

# Probing the flavour of New Physics with dipoles

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Work in collaboration with S. Jäger (U. Sussex)  
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# Outline



1 Introduction

2 Four-fermion operators

3 Conclusions

# Moving beyond the flavour structure of the SM

→ Dipole effects:  $\mathcal{L}_{dipole} = e \frac{\nu_{EW}}{\sqrt{2}} \mathcal{C}_{\psi\gamma}^{\beta\alpha} \bar{\psi}_\beta \sigma^{\mu\nu} P_R \psi_\alpha F_{\mu\nu} + \text{h.c.}$

**E.M. form factors:** *Magnetic Dipole Moment* (MDM),  
*Electric Dipole Moment* (EDM)

**Flavour transitions:**  $\mu \rightarrow e\gamma$ ,  $\tau \rightarrow (e, \mu)\gamma$ ,  $\nu' \rightarrow \nu\gamma$ ,   
 $s \rightarrow d\gamma$ ,  $b \rightarrow (s, d)\gamma$ , etc.

→ Multitask tool: flavour structure (e.g., LFV) & CPV sources of the SM & BSM, in quark & lepton sectors [Lomonosov: various talks]

$$\text{eEDM: } |\text{Im}[\mathcal{C}_{e\gamma}^{ee}]| \lesssim (8 \times 10^5 \text{ TeV})^{-2} \quad [\text{ACME}]$$

$$\mu \rightarrow e\gamma: \sqrt{|\mathcal{C}_{e\gamma}^{e\mu}|^2 + |\mathcal{C}_{e\gamma}^{\mu e}|^2} \lesssim (4 \times 10^4 \text{ TeV})^{-2} \quad [\text{MEG}]$$

$$\text{nEDM: } |\text{Im}[\mathcal{C}_{d\gamma}^{dd}]|, |\text{Im}[\mathcal{C}_{u\gamma}^{uu}]| \lesssim (2 \times 10^4 \text{ TeV})^{-2} \quad [\text{nEDM}]$$

→ **SM highly suppressed:** signs of NP are clearly identifiable

→ Possibly provide new insights to understand the origin of flavour

# SMEFT: new heavy sector much above EW scale

- No discovery of non-SM particles below the EW scale
- Generic NP involving new heavy sector  $\sim \Lambda \gg v_{\text{EW}}$
- Consider operators  $Q^{(n)}$  respecting SM local symmetries and containing SM d.o.f. only
- Non-SM interaction strengths  $C^{(n)}$  among the d.o.f. that we know

$$\frac{C^{(5)} \times Q^{(5)}}{\Lambda}, \quad \frac{C^{(6)} \times Q^{(6)}}{\Lambda^2}, \quad \frac{C^{(7)} \times Q^{(7)}}{\Lambda^3}, \quad \frac{C^{(8)} \times Q^{(8)}}{\Lambda^4}, \text{ etc.}$$

- New weak sector: typically effects from lower-dimensionality operators are more important for low-energy observables

# Dimension-six operators

- Focus on operators of **dimension-six**
- Equations Of Motion (EOMs) eliminate redundant cases:  
59 linearly independent operators,  
with 1350 CP-even + 1149 CP-odd couplings,  
assuming SM global symmetries,  $B_{\text{tot}}$  and  $L_{\text{tot}}$

Warsaw:  $X^3, H^6, H^4D^2, \psi^2H^3, X^2H^2, \psi^2XH, \psi^2H^2D, \psi^4$   
 [ $\psi$  fermions;  $D$  cov. derivative;  $X$  field strengths]

[Buchmüller, Wyler '86; Grzadkowski, Iskrzyński, Misiak, Rosiek '10]

$\underbrace{\psi^2XH}_{\mathcal{L}_{\text{dipole}} @ \text{tree}}$  class:  $(\bar{q}\sigma^{\mu\nu}d)HB_{\mu\nu}, (\bar{q}\sigma^{\mu\nu}d)\tau^IHW_{\mu\nu}^I, (\bar{q}\sigma^{\mu\nu}T^A d)HG_{\mu\nu}^A$ , etc.  
 [ $q, \ell, H$  ( $d, u, e$ )  $SU(2)$  doublet (singlet)]

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 [ $\psi$  fermions;  $D$  cov. derivative;  $X$  field strengths]

[Buchmüller, Wyler '86; Grzadkowski, Iskrzyński, Misiak, Rosiek '10]

$\underbrace{\psi^4}_{\text{Fermi-like}}$  class:  $(\bar{L}L)(\bar{L}L)$ ,  $(\bar{R}R)(\bar{R}R)$ ,  $(\bar{L}L)(\bar{R}R)$ ,  $(\bar{L}R)(\bar{R}L)$ ,  $(\bar{L}R)(\bar{L}R)$   
 [ $q, \ell, H$  ( $d, u, e$ )  $SU(2)$  doublet (singlet)]

# Probing non-dipole operators

Consider  $\mathcal{L} = \mathcal{L}_{\text{SM}} + \sum_i C_i Q_i$ , where  $C_i$  scales as  $\Lambda^{-2}$

Mixing with dipole:

$$16\pi^2 \frac{d}{d\ln(\mu)} C_{\psi^2 X H}(\mu) = \sum_i (C_{\psi^2 X H}, C_{\psi^4}, C_{X^3}, C_{X^2 H^2})_i(\mu) \gamma_{i,\psi^2 X H}^{(1\text{-loop})}$$

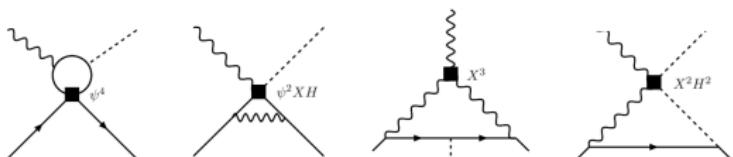
$$\{\psi^2 X H, \psi^4, X^3, X^2 H^2\} \xrightarrow[1\text{Loop}]{RGE} \psi^2 X H$$

[1-loop, e.g.: Alonso, Jenkins, Manohar, Trott '13,  
Cirigliano, Crivellin, Dekens, de Vries, Hoferichter, Mereghetti '19,  
Aebischer, Dekens, Jenkins, Manohar, Sengupta, Stoffer '21]

Example: [ACME]

$$|\text{Im } \tilde{C}_{\ell equ}^{(3), eett}| \lesssim (3 \times 10^5 \text{ TeV})^{-2}$$

$$Q_{\ell equ}^{(3)} = (\bar{\ell}^j \sigma_{\mu\nu} e) \epsilon_{jk} (\bar{q}^k \sigma^{\mu\nu} u)$$



[■: possible vertices]

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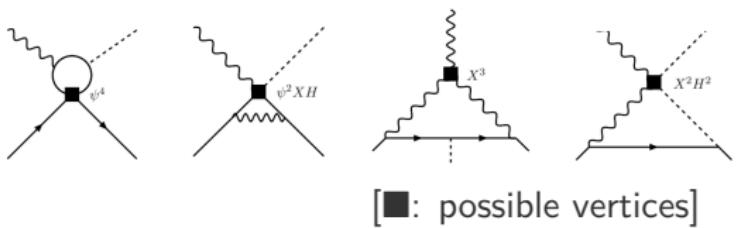
$$\{\psi^2 X H, \psi^4, X^3, X^2 H^2\} \xrightarrow[1\text{Loop}]{RGE} \psi^2 X H$$

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**HERE:** 4-fermion ops. for which  $\gamma_{i, \psi^2 X H}^{(1\text{-loop})} = 0$  (i.e., no mix. at 1-loop)

→ Leading Order mixing with the dipole arriving at 2-loops

→ Phenomenological implications

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→ Four-fermions: only  $Q_{\ell equ}^{(3)}$  mixes directly w/ dipoles at 1-loop

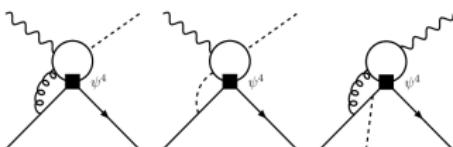
$$Q_{\ell equ}^{(1)} \xrightarrow[1\text{Loop}]{RGE} Q_{\ell equ}^{(3)} \xrightarrow[1\text{Loop}]{RGE} \psi^2 X H$$

### LRLR operators

$$\begin{aligned} Q_{\ell equ}^{(1)}(prst) &= (\bar{\ell}_p e_r) \epsilon_{jk} (\bar{q}_s^k u_t) \\ Q_{\ell equ}^{(3)}(prst) &= (\bar{\ell}_p^\beta \sigma_{\mu\nu} e_r) \epsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t) \\ Q_{\ell \nu qd}^{(1)}(prst) &= (\bar{\ell}_p^\beta \nu_r) \epsilon_{jk} (\bar{q}_s^k d_t) \\ Q_{\ell \nu qd}^{(3)}(prst) &= (\bar{\ell}_p^\beta \sigma_{\mu\nu} \nu_r) \epsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} d_t) \end{aligned}$$

### LRLR operators

$$\begin{aligned} Q_{\ell \nu \ell c}(prst) &= (\bar{\ell}_p^\beta \nu_r) \epsilon_{jk} (\bar{\ell}_s^k e_t) \\ Q_{quqd}^{(1)}(prst) &= (\bar{q}_p^j u_r) \epsilon_{jk} (\bar{q}_s^k d_t) \\ Q_{quqd}^{(8)}(prst) &= (\bar{q}_p^j T^A u_r) \epsilon_{jk} (\bar{q}_s^k T^A d_t) \end{aligned}$$



### LRRL operators

$$\begin{aligned} Q_{\ell edq}(prst) &= (\bar{\ell}_p e_t) (\bar{d}_s q_r) \\ Q_{\ell \nu uq}(prst) &= (\bar{\ell}_p \nu_t) (\bar{u}_s q_r) \end{aligned}$$

### [Fierzed] LLRR operators

$$\begin{aligned} Q_{\ell \ell c}(prst) &= (\bar{\ell}_p e_t) (\bar{e}_s \ell_r) \\ Q_{\ell \nu}(prst) &= (\bar{\ell}_p \nu_t) (\bar{\nu}_s \ell_r) \\ Q_{qu}^{(1)}(prst) &= (\bar{q}_p^\alpha u_r^\beta) (\bar{u}_s^\beta q_r^\alpha) \\ Q_{qu}^{(8)}(prst) &= (\bar{q}_p^\alpha T_{\alpha\tilde{\alpha}} u_r^\beta) (\bar{u}_s^\beta T_{\beta\tilde{\beta}} q_r^\alpha) \\ Q_{qd}^{(1)}(prst) &= (\bar{q}_p^\alpha d_r^\beta) (\bar{d}_s^\beta q_r^\alpha) \\ Q_{qd}^{(8)}(prst) &= (\bar{q}_p^\alpha T_{\alpha\tilde{\alpha}} d_r^\beta) (\bar{d}_s^\beta T_{\beta\tilde{\beta}} q_r^\alpha) \end{aligned}$$

### [Fierzed] LLRR operators

$$\begin{aligned} Q_{\ell u}(prst) &= (\bar{\ell}_p u_t) (\bar{u}_s \ell_r) \\ Q_{td}(prst) &= (\bar{\ell}_p d_t) (\bar{d}_s \ell_r) \\ Q_{qe}(prst) &= (\bar{q}_p e_t) (\bar{e}_s q_r) \\ Q_{qu}(prst) &= (\bar{q}_p \nu_t) (\bar{\nu}_s q_r) \end{aligned}$$

### LLLL operators

$$\begin{aligned} Q_{\ell\ell}(prst) &= (\bar{\ell}_p \gamma_\mu \ell_r) (\bar{\ell}_s \gamma^\mu \ell_t) \\ Q_{qq}^{(1)}(prst) &= (\bar{q}_p \gamma_\mu q_r) (\bar{q}_s \gamma^\mu q_t) \\ Q_{qq}^{(3)}(prst) &= (\bar{q}_p \gamma_\mu \tau^I q_r) (\bar{q}_s \gamma^\mu \tau^I q_t) \\ Q_{\ell q}^{(1)}(prst) &= (\bar{\ell}_p \gamma_\mu \ell_r) (\bar{q}_s \gamma^\mu q_t) \\ Q_{\ell q}^{(3)}(prst) &= (\bar{\ell}_p \gamma_\mu \tau^I \ell_r) (\bar{q}_s \gamma^\mu \tau^I q_t) \end{aligned}$$

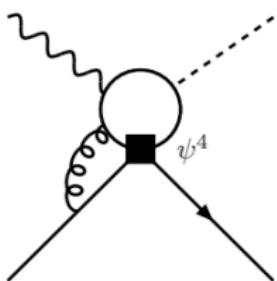
### RRRR operators

$$\begin{aligned} Q_{ee}(prst) &= (\bar{e}_p \gamma_\mu e_r) (\bar{e}_s \gamma^\mu e_t) \\ Q_{\nu\nu}(prst) &= (\bar{\nu}_p \gamma_\mu \nu_r) (\bar{\nu}_s \gamma^\mu \nu_t) \\ Q_{uu}(prst) &= (\bar{u}_p \gamma_\mu u_r) (\bar{u}_s \gamma^\mu u_t) \\ Q_{dd}(prst) &= (\bar{d}_p \gamma_\mu d_r) (\bar{d}_s \gamma^\mu d_t) \\ Q_{eu}(prst) &= (\bar{u}_p \gamma^\mu u_r) (\bar{e}_s \gamma_\mu e_t) \\ Q_{ed}(prst) &= (\bar{e}_p \gamma_\mu e_r) (\bar{d}_s \gamma^\mu d_t) \\ Q_{\nu u}(prst) &= (\bar{\nu}_p \gamma_\mu \nu_r) (\bar{u}_s \gamma^\mu u_t) \\ Q_{\nu d}(prst) &= (\bar{\nu}_p \gamma_\mu \nu_r) (\bar{d}_s \gamma^\mu d_t) \\ Q_{e\nu}(prst) &= (\bar{\nu}_p \gamma_\mu \nu_r) (\bar{e}_s \gamma^\mu e_t) \\ Q_{ud}^{(1)}(prst) &= (\bar{u}_p \gamma_\mu u_r) (\bar{d}_s \gamma^\mu d_t) \\ Q_{ud}^{(8)}(prst) &= (\bar{u}_p \gamma_\mu T^A u_r) (\bar{d}_s \gamma^\mu T^A d_t) \\ Q_{duve}(prst) &= (\bar{d}_p \gamma_\mu u_r) (\bar{\nu}_s \gamma^\mu e_t) \end{aligned}$$

→ Focus on light external fermions:  LRLR,  LRRL,  LRLR

→  1-loop,  main focus here (preliminary),  ongoing calculation

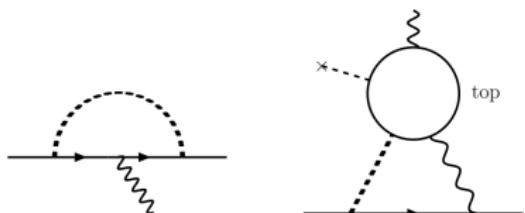
# Contributions proportional to a large Yukawa



Possible enhancements: large Yukawa, strong coupling, color factor

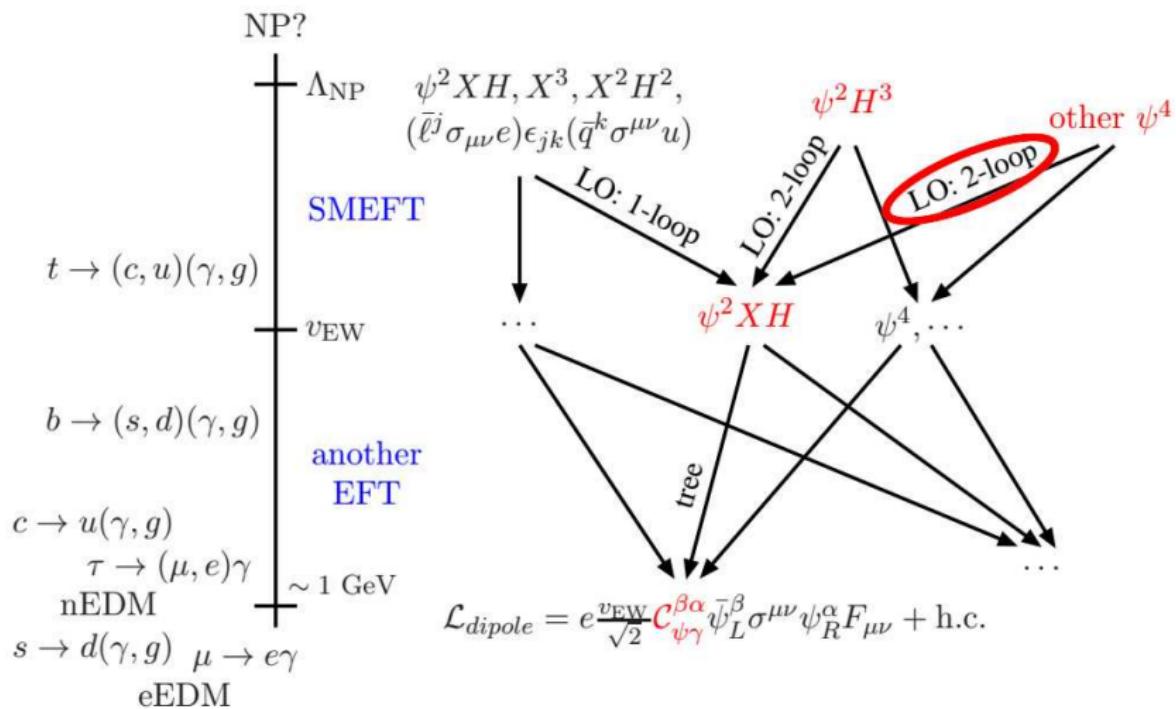
→ Analogous to Barr-Zee diagrams

[Bjorken, S. Weinberg '77; Barr, Zee '90; see also Davidson '16]



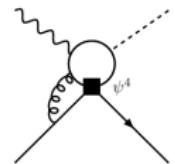
→ In the following: preliminary bounds from  $\mu \rightarrow e\gamma$ , EDMs

# Roadmap to phenomenology



# CP violation in light quark dipoles

- One-loop ADM:  $Q_{\ell equ}^{(1)}$ ,  $Q_{\ell equ}^{(3)}$
- Two-loop,  $y_t$ -enhancement:  $Q_{qu}^{(1)}$ ,  $Q_{qu}^{(8)}$ ,  $Q_{quqd}^{(1)}$ ,  $Q_{quqd}^{(8)}$
- Two-loop:  $Q_{qd}^{(1)}$ ,  $Q_{qd}^{(8)}$ ,  $Q_{\ell edq}$



$$(16\pi^2)^2 \frac{d}{d\ln(\mu)} C_{\psi^2 X H}(\mu) = (g_Y^2 \gamma_Y^X + g_L^2 \gamma_L^X + g_C^2 \gamma_c^X + Y^2 \gamma^X) \times Y \times C_{\psi^4}(\mu)$$

$$Q_{qu}^{(1)} = (\bar{q}_p^\alpha u_t^\beta)(\bar{u}_s^\beta q_r^\alpha) \quad Q_{qu}^{(8)} = (\bar{q}_p^\alpha T_{\alpha\tilde{\alpha}}^A u_t^{\tilde{\beta}})(\bar{u}_s^\beta T_{\beta\tilde{\beta}}^A q_r^{\tilde{\alpha}})$$

$\xrightarrow{\text{ext}}$ $\downarrow \text{int}$	$X = B$	$X = W$	$X = G$	$\xrightarrow{\text{ext}}$ $\downarrow \text{int}$	$X = B$	$X = W$	$X = G$
$\gamma_Y^X$	$-\frac{1655}{6912}$	$+\frac{701}{2304}$	$+\frac{7}{72}$	$\gamma_Y^X$	$-\frac{1655}{1296}$	$+\frac{701}{432}$	$-\frac{679}{576}$
$\gamma_L^X$	$+\frac{587}{768}$	$-\frac{923}{768}$	$+\frac{5}{8}$	$\gamma_L^X$	$+\frac{587}{144}$	$-\frac{923}{144}$	$-\frac{935}{192}$
$\gamma_c^X$	$-\frac{20}{9}$	$-\frac{4}{3}$	$+\frac{11}{3}$	$\gamma_c^X$	$+\frac{760}{27}$	$+\frac{152}{9}$	$+\frac{446}{9}$

- $X = G$ : Chromo-Magnetic Dipole Moment

# Light quark dipole moments, pheno

→ Electric Dipole Moment:

$$c_{u\gamma}(\mu) \simeq \frac{1}{(16\pi^2)^2} \times \ell n \left( \frac{\Lambda^2}{\mu^2} \right) \times \mathbf{y}_{top} \times \left\{ C_{qu}^{(1)}(\Lambda) \left( -0.9 \times g_L^2 + 0.4 \times g_c^2 \right) + C_{qu}^{(8)}(\Lambda) \left( -4.8 \times g_L^2 - 5.6 \times g_c^2 \right) \right\}$$

→ Chromo-MDM generates a CPV  $\pi NN$  coupling [see, e.g., Pospelov, Ritz '05]

$$c_{uG}(\mu) \simeq \frac{1}{(16\pi^2)^2} \times \ell n \left( \frac{\Lambda^2}{\mu^2} \right) \times \mathbf{y}_{top} \times \left\{ C_{qu}^{(1)}(\Lambda) \left( -0.3 \times g_L^2 - 1.8 \times g_c^2 \right) + C_{qu}^{(8)}(\Lambda) \left( 2.6 \times g_L^2 - 24.8 \times g_c^2 \right) \right\}$$

	$y_{top} \times  \text{Im}\{\tilde{C}_{qu}^{(1)}(\Lambda)\} $	$y_{top} \times  \text{Im}\{\tilde{C}_{qu}^{(8)}(\Lambda)\} $
$ d_N $	$\mathcal{O}(10^{-4}) \text{ TeV}^{-2}$	$\mathcal{O}(10^{-5}) \text{ TeV}^{-2}$
$ d_{Hg} $	$\mathcal{O}(10^{-6}) \text{ TeV}^{-2}$	$\mathcal{O}(10^{-7}) \text{ TeV}^{-2}$

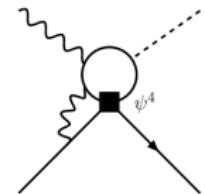
→ Wilson coefficients  $\lesssim (700 \text{ TeV})^{-2} - (3000 \text{ TeV})^{-2}$

→ No dynamical tops below EW scale: effects from mix in SMEFT

# Charged light lepton dipoles

→ One-loop ADM:  $Q_{\ell equ}^{(1)}, Q_{\ell equ}^{(3)}$

→ Two-loop,  $y_\tau, y_b$ -enhanced:  $Q_{\ell e}, Q_{\ell edq}$



$$(16\pi^2)^2 \frac{d}{d\ln(\mu)} C_{\psi^2 X H}(\mu) = (g_Y^2 \gamma_Y^X + g_L^2 \gamma_L^X + g_C^2 \gamma_c^X + Y^2 \gamma^X) \times Y \times C_{\psi^4}(\mu)$$

$$Q_{\ell e} = (\bar{\ell}_p e_t)(\bar{e}_s \ell_r)$$

$$Q_{\ell edq} = (\bar{\ell}_p e_t)(\bar{d}_s q_r)$$

$\begin{matrix} \text{ext} \\ \downarrow \\ \text{int} \end{matrix}$	$X = B$	$X = W$	$X = G$	$\begin{matrix} \text{ext} \\ \downarrow \\ \text{int} \end{matrix}$	$X = B$	$X = W$	$X = G$
$\gamma_Y^X$	$+\frac{185}{256}$	$+\frac{331}{768}$	0	$\gamma_Y^X$	$-\frac{135}{256}$	$+\frac{619}{768}$	0
$\gamma_L^X$	$-\frac{249}{256}$	$-\frac{923}{768}$	0	$\gamma_L^X$	$-\frac{345}{256}$	$-\frac{923}{768}$	0
$\gamma_c^X$	0	0	0	$\gamma_c^X$	0	0	0

$$C_{e\gamma}(\mu) \simeq \frac{1}{(16\pi^2)^2} \times \ell n \left( \frac{\Lambda^2}{\mu^2} \right) \times \{-0.2 \times C_{\ell e}(\Lambda) \times \mathbf{y}_\tau + 0.3 \times C_{\ell edq}(\Lambda) \times \mathbf{y}_b\} \times g_L^2$$

# Charged light lepton dipoles, pheno

→ Mixing below EW scale, e.g.,  $(\bar{\ell} P_L \ell') (\bar{f} P_R f)$ ,  $\ell, \ell' = \mu, e$ ,  $f = b, \tau$

[Estimate of RGE below EW scale: Crivellin, Davidson, Pruna, Signer '17]

**eEDM:**  $Q_{\ell e}$

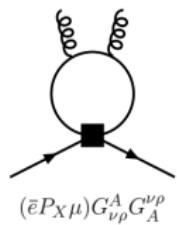
$$|\text{Im}\{\tilde{C}_{\ell e}^{\ell \tau \tau e}(\Lambda)\}| \times y_\tau \lesssim \mathcal{O}(10^{-7}) \text{ TeV}^{-2}$$

[Similar bounds found by Panico, Pomarol, Riembau '18]

$\mu \rightarrow e\gamma$ :  $Q_{\ell e}$

$$|\tilde{C}_{\ell e}^{\mu \tau \tau e}(\Lambda)| \times y_\tau \lesssim \mathcal{O}(10^{-5}) \text{ TeV}^{-2}$$

→ Wilson coefficients  $\lesssim (10 \text{ TeV})^{-2} - (400 \text{ TeV})^{-2}$

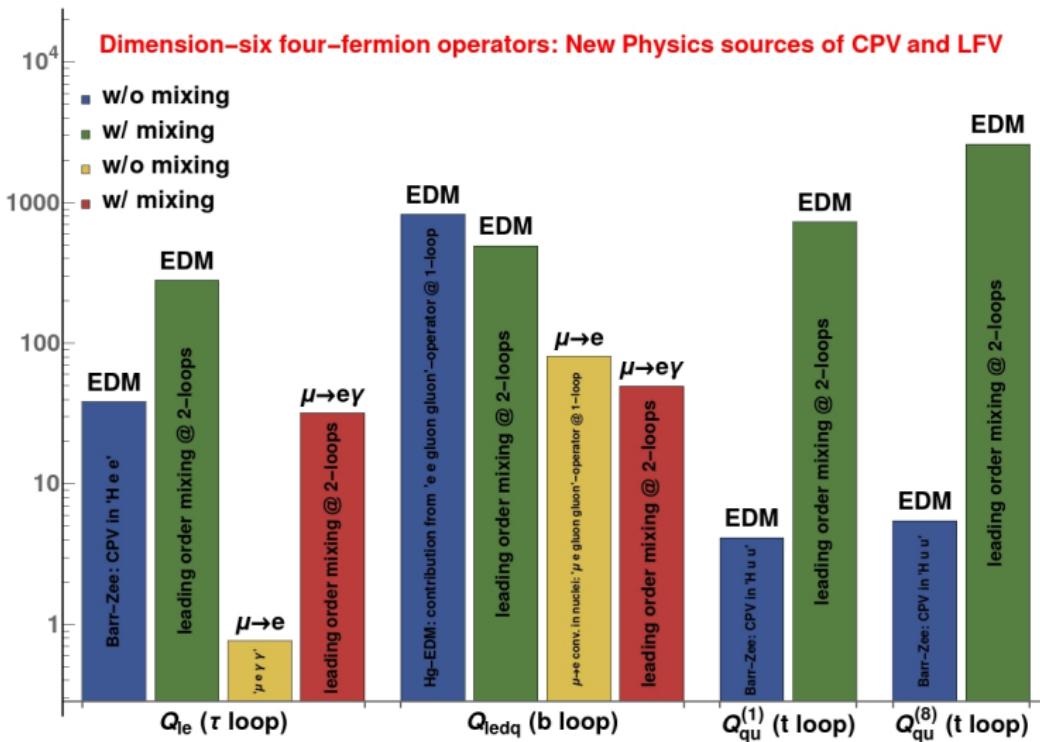


$Q_{\ell edq}$ , effect at 1-loop : stronger bound on  $\tilde{C}_{\ell edq}^{\mu bbe, ebbe}(\Lambda)$

[Shifman, Vainshtein, Zakharov '78; Crivellin, Davidson, Pruna, Signer '17;  $\gamma\gamma$ : Davidson, Kuno, Uesaka, Yamanaka '20]

# Summary, pheno

New Physics scale in TeV (Wilson coefficients = 1)



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# Conclusions

- Dipoles: probe very high energy scales, e.g., EDMs,  $\mu \rightarrow e\gamma$
- **Generic tool** for improving our understanding of flavour and CPV
- SMEFT: **systematic approach** to deal with new heavy sector
- Here: Leading-Order 2-loop effects generated by operator mixing
- Present measurements already allow strong bounds on NP

**Thanks!** (luizva -\*- ific.uv.es)

# Backup

*Painting: Moscow by Alexander Pervukhin*

# Summary $\psi^4$

→ 2-loops in many cases: better bounds than tree and 1-loop

[e.g., (semi-)leptonic, low-energy + LHC: Falkowski, González-Alonso, Mimouni '15 '17]

$$\psi^4 \xrightarrow[2\text{Loop}]{RGE} \psi^2 XH, \text{ preliminary}$$

	Observable	Coupling	Bound
$Q_{qu}^{(1)}$	Hg-EDM	$y_{top} \times  \text{Im}[\tilde{C}_{qu}^{(1), uttu}(\Lambda)] $	$\lesssim \mathcal{O}(10^{-6}) \text{ TeV}^{-2}$
		$y_{top} \times  \text{Im}[\tilde{C}_{qu}^{(8), uttu}(\Lambda)] $	$\lesssim \mathcal{O}(10^{-7}) \text{ TeV}^{-2}$
$Q_{\ell e}$	$\mu \rightarrow e\gamma$	$y_\tau \times \sqrt{ \tilde{C}_{\ell e}^{e\tau\tau\mu}(\Lambda) ^2 +  \tilde{C}_{\ell e}^{\mu\tau\tau e}(\Lambda) ^2}$	$\lesssim \mathcal{O}(10^{-5}) \text{ TeV}^{-2}$
	eEDM	$y_\tau \times  \text{Im}[\tilde{C}_{\ell e}^{e\tau\tau e}(\Lambda)] $	$\lesssim \mathcal{O}(10^{-7}) \text{ TeV}^{-2}$
$Q_{\ell edq}$	$\mu \rightarrow e$ conv.	$y_b \times \sqrt{ \tilde{C}_{\ell edq}^{ebb\mu}(\Lambda) ^2 +  \tilde{C}_{\ell edq}^{\mu bbe}(\Lambda) ^2}$	(1Loop)
	Hg-EDM	$y_b \times  \text{Im}[\tilde{C}_{\ell edq}^{ebbe}(\Lambda)] $	(1Loop)

(ongoing analysis for further operators, channels, and couplings)

2-Loop effects set most important bounds in many cases

# Summary $\psi^2 H^3$

$$\psi^2 H^3 \xrightarrow[2\text{Loop}]{RGE} \psi^2 XH, \text{ preliminary}$$

Observable	Coupling	Bound
$\mu \rightarrow e\gamma$	$\sqrt{ \tilde{C}_{eH}^{e\mu}(\Lambda) ^2 +  \tilde{C}_{eH}^{\mu e}(\Lambda) ^2}$	$\lesssim 0.02 \times \frac{\sqrt{2m_e m_\mu}}{\sqrt[3]{EW}}$
eEDM	$ \text{Im}[\tilde{C}_{eH}^{ee}(\Lambda)] $	$\lesssim 0.002 \times \frac{\sqrt{2m_e}}{\sqrt[3]{EW}}$
$h \rightarrow e\tau$	$\sqrt{ \tilde{C}_{eH}^{e\tau} ^2 +  \tilde{C}_{eH}^{\tau e} ^2}$	(tree)
$h \rightarrow \mu\tau$	$\sqrt{ \tilde{C}_{eH}^{\mu\tau} ^2 +  \tilde{C}_{eH}^{\tau\mu} ^2}$	(tree)
$h \rightarrow ee$	$ \tilde{C}_{eH}^{ee} $	(tree)
$h \rightarrow \mu\mu$	$ \tilde{C}_{eH}^{\mu\mu} $	(tree)
nEDM	$\left  \text{Im}[\tilde{C}_{\psi H}^{\psi\psi}(\Lambda)] \right _{(\psi=u,d)}$	$\lesssim 3 \times \frac{\sqrt{2m_d}}{\sqrt[3]{EW}}$
$ \Delta q' ,  \Delta q  = 2$ $(q, q' = u, d, s, c, b)$	$ \tilde{C}_{\psi H}^{qq'} ^2 +  \tilde{C}_{\psi H}^{q'q} ^2$	(tree)

2-Loop effects set most important bounds in many cases

$$\mathcal{B}(h \rightarrow e\mu) < 6.1 \times 10^{-5} \text{ (95% CL)} \quad [\text{Aad:2019ojw}]$$

$$\mathcal{B}(h \rightarrow e\tau) < 4.7 \times 10^{-3} \text{ (95% CL)} \quad [\text{Aad:2019ugc}]$$

$$\mathcal{B}(h \rightarrow \mu\tau) < 2.5 \times 10^{-3} \text{ (95% CL)} \quad [\text{Sirunyan:2017xzt}]$$

$$\mathcal{B}(\mu \rightarrow e\gamma) < 4.2 \times 10^{-13} \text{ (90% CL)} \quad [\text{TheMEG:2016wtm}]$$

$$\mathcal{B}(\tau \rightarrow e\gamma) < 3.3 \times 10^{-8} \text{ (90% CL)} \quad [\text{Aubert:2009ag}]$$

$$\mathcal{B}(\tau \rightarrow \mu\gamma) < 4.4 \times 10^{-8} \text{ (90% CL)} \quad [\text{Aubert:2009ag}]$$

$$\Delta a_e = a_e^{\text{exp}} - a_e^{\text{SM}} = -0.88(0.36) \times 10^{-12} @ 1\sigma \quad [\text{Parker:2018}]$$

$$\Delta a_\mu = a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = 268(63)(43) \times 10^{-11} @ 1\sigma \quad [\text{Tanabashi:2018oca}]$$

$$|d_e|/e < 1.1 \times 10^{-29} \text{ cm (90% CL)} \quad [\text{Andreev:2018ayy}]$$

$$|d_\mu|/e < 1.8 \times 10^{-19} \text{ cm (95% CL)} \quad [\text{Bennett:2008dy, PDG}]$$

$$d_\tau/e \in [-2.2, 4.5] \times 10^{-17} \text{ cm (95% CL)} \quad [\text{Inami:2002ah}]$$

$$|d_N|/e < 1.8 \times 10^{-26} \text{ cm (90% CL)} \quad [\text{Abel:2020gbr}]$$

$$|d_{\text{Hg}}|/e < 7.4 \times 10^{-30} \text{ cm (95% CL)} \quad [\text{Graner:2016ses}]$$