} (\sigma)$	p-value (%)
$(\mathcal{C}_{9\mu}^V = -\mathcal{C}_{10\mu}^V, \mathcal{C}_9^U)$	$(-0.36, -0.74)$	$([-0.43, -0.28], [-0.86, -0.61])$	8.1	51.4

# Consistency of scenarios with $B \rightarrow K^* \mu \mu$ : $\langle P'_5 \rangle_{[4,6]}$ vs $\langle R_K \rangle_{[1.1,6]}$

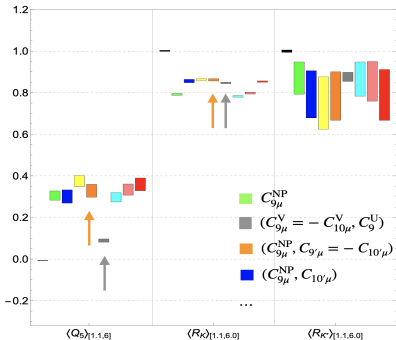


- Bfeps not significantly changed in 2021.
- Increase of significance for some scenarios, but same hierarchies
- Better internal coherences of the fit
  - for  $P'_5$
  - between  $P'_5$  and  $R_K$
 for some of the scenarios
- $C_{9\mu}$  on the edge with  $R_K$ .  
 $C_{9\mu} = -C_{10\mu}$  and  $C_{10\mu}$  completely fail to explain  $P'_5$ .
- **RHCs counterbalance a very large and negative  $C_{9\mu}$  in  $R_K$**

# Summary of dominant scenarios and future outlook

Hypotheses	Param.	$P_5'^{[4,6]}$	$R_K$	$Q_5^{[1,6]}$	$\text{Pull}_{\text{SM}}$
$C_{9\mu}^{\text{NP}}$	1	✓	✓	+0.29	7.0
$\rightarrow [C_{9\mu}^{\text{V}} = -C_{10\mu}^{\text{V}}, C_9^{\text{U}}]^*$	2	✓	✓	+0.09	7.3
$\rightarrow [C_{9\mu}^{\text{NP}}, C_{9'\mu} = -C_{10'\mu}]$	2	✓	✓	+0.31	7.4

With only 1 or 2 parameters one gets excellent fit to data. Scenario (\*) moreover link with  $b \rightarrow c\tau\nu$  anomaly and naturally generates LFU in  $C_9$ +imply large  $b \rightarrow s\tau\tau$ .



Can we disentangle the two most interesting ones?:

- 1)  $[C_{9\mu}^{\text{NP}}, C_{9'\mu} = -C_{10'\mu}] \Rightarrow \text{Pull}_{\text{SM}} = 7.4\sigma$
- 2)  $[C_{9\mu}^{\text{V}} = -C_{10\mu}^{\text{V}}, C_9^{\text{U}}] \Rightarrow \text{Pull}_{\text{SM}} = 7.3\sigma$

- $R_K$  and  $R_{K^*}$  **cannot**.
- $Q_5$  **can**. It is a discriminator that can tell us if NP prefers a  $SU(2)_L$  structure  $C_{9\mu} = -C_{10\mu}$  or a vector one  $C_{9\mu}$ .

**Outlook:** a) large  $b \rightarrow s\tau\tau$  would point in favour of LFU ( $C_9^{\text{U}}$ ). b) large and  $Q_5 > 0$  would point in favour of large  $C_{9\mu}^{\text{NP}} < 0$  + possible RHCs.

# What else?



## Further work...

[M. Algueró et al., arXiv: 2107.05301]

I. We are now opening a new direction, turning nuisance parameters into signal.

The complete angular distribution

$$\frac{d^5\Gamma}{dq^2 dm_{K\pi}^2 d\Omega} = \frac{d^5\Gamma_P}{dq^2 dm_{K\pi}^2 d\Omega} + \frac{d^5\Gamma_S}{dq^2 dm_{K\pi}^2 d\Omega}$$

New observables from the S-wave piece  $B \rightarrow K_0^*(\rightarrow K\pi)l^+l^-$  ( $K_0^*$  a broad scalar resonance).

- ▶ Strong bounds on each individual new observable and globally  $< 0.3$  from symmetries.
- ▶ Two new S-wave optimized observables  $W_{1,2}$  defined and predicted from P-wave.
- ▶ Experimental present and future prospects at LHCb are presented.

II. In non-leptonic B decays ( $B_{d,s} \rightarrow K^{*0}\bar{K}^{*0}$ ) we build a new observable **L** based on a ratio of longitudinal amplitudes of  $b \rightarrow \textcolor{red}{s}/b \rightarrow \textcolor{red}{d}$  transitions analog of  $R_K$  ( $b \rightarrow s\mu^+\mu^-/b \rightarrow se^+e^-$ ).

- ▶  $L_{K^*\bar{K}^*}^{\text{exp}} = 4.43 \pm 0.92$  vs  $L_{K^*\bar{K}^*}^{\text{SM}} = 19.5_{-6.8}^{+9.3} \Rightarrow \mathbf{2.6\sigma \text{ tension.}}$  [M. Algueró et al., JHEP 04 (2021) 066]
- ▶ We identified the most probable responsible model-independently:

$$\mathcal{Q}_{4s} = (\bar{s}_i b_j)_{V-A} \sum_q (\bar{q}_j q_i)_{V-A}$$

- ▶ Natural candidate: Tree level massive  $SU(3)_c$  octet vector particle (KK gluon).  
...but significant fine-tuning due to  $\Delta M_{B_s}$ , dijet searches, ...
- ▶ Possible link to  $b \rightarrow s\ell\ell$ ?: KK gluon part of spectrum of composite model+ $Z'$  boson.

# Conclusions

We observe for the first time in particle physics a large set of **coherent** anomalies.

- ▶ Increase in the  $\text{Pull}_{\text{SM}}$  of the favoured scenarios, no change in hierarchy of scenarios.
- ▶ Three dominant scenarios:
  - ▶  $C_{9\mu}$  this basically rules out any scenario not including it:  $7.0\sigma$ .
  - ▶ **RHCs** in several scenarios: **Hypothesis V** ( $C_{9\mu}, C_{9'\mu} = -C_{10'\mu}$ ):  $7.4\sigma$ .
  - ▶ **LFU contributions**, in good agreement with simple EFT interpretations combining  $b \rightarrow c\ell\nu$  and  $b \rightarrow s\ell\ell$  anomalies: **Scenario 8** ( $C_9^U, C_9^V = -C_{10}^V$ ):  $7.3\sigma$ .

## Outlook and future directions:

We extended the analysis of  $B \rightarrow K\pi\mu\mu$  including **new S-wave observables**. We pointed out the relevance of two measurements:

- ▶  $b \rightarrow s\tau\tau$  governed decays that if enhanced favours LFU NP in  $C_9^U$  (Scenario 8).
- ▶  $Q_5$  that can disentangle between Hypothesis V (RHCs) and Scenario 8 (LFU).

A very **promising** new B-flavour anomaly in the non-leptonic sector has emerged showing a  $2.6\sigma$  tension w.r.t. SM in a new observable called **L-observable**  
... the dominant Wilson coefficients are identified and a possible first model...

# Backup slides

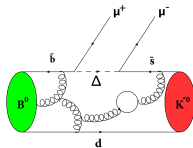
# A possible successful candidate?

A very promising candidate is:

Vector leptoquark  $SU(2)$  singlet:

$$U_1(3, 1, 2/3)$$

Coupled mainly to  $3^{rd}$  generation

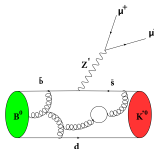


- ▶ It can explain both charged and neutral anomalies
- ▶  $C_9^V = -C_{10}^V$  pattern
- ▶ No tree level effect for  $b \rightarrow s \nu \bar{\nu}$
- ▶ No conflict with direct searches

**Good solution, but challenging UV completion.**

Examples:  $SU(4) \times U(2)_L \times SU(2)_R$  + vector like ferm (Calibbi, Crivellin, Li),  
 $SU(4) \times U(2) \times SU(2)_R$  in RS (Blanke, Crivellin),...

Many realizations of LFUV  $Z'$  models (if only  $b \rightarrow s \ell \ell$  is considered).



Pati-Salam extended  $PS^3 \equiv PS_1 \times PS_2 \times PS_3$  with  $PS_i = SU(4)_i \times [SU(2)_L]_i \times [SU(2)_R]_i$   
(Bordone et al.) TeV LQ associated to 3rd gen.



# A complete basis of optimized observables for the distribution

JHEP 04 (2012) 104, JHEP 01 (2013) 048

The most relevant ones are:

$$\mathbf{P}_1 = \frac{J_3}{2J_{2s}} = \frac{|A_{\perp}|^2 - |A_{\parallel}|^2}{|A_{\perp}|^2 + |A_{\parallel}|^2}$$

$$\mathbf{P}_2 = \frac{J_{6s}}{8J_{2s}} = \frac{\text{Re}[A_{\perp}^{L*} A_{\parallel}^L - A_{\perp}^R A_{\parallel}^{R*}]}{|A_{\perp}|^2 + |A_{\parallel}|^2}$$

$$\mathbf{P}'_4 = \frac{J_4}{\sqrt{-J_{2s}J_{2c}}} = \sqrt{2} \frac{\text{Re}[A_0^L A_{\parallel}^{L*} + A_0^R A_{\parallel}^{R*}]}{\sqrt{|A_0|^2(|A_{\perp}|^2 + |A_{\parallel}|^2)}}$$

$$\mathbf{P}'_5 = \frac{J_5}{2\sqrt{-J_{2s}J_{2c}}} = \sqrt{2} \frac{\text{Re}[A_0^L A_{\perp}^{L*} - A_0^R A_{\perp}^{R*}]}{\sqrt{|A_0|^2(|A_{\perp}|^2 + |A_{\parallel}|^2)}}$$

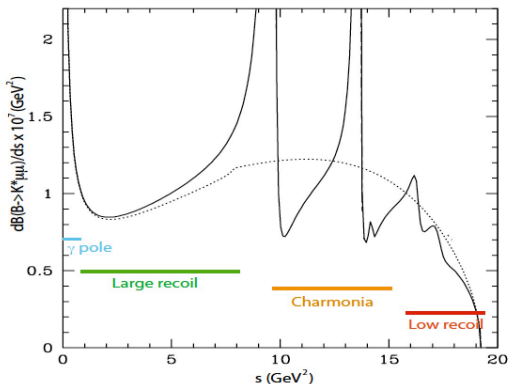
and the angular distribution:

$$\begin{aligned} \frac{1}{\Gamma'_{full}} \frac{d^4\Gamma}{dq^2 d\cos\theta_K d\cos\theta_l d\phi} &= \frac{9}{32\pi} \left[ \frac{3}{4} \mathbf{F_T} \sin^2\theta_K + \mathbf{F_L} \cos^2\theta_K + \left( \frac{1}{4} \mathbf{F_T} \sin^2\theta_K - \mathbf{F_L} \cos^2\theta_K \right) \cos 2\theta_l \right. \\ &+ \sqrt{\mathbf{F_T F_L}} \left( \frac{1}{2} \mathbf{P}'_4 \sin 2\theta_K \sin 2\theta_l \cos\phi + \mathbf{P}'_5 \sin 2\theta_K \sin\theta_l \cos\phi \right) + 2\mathbf{P}_2 \mathbf{F_T} \sin^2\theta_K \cos\theta_l + \frac{1}{2} \mathbf{P}_1 \mathbf{F_T} \sin^2\theta_K \sin^2\theta_l \cos \\ &\left. - \sqrt{\mathbf{F_T F_L}} \left( \mathbf{P}'_6 \sin 2\theta_K \sin\theta_l \sin\phi - \frac{1}{2} \mathbf{P}'_8 \sin 2\theta_K \sin 2\theta_l \sin\phi \right) - \mathbf{P}_3 \mathbf{F_T} \sin^2\theta_K \sin^2\theta_l \sin 2\phi \right] (1 - \mathbf{F_S}) + \frac{1}{\Gamma'_{full}} \mathbf{W_S} \end{aligned}$$

All  $P_i$ 's are constructed to cancel exactly at LO the dependence on SFF:  $7 \text{ FFs } (V, A_i, T_i) \rightarrow \xi_{\perp, \parallel} \text{ (SFF)}$

Our computation includes soft FF +  $\alpha_s$  factorizable from QCDF + power corrections to FFs + non-factorizable  $\alpha_s$  corrections from QCDF + long distance charm contributions (KMPW).

# Four regions in $q^2$ for the angular distribution $B \rightarrow K^*(\rightarrow K\pi)\mu^+\mu^-$



- ▶ **very large  $K^*$ -recoil** ( $4m_\ell^2 < q^2 < 1 \text{ GeV}^2$ ):  $\gamma$  almost real.
- ▶ **large  $K^*$ -recoil/low- $q^2$** :  $E_{K^*} \gg \Lambda_{QCD}$  or  $4m_\ell^2 \leq q^2 < 9 \text{ GeV}^2$ : LCSR-FF
- ▶ **charmonium region** ( $q^2 = m_{J/\psi}^2, \dots$ ) between  $9 < q^2 < 14 \text{ GeV}^2$ .
- ▶ **low  $K^*$ -recoil/large- $q^2$** :  $E_{K^*} \sim \Lambda_{QCD}$  or  $14 < q^2 \leq (m_B - m_{K^*})^2$ : LQCD-FF

## Soft Form Factors to parametrize $B \rightarrow K^*$

⇒ Different sets of form factors ( $V, A_{1,2}, T_{1,2,3}$ ) available:

KMPW (LCSR B meson DA, low  $q^2$ ) or BSZ (fit LCSR light meson DA + lattice).

► low  $q^2$  region: using EFT correlations arising in  $m_b \rightarrow \infty$ , e.g., at large  $K^*$  recoil

$$\begin{aligned}\xi_{\perp} &= \frac{m_B}{m_B + m_{K^*}} V = \frac{m_B + m_{K^*}}{2E_{K^*}} A_1 = T_1 = \frac{m_B}{2E_{K^*}} T_2 \\ \xi_{||} &= \frac{m_{K^*}}{E_{K^*}} A_0 = \frac{m_B + m_{K^*}}{2E_{K^*}} A_1 - \frac{m_B - m_{K^*}}{m_B} A_2 = \frac{m_B}{2E_{K^*}} T_2 - T_3\end{aligned}$$

$\xi_{\perp,||}$  are the *soft FF*.

Our analysis includes soft FF +  $\alpha_s$  factorizable from QCDF + power corrections + non-factorizable  $\alpha_s$  corrections and long distance charm (KMPW).

Even if the SM is extremely successful theory most likely is an effective theory,  
...it does not explain:

- ▶ why 3 generations of fermions? why their masses are so hierarchical.
- ▶ origin of the Baryon asymmetry in the universe? matter anti-matter asymmetry too small in SM.
- ▶ **lack of a candidate of the dark matter observed in the Universe**
- ▶ ...



a more fundamental theory with new degrees of freedom (**new properties**)

*This new theory defines what is usually called **New Physics***

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Two ways of searching for New Physics:

- ▶ **DIRECT** production of New Particles: so far nothing new....besides SM Higgs. It needs **Energy**.
- ▶ **INDIRECT** or VIRTUAL production of New Particles affecting (i.e. loops) couplings & **decays**
  - ⇒ Energy scales not directly accessible at accelerators.
  - ⇒ This is the approach of **Flavour Physics**