

A theory perspective on sterile neutrinos at colliders

**Lomonosov Conference – Moscow State University, Zoom
Campus**

Richard E. Ruiz

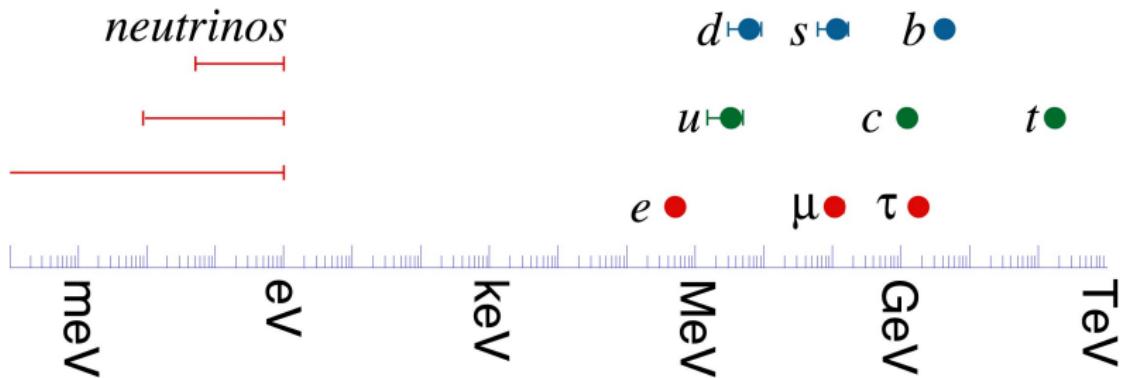
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20 August 2021



the ν case for new physics

Problem: according to the SM, $m_\nu = 0$. (The data disagree, obviously.)



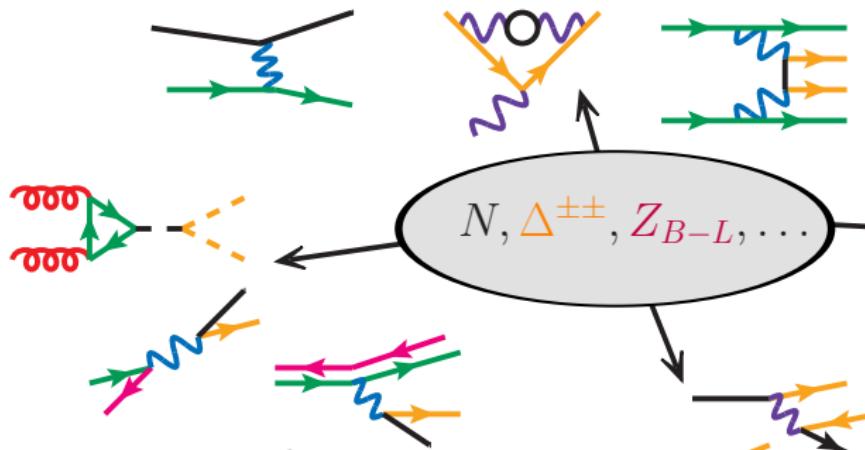
Neutrino masses  ('15) \Rightarrow **many open questions:**

- ν have mass. **What is generating m_ν ?**
- ν masses are *tiny*. **What sets the scale of m_ν ?**
- m_ν are nearly degenerate. **What sets the pattern of m_ν ?**
- ν carry no QCD/QED charge. **Are $\nu, \bar{\nu}$ the same (Majorana)?**

Neutrino mass (Seesaw) models give answers to these questions!

Many ways to explore neutrino mass models

1. Indirect production at non – accelerator laboratories



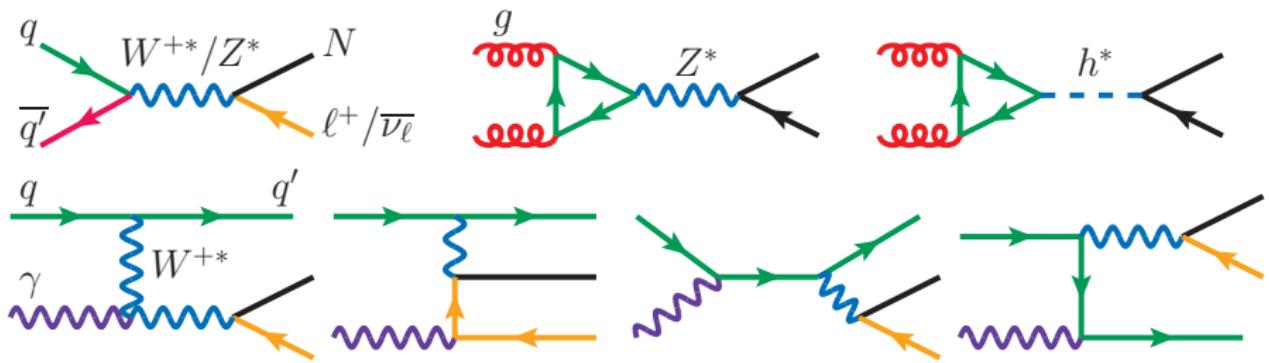
2. Direct production $h^0, W^\pm, \pi^\pm, {}^3H, \dots$

3. Infer properties from SM processes

4. Simulation software/tools

```
subroutine getDecay
    implicit none
    double precision,
    lifetime = hbar /
    print *, ...
end subroutine
```

Sterile neutrinos and the Type I Seesaw Mechanism(s)¹



¹ See backup for Weinberg Operator!

To generate Dirac masses for ν like other SM fermions, we need ν_R

$$\mathcal{L}_{\nu \text{ Yuk.}} = -y_{\nu} \bar{L} \tilde{\Phi} \nu_R + \dots = \underbrace{-y_{\nu} \langle \Phi \rangle \bar{\nu}_L \nu_R}_{\equiv m_{\nu}} + \dots$$

ν_R do not exist in the SM, so pretend that they do!

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Type I Seesaw mechanisms: hypothesize SM + ν_R with right-handed Majorana mass $m_R = \Lambda_{\text{LNV}}$

- **Depending** on assumptions, $m_{\nu} \sim \Lambda_{\text{LNV}}$ or $\langle \Phi \rangle^2 / \Lambda_{\text{LNV}}$
- **Important:** EW-scale N do **not** decouple in pure Type I, only LNV

Pascoli, et al [1712.07611]

- **Corollary:** EW-scale N + LNV \implies more new particles RR [1703.04669]

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At low energies, ν_{ℓ} and ν_R have same quantum numbers \implies mixing!

- Express chiral/interaction eigenstates in terms of mass states:

$$\underbrace{|\nu_L\rangle}_{\text{interaction basis}} = \cos \theta \underbrace{|\nu\rangle}_{\text{light}} + \sin \theta \underbrace{|N\rangle}_{\text{heavy}}$$

In practice (1 slide)

Generically parameterize active-sterile neutrino mixing via

Atre, Han, Pascoli, Zhang [0901.3589]

$$\underbrace{\nu_{\ell L}}_{\text{flavor basis}} \approx \underbrace{\sum_{m=1}^3 U_{\ell m} \nu_m + V_{\ell m'=4} N_{m'=4}}_{\text{mass basis}}$$

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The SM W chiral coupling to **leptons** in **flavor basis** is

$$\mathcal{L}_{\text{Int.}} = -\frac{g_W}{\sqrt{2}} W_\mu^- \sum_{\ell=e}^\tau [\bar{\ell} \gamma^\mu P_L \nu_\ell] + \text{H.c.}, \quad \text{where } P_L = \frac{1}{2}(1 - \gamma^5)$$

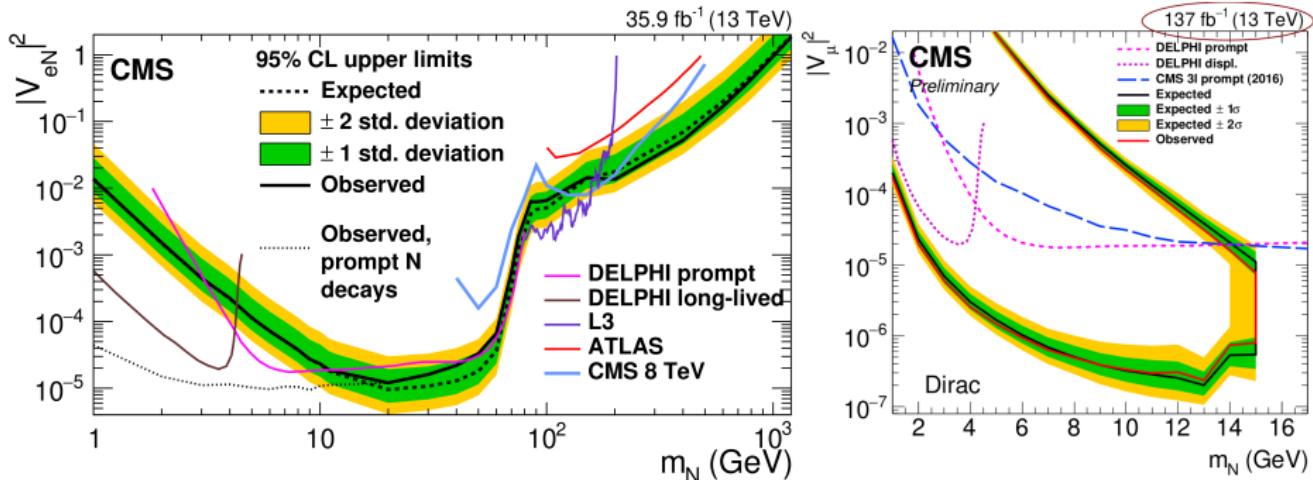
⇒ SM W coupling to N and charged **leptons** in the **mass basis** is

$$\mathcal{L}_{\text{Int.}} = -\frac{g_W}{\sqrt{2}} W_\mu^- \sum_{\ell=e}^\tau \left[\bar{\ell} \gamma^\mu P_L \left(\sum_{m=1}^3 U_{\ell m} \nu_m + V_{\ell N} N \right) \right] + \text{H.c.}$$

⇒ N is **accessible through $W/Z/h$ bosons**

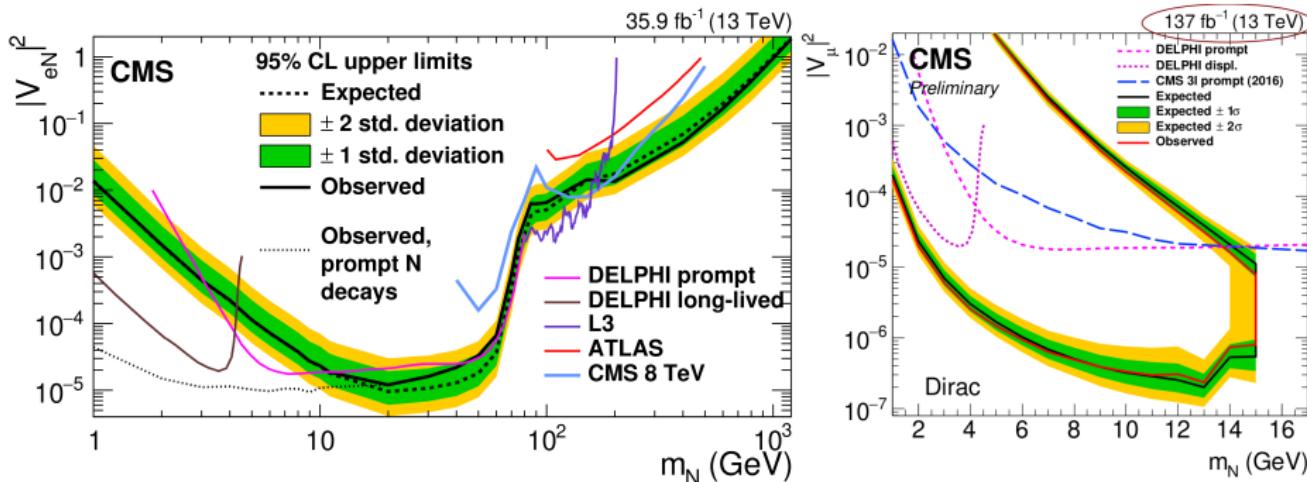
what do the experiments say?

Plotted: LHC 13 limits in search for $pp \rightarrow 3\ell + MET$ ($\ell_X = e, \mu$)



No discovery 😞 but there is hope with $20\times$ more data! 😊

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No discovery 😞 but there is hope with $20\times$ more data! 😊

- (L) CMS experiments's trilepton search for short-lived N [1802.02965]
- (R) NEW: search for long-lived N [CMS-PAS-EXO-20-009]
- same-sign dilepton searches [1806.10905]
- ATLAS search for long-lived N [1905.09787]

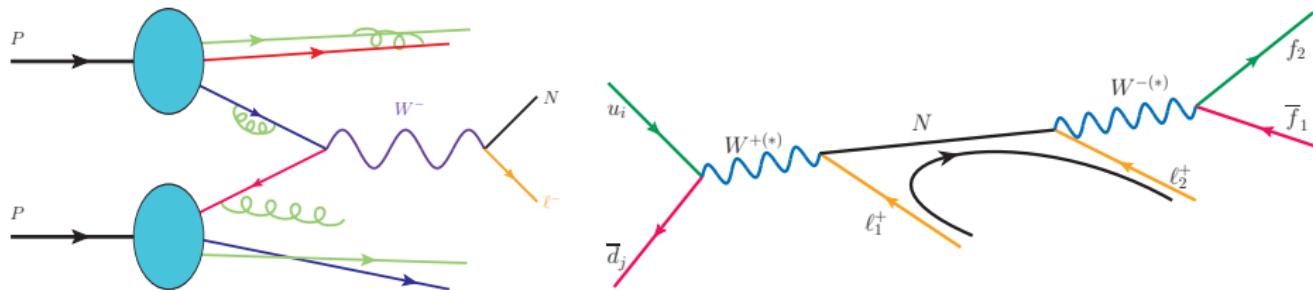
Take away: major improvement in sensitivity! (not just energy and lumi.)

Three sources of improvement

1. New production channels

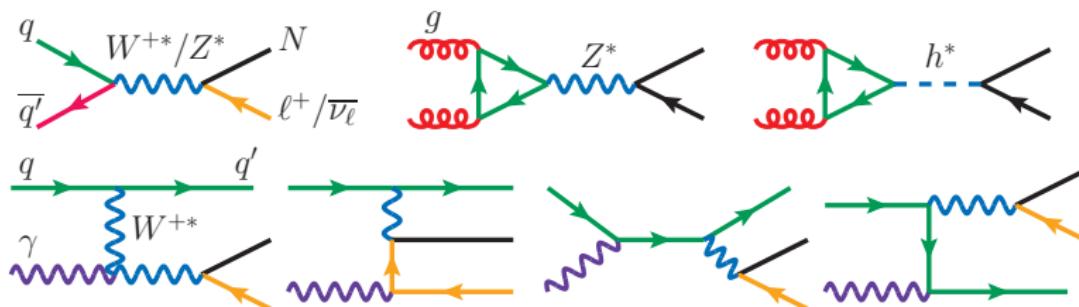
Historically, searches for N relied on $(q\bar{q})$ annihilation

Keung & Senjanovic (PRL'83)

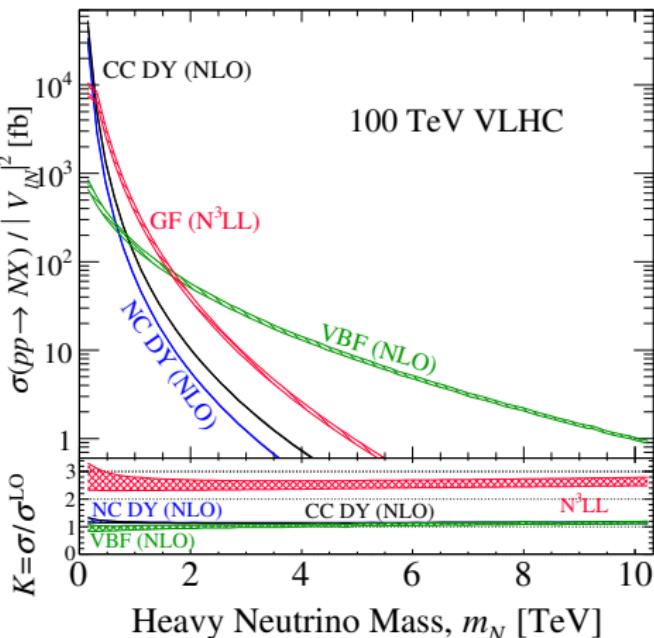
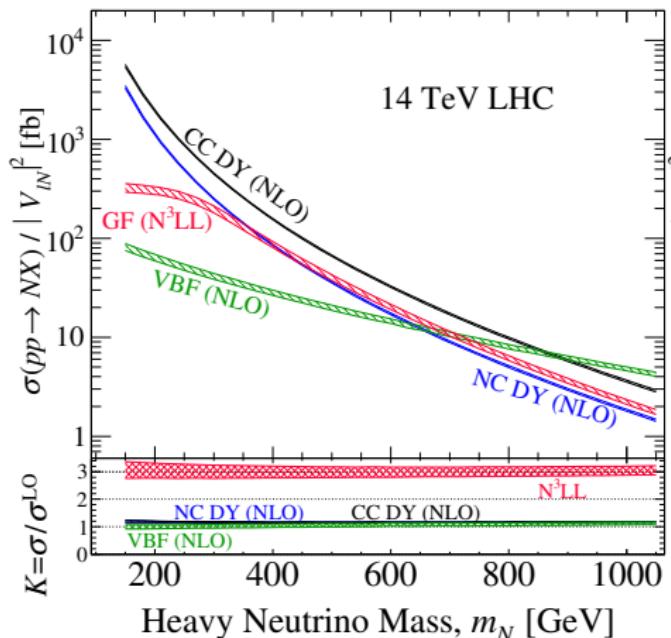


At the LHC, a **canonical** signature for N : $pp \rightarrow \ell_i^\pm \ell_j^\pm + nj + \text{no MET}$

based on seminal works by K&S, del Aguila & Aguilar-Saavedra [0808.2468], and Atre, et al [0901.3589]

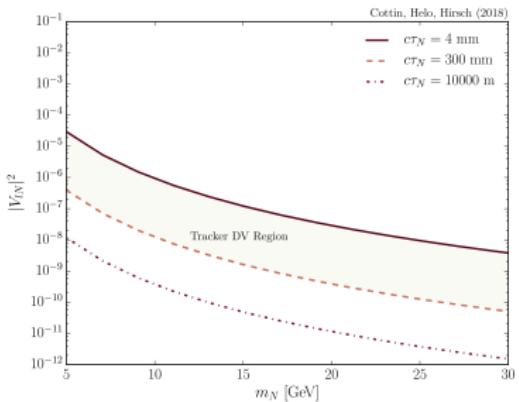
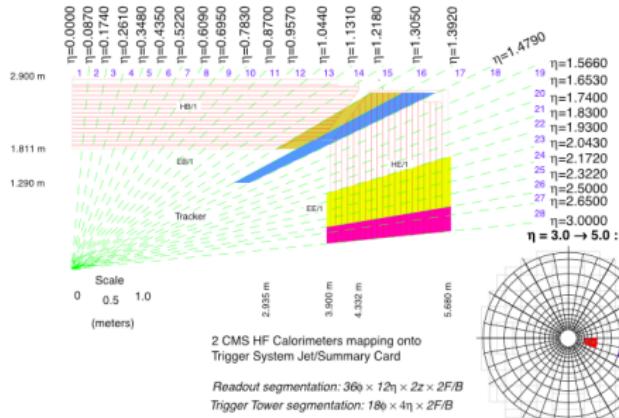


Plotted: Normalized production rate ($\sigma / |V|_N^2$) vs heavy N mass (m_N)



Wild interplay between proton structure and matrix elements!

2. New search strategies (e.g., displaced vertex searches)



Decays of light N through SM weak currents can be very long-lived:

$$\Gamma_{\text{Tot.}} \sim G_F^2 m_N^5 \sum |V|^2 \quad (\text{small } |V| \implies \text{long lifetime!})$$

$$\implies d_0 = \beta c\tau = \frac{\beta c\hbar}{\Gamma_{\text{Tot.}}} \sim \frac{1.45 \text{ m}}{\sum |V|^2} \left(\frac{1 \text{ GeV}}{m_N} \right)$$

(Near) detectors have *finite* detector volume, with radius $< \mathcal{O}(10) \text{ m}$

Many good works, e.g., Cottin, Helo, Hirsch, et al [1801.02734, 1806.05191, 2105.13851]

3. New tools

Searching for heavy Majorana and (pseudo)Dirac neutrinos N at LHC follows any other analysis chain

- BIG PROBLEM/SOLUTION (sterile neutrinos!) ✓
- Signal/bkg simulation with favorite generator ← updates here!
e.g., MadGraph5, Whizard, SHERPA
- Collect data, control regions, unblind, do some statistics ✓

Major effort to support neutrino mass models in your favorite generator

- Universal FeynRules Object (UFO) libs. encode Feynman rules (.py) that work with popular event generators, e.g., MadGraph5, Whizard

Alloul, Christensen, Duhr, Degrande, and Fuks feynrules.irmp.ucl.ac.be

HeavyN_vSMEFTdim6, TypeIISeesaw, EffLRSM, WZPrime, SMWeinberg also available feynrules.irmp.ucl.ac.be/wiki/NLOModels!

HeavyN : The Standard Model + Heavy Neutrinos at NLO in QCD

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In collaboration with:

D. Alva and T. Han [1]; C. Degrande, O. Mattelear, and J. Turner [2]; S. Pascoli and C. Weiland [3, 4]; and V. Cirigliano, W. Dekens, J. de Vries, K. Fuyuto, E. Mere

Usage resources

- For detailed instructions and examples on using the HeavyN UFO libraries, see C. Degrande, et al, [arXiv:1602.06957](#) and S. Pascoli, et al, [arXiv:1812.08750](#) .
- ***New*** For heavy neutrinos in vSMEFT, see V. Cirigliano, et al, [arXiv:2105.11462](#).
- See **Validation** section below for additional information

Citation requests

- For studies of heavy Majorana neutrinos, please consider citing [6] for the Lagrangian and [1, 2] for the Majorana FR/UFO files.
- For studies of heavy Dirac neutrinos, please also consider citing [4].
- ***New*** For studies of heavy neutrinos in vSMEFT, please consider citing [5].

Model Description

Majorana N

This effective/simplified model extends the Standard Model (SM) field content by introducing three right-handed (RH) neutrinos, which are singlets under the SM gauge symmetries. After electroweak symmetry breaking, the Lagrangian with three heavy Majorana neutrinos N^i (for $i=1,2,3$) is given by [6]

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \mathcal{L}_N + \mathcal{L}_{N \text{ Int.}} \quad (1)$$

The first term is the Standard Model Lagrangian. In the mass basis, i.e., after mixing with active neutrinos, the heavy Majorana neutrinos' kinetic and mass terms are

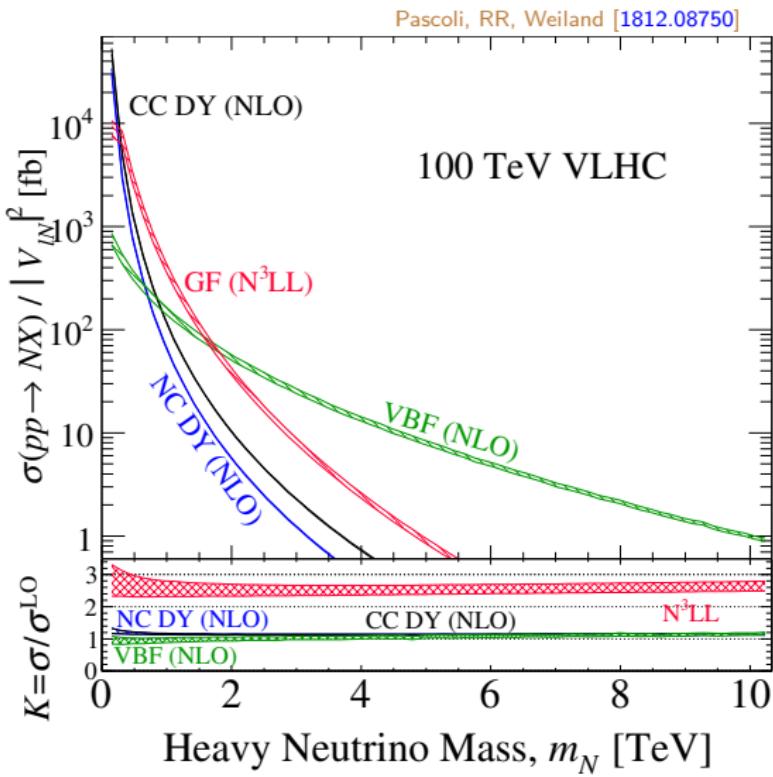
$$\mathcal{L}_N = \frac{1}{2} \overline{N}_k i \not{\partial} N_k - \frac{1}{2} m_{N_k} \overline{N}_k N_k, \quad k = 1, \dots, 3, \quad (1)$$

FeynRules to MadGraph5aMC@NLO

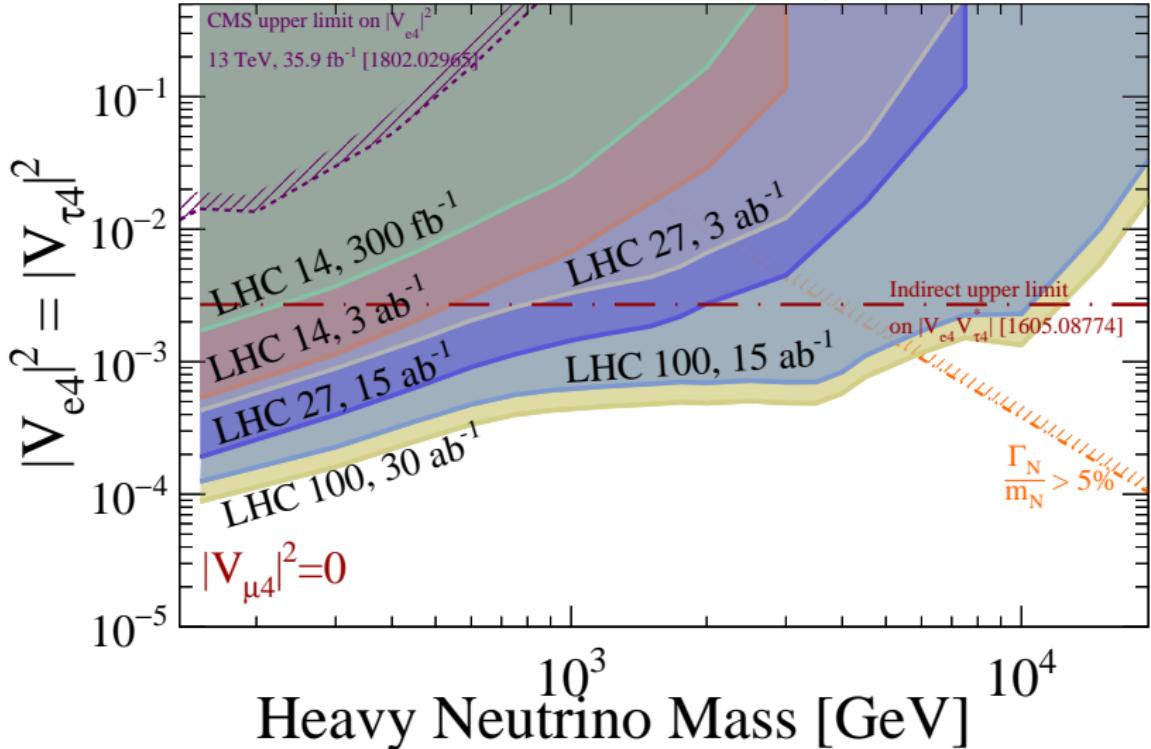
Given a *Universal FeynRules Object* (UFO) file, run `mg5amc` out of the box

```
$ ./bin/mg5_aMC
> import model SM_HeavyN_NLO
> define p = g u c d s b u~ c~
d~ s~ b~ a
> define ell = mu+ mu-
> generate p p > n2 ell [QCD]
> output PP_Nmu_NLO
> launch PP_Nmu_NLO
> order=NLO
> fixed_order=ON
> set LHC 100
> set vmu2 1.0
> set mn2 scan:range(5,1001,25)
> set wn2 auto
```

$\mathcal{O}(10)$ lines to get each curve →



95% Sensitivity - $\text{pp} \rightarrow \tau_h e l_X / 3e / 2e\mu$



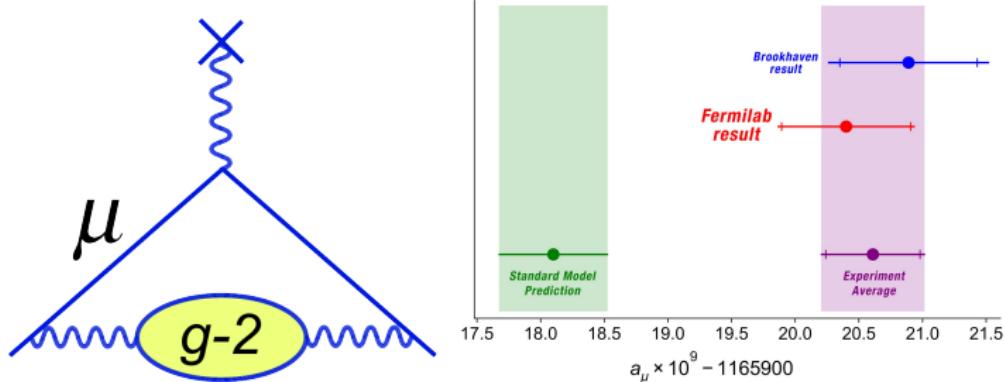
Major improvements $\implies > 10\times$ better sensitivity to LNV + cLFV

Only a few results. See the big paper for various flavor, Dirac vs Majorana, and \sqrt{s} permutations [1812.08750]

New ideas

NEW² sterile neutrinos and Δa_μ

Anomalous magnetic moment of the μ



Fermilab's Muon g-2 has *confirmed* that $a_\mu = (g_\mu - 2)/2$ is *a bit* large

[2104.03281]

$$a_\mu^{\text{average}} = (116\,592\,061 \pm 41) \cdot 10^{-11}$$

$$a_\mu^{\text{SM}} = (116\,591\,810 \pm 43) \cdot 10^{-11}$$

The difference? Large enough to start taking BSM solutions seriously.

$$\Delta a_\mu = (251 \pm 59) \cdot 10^{-11} \text{ or about } 4.2\sigma!$$

Can new N interactions account for this?

Yes, in a surprisingly succinct manner.

ν SMEFT is the Standard Model Effective Field Theory extended by ν_R

$\psi^2 H^3$		$\psi^2 H^2 D$		$\psi^2 H X (+\text{H.c.})$	
$\mathcal{O}_{L\nu H} (+\text{H.c.})$	$(\bar{L}\nu_R)\bar{H}(H^\dagger H)$	$\mathcal{O}_{H\nu}$	$(\bar{\nu}_R\gamma^\mu\nu_R)(H^\dagger i\overleftrightarrow{D}_\mu H)$	$\mathcal{O}_{\nu B}$	$(\bar{L}\sigma_{\mu\nu}\nu_R)\bar{H}B^{\mu\nu}$
		$\mathcal{O}_{H\nu e} (+\text{H.c.})$	$(\bar{\nu}_R\gamma^\mu e)(\bar{H}^\dagger iD_\mu H)$	$\mathcal{O}_{\nu W}$	$(\bar{L}\sigma_{\mu\nu}\nu_R)\tau^I \bar{H}W^{I\mu\nu}$
$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$		$(\bar{L}R)(\bar{L}R) (+\text{H.c.})$	
$\mathcal{O}_{\nu\nu}$	$(\bar{\nu}_R\gamma^\mu\nu_R)(\bar{\nu}_R\gamma_\mu\nu_R)$	$\mathcal{O}_{L\nu}$	$(\bar{L}\gamma^\mu L)(\bar{\nu}_R\gamma_\mu\nu_R)$	$\mathcal{O}_{L\nu Le}$	$(\bar{L}\nu_R)e(\bar{L}e)$
$\mathcal{O}_{e\nu}$	$(\bar{e}\gamma^\mu e)(\bar{\nu}_R\gamma_\mu\nu_R)$	$\mathcal{O}_{Q\nu}$	$(\bar{Q}\gamma^\mu Q)(\bar{\nu}_R\gamma_\mu\nu_R)$	$\mathcal{O}_{L\nu Qd}$	$(\bar{L}\nu_R)e(\bar{Q}d)$
$\mathcal{O}_{u\nu}$	$(\bar{u}\gamma^\mu u)(\bar{\nu}_R\gamma_\mu\nu_R)$			$\mathcal{O}_{LdQ\nu}$	$(\bar{L}d)e(\bar{Q}\nu_R)$
$\mathcal{O}_{d\nu}$	$(\bar{d}\gamma^\mu d)(\bar{\nu}_R\gamma_\mu\nu_R)$				
$\mathcal{O}_{duwe} (+\text{H.c.})$	$(\bar{d}\gamma^\mu u)(\bar{\nu}_R\gamma_\mu e)$				
$(\bar{L}R)(\bar{R}L)$		$(\bar{L} \cap B) (+\text{H.c.})$		$(\bar{L} \cap \mathcal{B}) (+\text{H.c.})$	
$\mathcal{O}_{Qu\nu L} (+\text{H.c.})$	$(\bar{Q}u)(\bar{\nu}_R L)$	$\mathcal{O}_{\nu\nu\nu\nu}$	$(\bar{\nu}_R^\ell\nu_R)(\bar{\nu}_R^\ell\nu_R)$	$\mathcal{O}_{QQd\nu}$	$\epsilon_{ij}\epsilon_{\alpha\beta\sigma}(Q_\alpha^\ell C Q_\beta^\ell)(d_\sigma C\nu_R)$
				$\mathcal{O}_{udd\nu}$	$\epsilon_{\alpha\beta\sigma}(u_\alpha C d_\beta)(d_\sigma C\nu_R)$

Table 1: The complete basis of dimension-six operators involving ν_R taken from Ref. [24]. The operators are expressed in terms of a column vector of n gauge singlet fields, ν_R , and of SM fields, the lepton and Higgs doublets, L and H , the quark left-handed doublet $Q = (u_L, d_L)^T$, and the right-handed fields e , u , and d .

Unexpectedly, only one ν SMEFT can generate the right Δa_μ

$$\mathcal{L}_{H\nu e} \approx \frac{gv^2}{2\sqrt{2}\Lambda^2} \sum_{k=1}^3 [\bar{C}_{H\nu e}]_{k\ell} (\bar{N}_k \gamma^\mu P_R \ell_R) W_\mu^+ (1 + \frac{h}{v})^2 + \text{H.c.}$$

This generates Δa_μ of the form

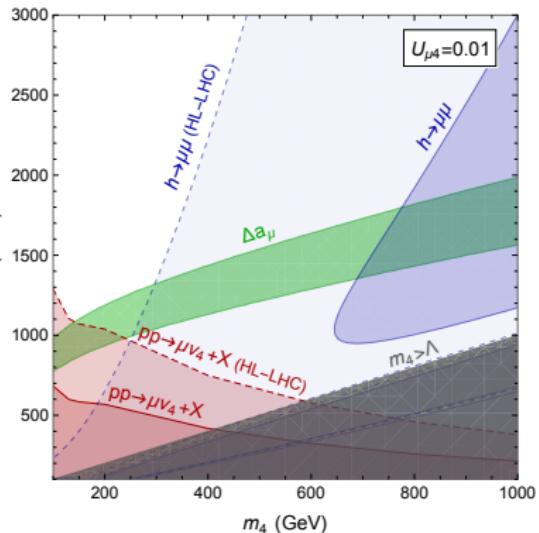
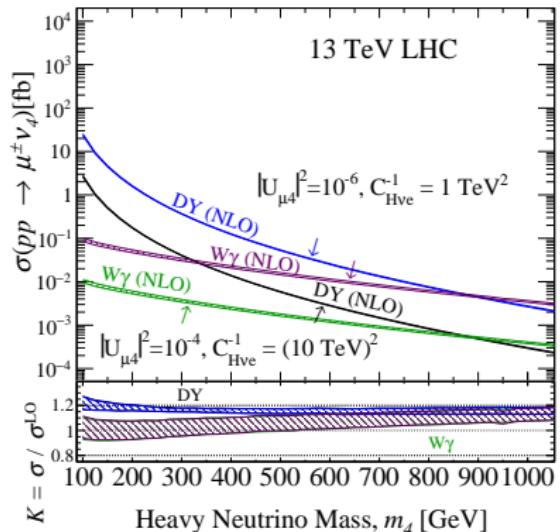
$$\Delta a_\mu \sim -\frac{2m_\mu m_N}{(4\pi)^2 \Lambda^2} \text{Re} \left(V_{\mu N} [\bar{C}_{H\nu e}]_{N\mu} \right)$$

(see [2105.11462] for exact formula!)

Δa_μ at the LHC

We created a new UFO HeavyN_vSMEFTdim6 containing $\mathcal{O}_{H\nu e}$

Already available from the FeynRules UFO database: feynrules.irmp.ucl.ac.be/wiki/HeavyN



Conclusion: If N are involved in Δa_μ , then expect something in

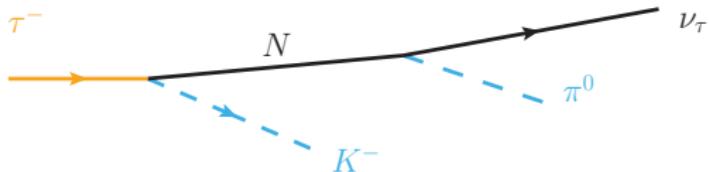
$$pp \rightarrow N\mu^\pm + X \text{ and } H \rightarrow \mu^+ \mu^-$$

in Run III data and at the HL-LHC (see the paper for more details! [\[2105.11462\]](#))

In development³ ultra light sterile neutrinos

³ Fernandez Martinez, Hernandez, Jeon, Kulkarni, Lopez, RR [In Progress]

Question: How light N can accelerator experiments see?

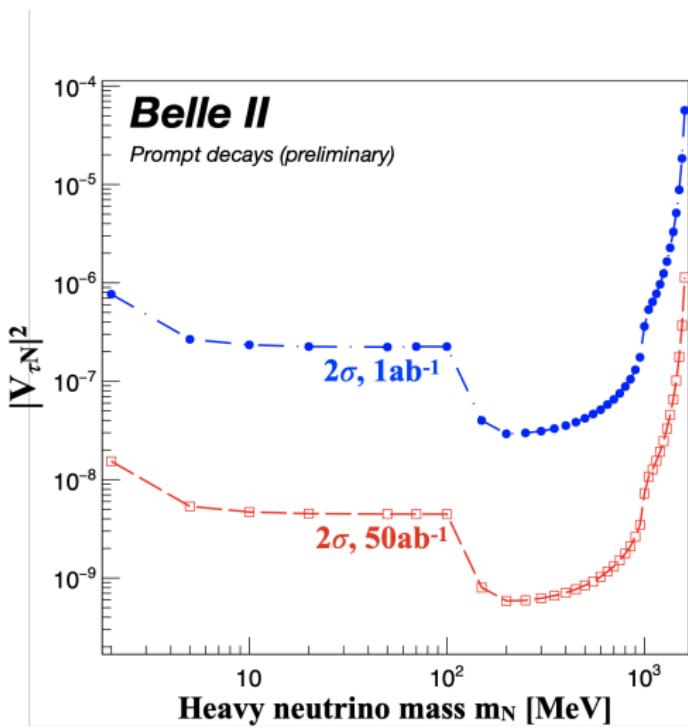


Answer: Pretty small!

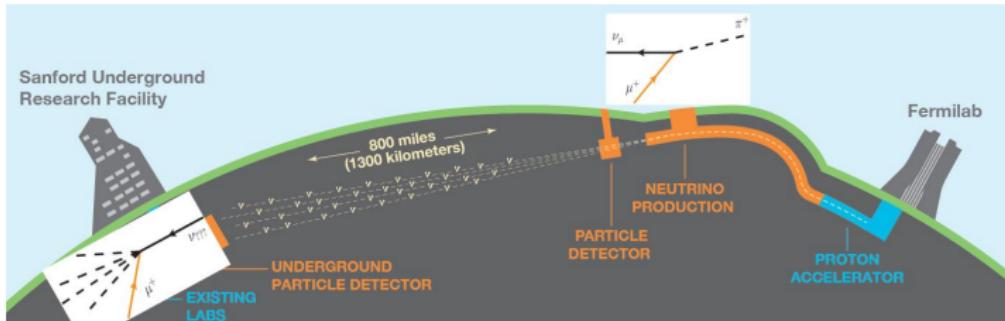
- Low- \sqrt{s} colliders are meson and τ factories!
- Ultra-high lumi. for ultra-tiny masses and mixing
- Competitive with beam dumps and meson factories

e.g., Bondarenko, et al [1805.08567]; de Vries, et al

[2010.07305]



Summary



Big picture: ν unambiguously point the existence of new physics!!

Active research community using accelerators to investigate how and why some matter (ν) is *much* lighter than others

Outlook: is incredibly encouraging!

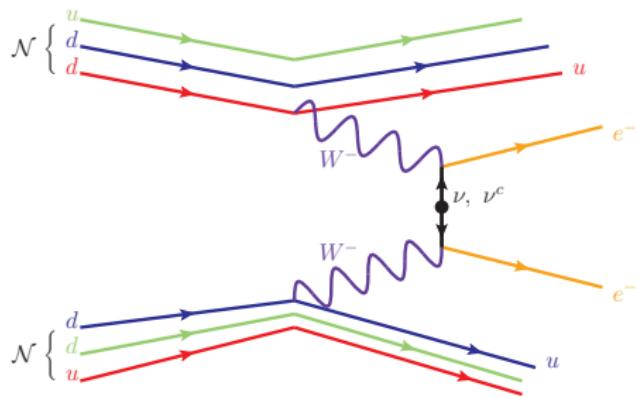
- The LHC has collected only < 5% of full dataset
- New accelerator-based experiments are coming online
- New ideas are creating new windows into the nature of ν

Thank you.

Backup: Weinberg Opterator

A fun idea: is it possible to see the neutrinoless $\beta\beta$ process ($0\nu\beta\beta$) at accelerators?

Fuks, Neundorf, Peters, RR, Saimpert [2011.02547, 2012.09882]



Why? Colliders, beam dumps, etc., can access μ and τ sectors!

Many ways to explain $m_\nu \neq 0$, so take an effective field theory approach:

The **Weinberg operator** is the only SMEFT operator at $d = 5$: Weinberg ('97)

$$\mathcal{L} = \frac{C_5^{\ell\ell'}}{\Lambda} [\Phi \cdot \bar{L}_\ell^c] [L_{\ell'} \cdot \Phi] \xrightarrow{\text{low energies (EWBS)}} \frac{1}{2} \underbrace{\frac{C_5^{\ell\ell'}}{\Lambda} \langle \Phi \rangle^2}_{=m_{\ell\ell'}} \times \bar{\nu}_{L\ell}^c \nu_{L\ell'}$$

Can be generated in **many** ways at tree- and loop-level

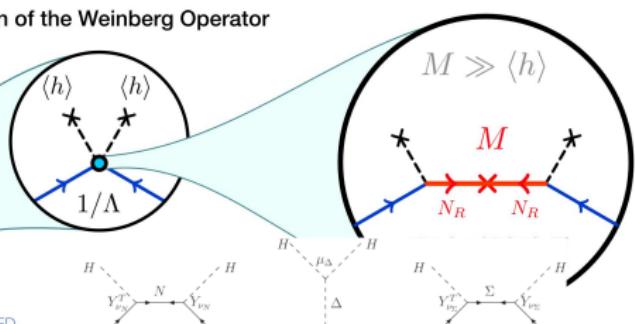
Eg. Ma ('98), Bonnet, et al [1204.5862]

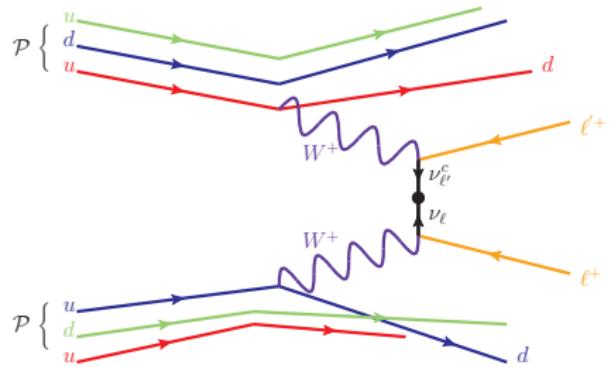
Importantly, after EWSB, generates a Majorana mass matrix for ν

$$m_{\ell\ell'} = C_5^{\ell\ell'} \langle \Phi \rangle^2 / 2\Lambda \quad \leftarrow (\text{flavor basis!})$$

Type-I See-Saw Completion of the Weinberg Operator

one interesting way to generate the Weinberg operator is if a heavy gauge-singlet fermion has Yukawa couplings to the left-handed leptons





The helicity amplitude for the $0\nu\beta\beta$ process $q\bar{q}' \rightarrow \ell_1^+\ell_2^+\bar{f}f'$ is

$$\mathcal{M}_{LNV} = J_{f_1 f'_1}^\mu J_{f_2 f'_2}^\nu \Delta_{\mu\alpha}^W \Delta_{\nu\beta}^W \underbrace{T_{LNV}^{\alpha\beta}}_{\text{lepton current}} \mathcal{D}(p_\nu)$$

Difficult to simulate events since Weinberg op. modifies propagator of ν_ℓ

modern Monte Carlo tools work in mass basis and do not like the idea of modifying $\langle 0 | \bar{\nu}_\ell' \nu_\ell | 0 \rangle$

$$\frac{\nu_\ell(p)}{p} \frac{\nu_{\ell'}^c(-p)}{p} = \frac{ip}{p^2} \frac{-iC_5^{\ell\ell'} v^2}{\Lambda} \frac{ip}{p^2} = \frac{im_{\ell\ell'}}{p^2}$$

Solution: Treat vertex as a particle! Invent unphysical Majorana fermion with (small) mass $m_{\ell\ell'}$ that couples to all lepton flavors

recovers right behavior!

$$T_{LNV}^{\alpha\beta} \mathcal{D}(p_\nu) \propto \gamma^\alpha P_L \frac{i(p + m_{\ell\ell'})}{p^2 - m_{\ell\ell'}^2} \gamma^\beta P_R = \gamma^\alpha P_L \frac{i m_{\ell\ell'}}{p^2} P_L \gamma^\beta \times \left[1 + \mathcal{O}\left(\left|\frac{m_{\ell\ell'}}{p^2}\right|\right) \right]$$

Plotted: Normalized production rate ($C_5 = 1$) vs scale (Λ)

w/ Fuks, Neundorf, Peters, Sainpert [2012.09882]

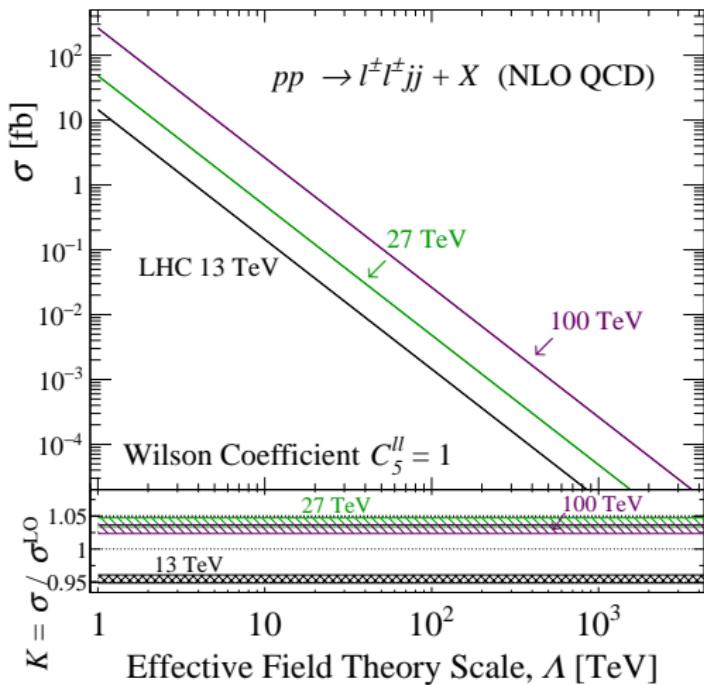
Full $2 \rightarrow 4$ calculation at NLO(+PS)
in QCD is more involved

Used mg5amc + NEW SMWeinberg UFO libraries

Driven by $W_0^+ W_0^+$ scattering
 $\hat{\sigma}(W^+ W^+ \rightarrow \ell^+ \ell^+) \sim \frac{|C_5^{\ell\ell}|^2}{18\pi\Lambda^2}$

Once σ is obtained for a “high”
scale, i.e., $C_5^{\ell\ell'} = 1, \Lambda = 200$ TeV,
rescale for other Λ/C_5 .

C_5^{ee}/Λ is heavily constrained. **What**
can the LHC say about $C_5^{\ell\ell'}$?

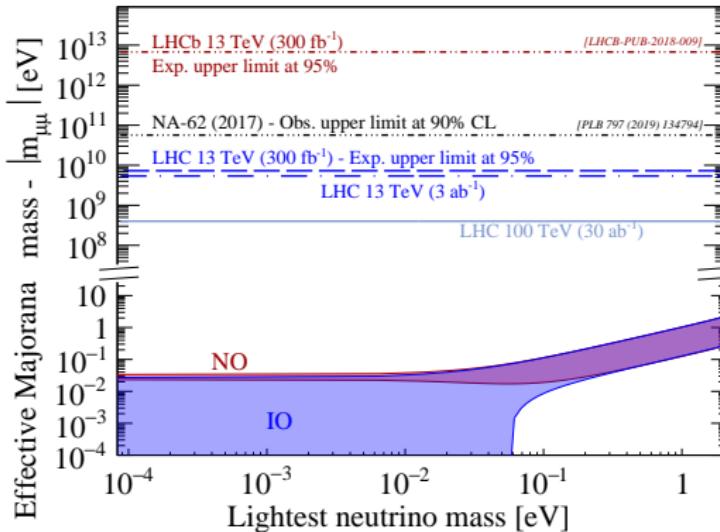


With a VBS-style analysis $\mathcal{L} = 300$ (3000) fb^{-1}

$$\Lambda / |C_5^{\mu\mu}| \lesssim 8.3 \text{ (11)} \text{ TeV} \implies |m_{\mu\mu}| \gtrsim 7.3 \text{ (5.4)} \text{ GeV}$$

Plotted: Allowed and projected reach of $|m_{\mu\mu}|$ vs lightest ν mass

$$|m_{\ell\ell'}| = |C_5^{\ell\ell'}| \langle \Phi \rangle^2 / 2\Lambda = \left| \sum_{k=1}^3 U_{\ell k} m_{\nu_k} U_{\ell' k} \right|$$



Competitive race between accelerator-based experiments; all analyses can be improved!